

# Dense gas tracers and star formation laws:

Multiple transition CS lines  
in nearby active star-forming galaxies

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# Which gases are forming stars?

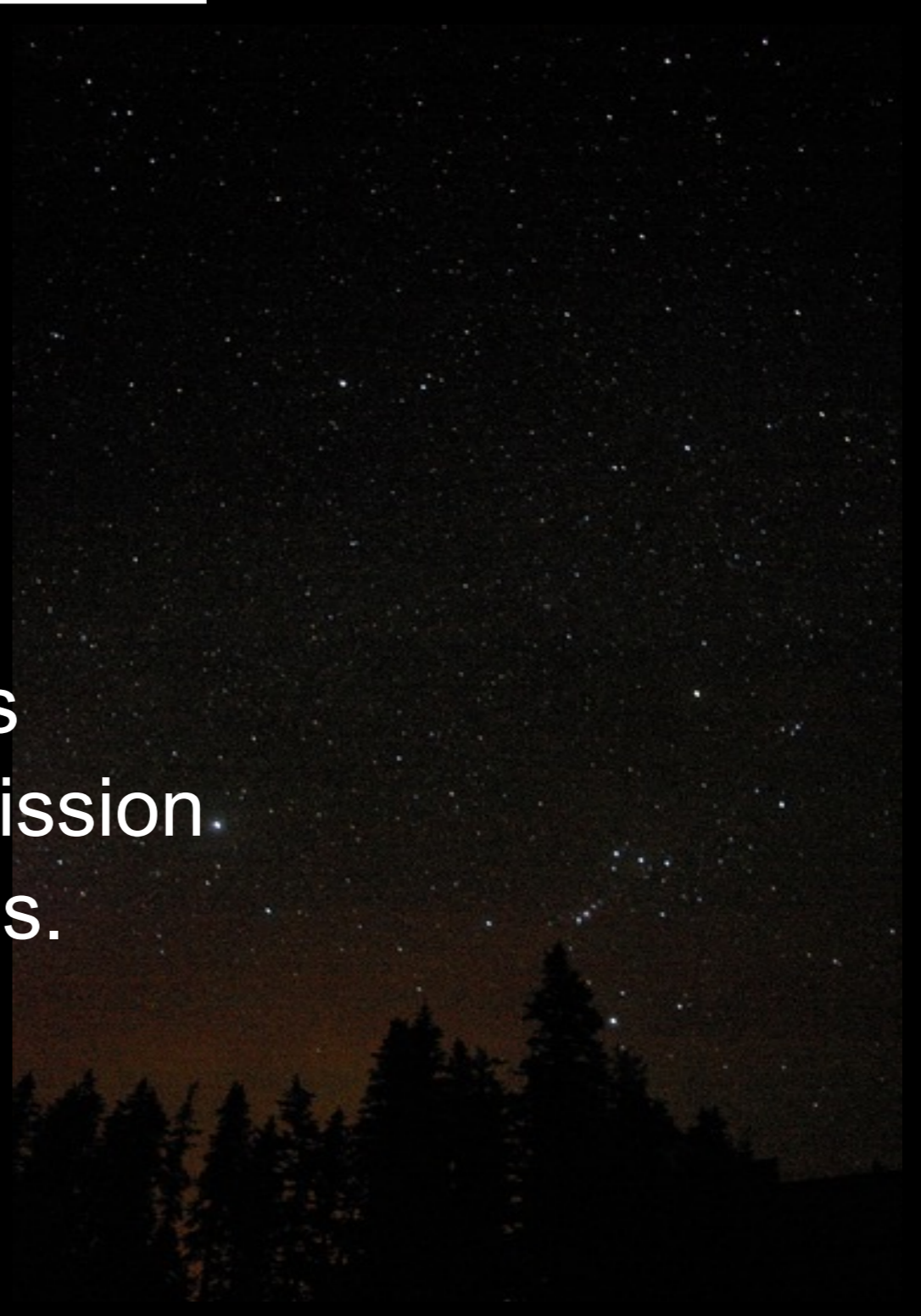
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et al.



# Outline

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- Background
- Gas tracers and Star formation
- Star formation laws
  
- Surveys and Results
- Multiple-J CS surveys in galaxies
- Star formation vs. dense gas emission
- DeMoGas and Excitation analysis.
  
- Summary

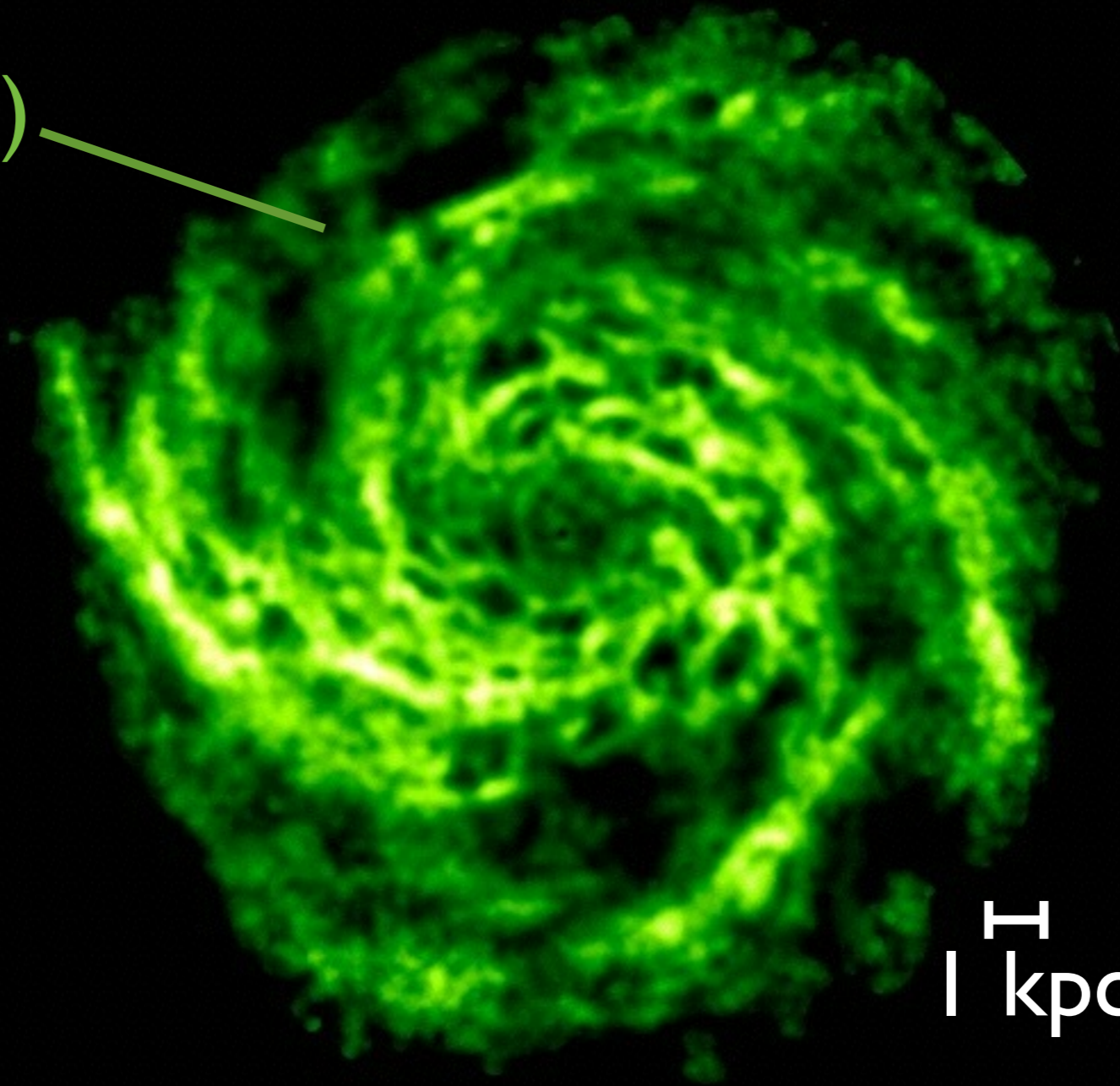


# Which gases are forming stars?

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IC 342

HI (atomic gas)



THINGS

1 kpc

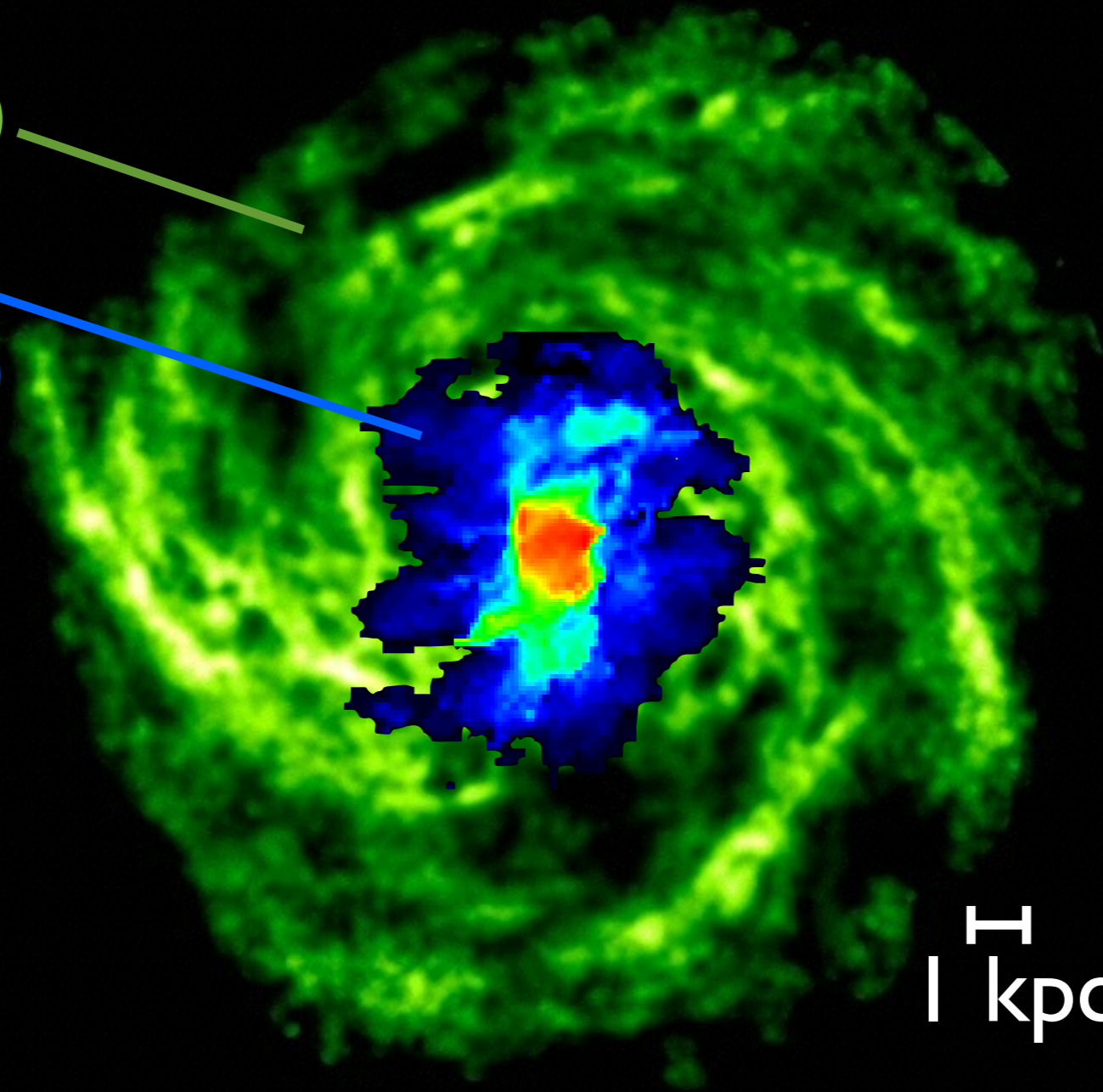
# Which gases are forming stars?

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IC 342

HI (atomic gas)

$^{12}\text{CO } J=1-0$   
(molecular gas)



THINGS

NRAO 12m

1 kpc



# Which gases are forming stars?

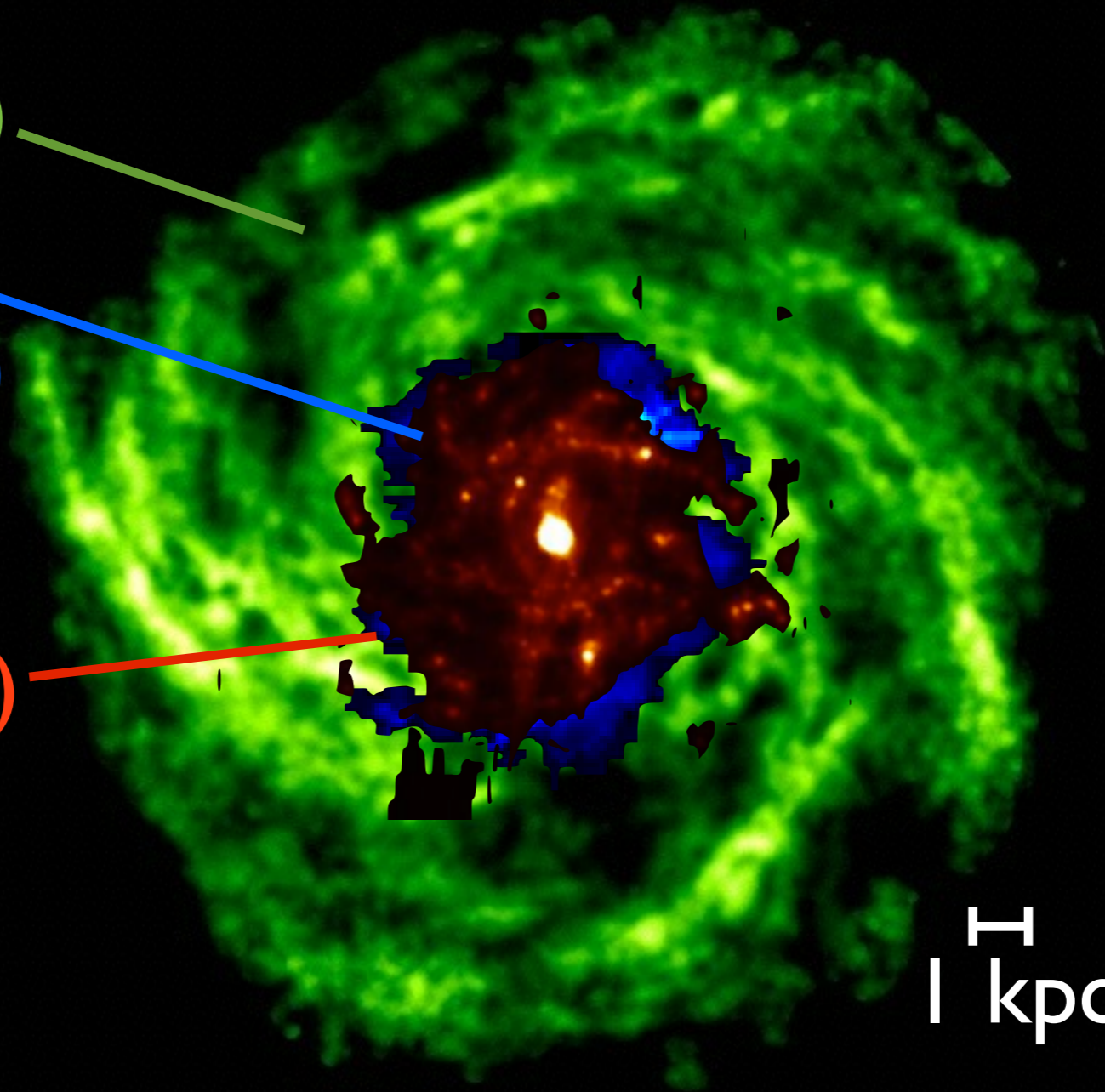
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IC 342

HI (atomic gas)

$^{12}\text{CO } J=1-0$   
(molecular gas)

IR emission  
(star formation)



THINGS

NRAO 12m

Spitzer 70um

1 kpc

On kpc scales, SFR is related to  $\text{H}_2$  gas, rather than HI

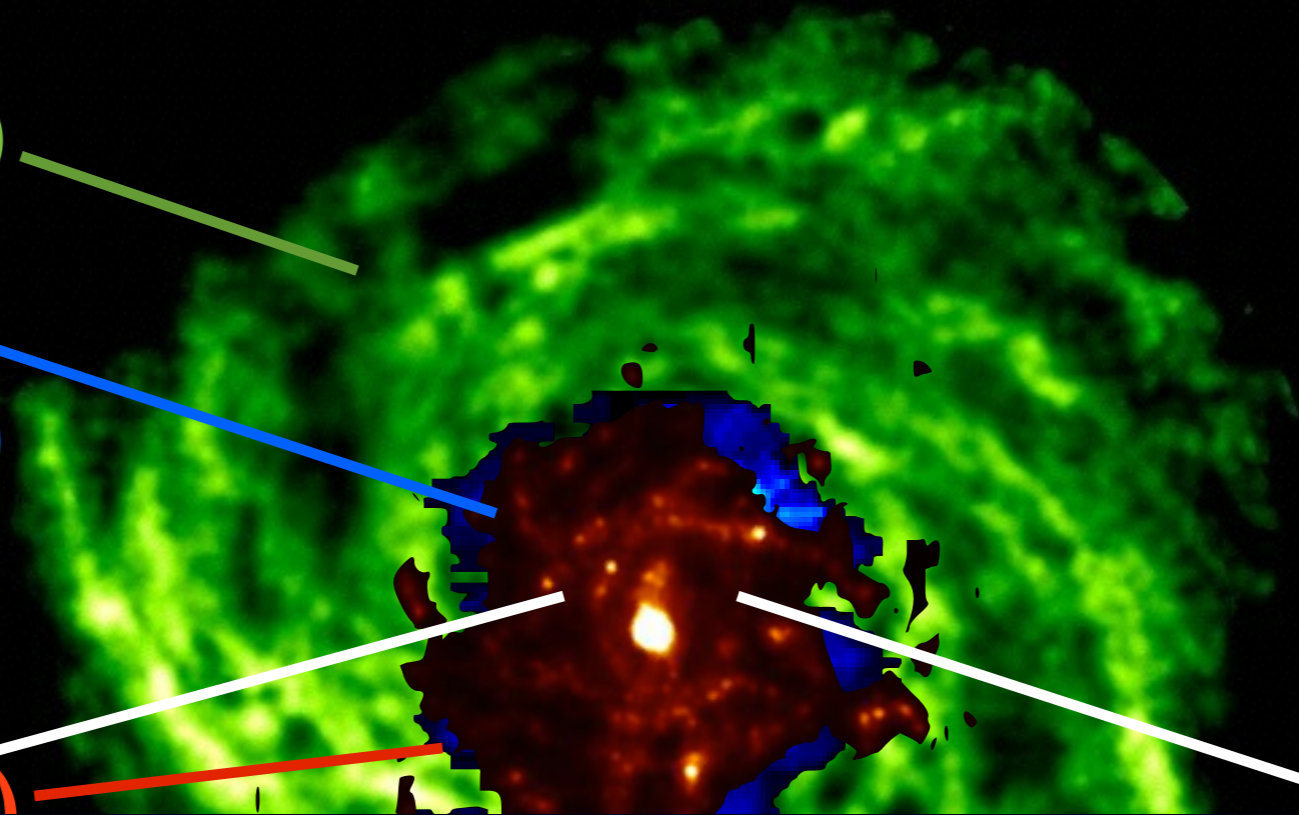
# Which gases are forming stars?

IC 342

HI (atomic gas)

$^{12}\text{CO } J=1-0$   
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IR emission  
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THINGS

NRAO 12m

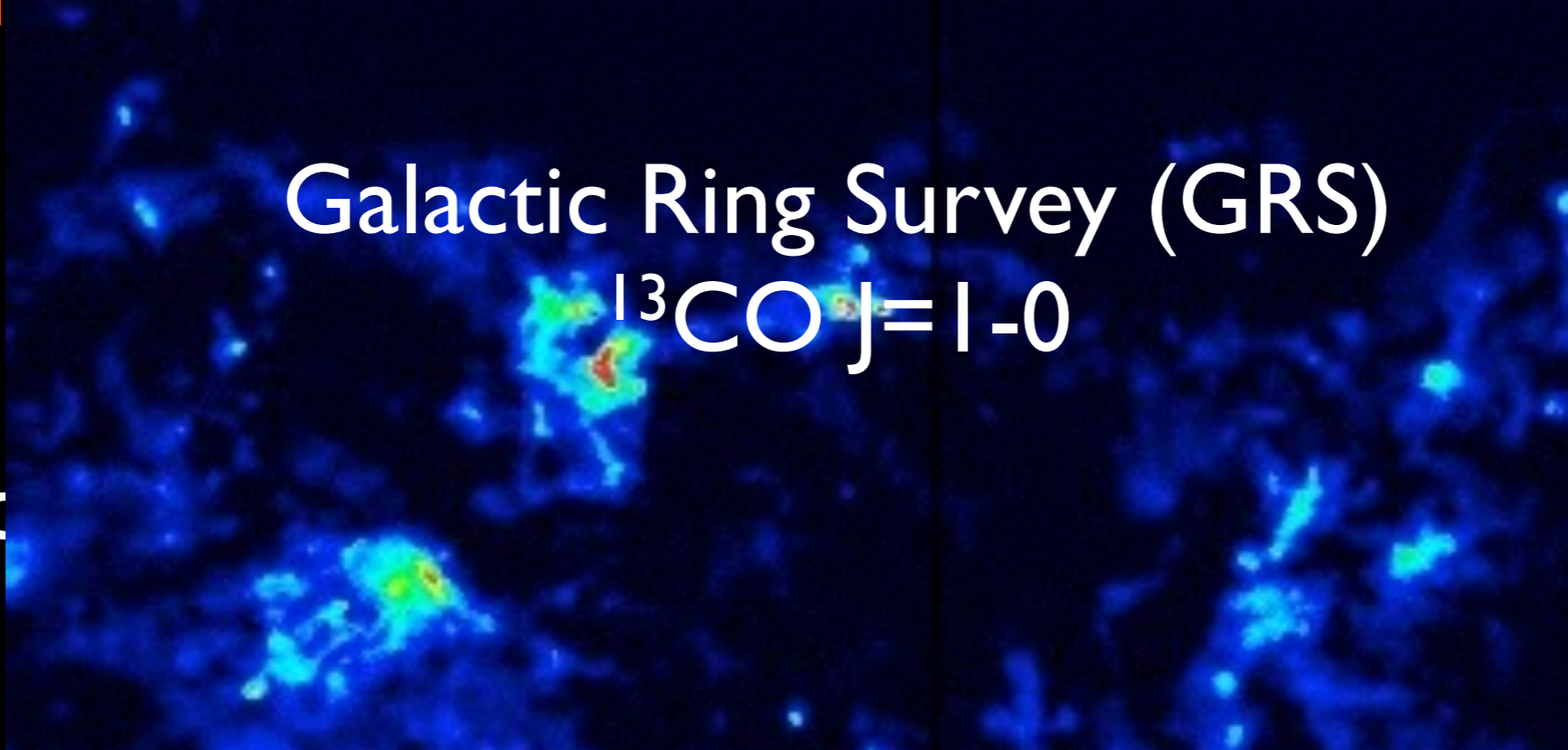
Spitzer 70um

Galactic Ring Survey (GRS)

$^{13}\text{CO } J=1-0$

On kpc

than HI





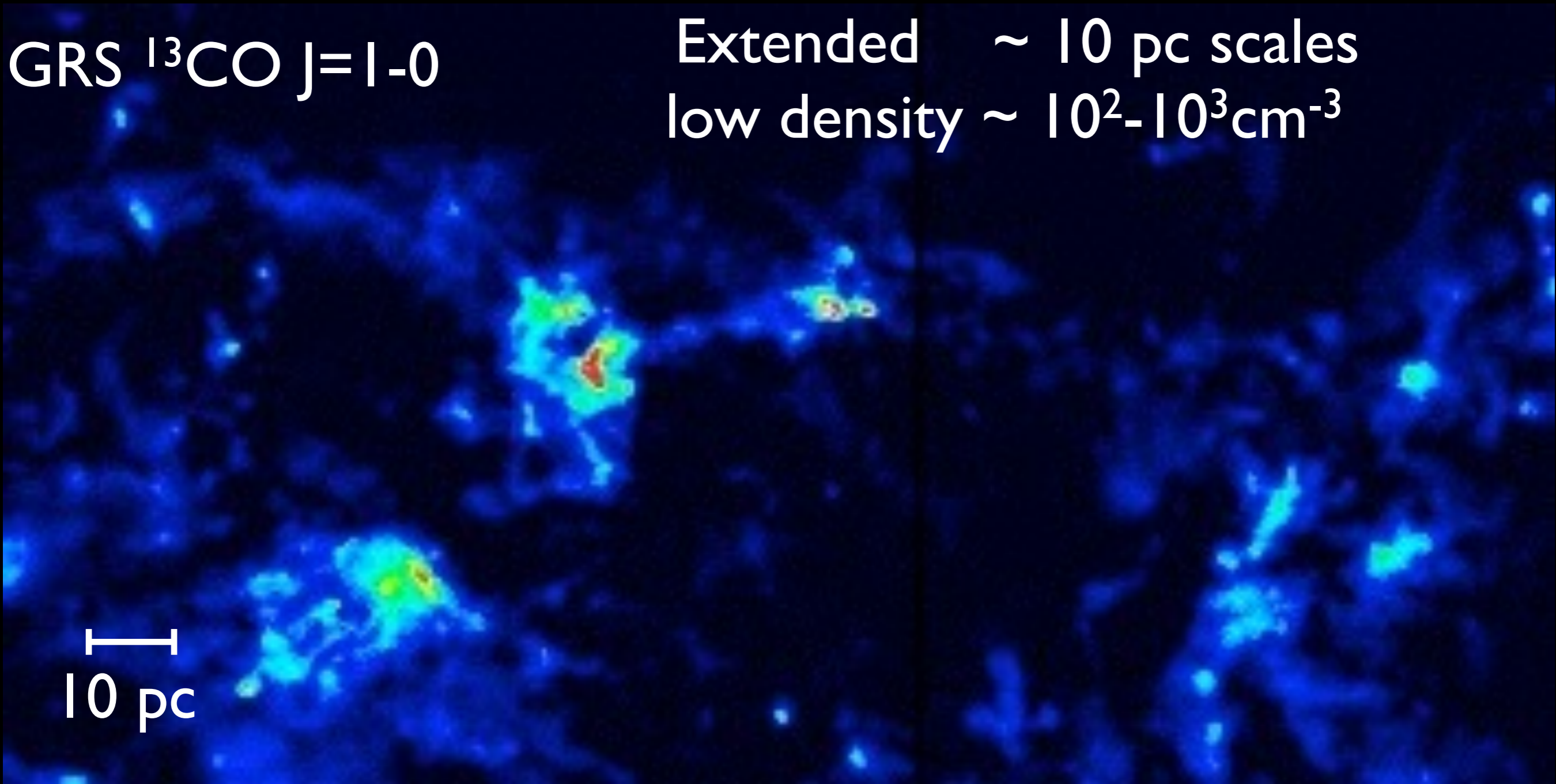
# Which gases are forming stars? - Galactic view

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GRS  $^{13}\text{CO}$  J=1-0

Extended  $\sim 10$  pc scales  
low density  $\sim 10^2$ - $10^3$  cm $^{-3}$

┌──┐  
10 pc





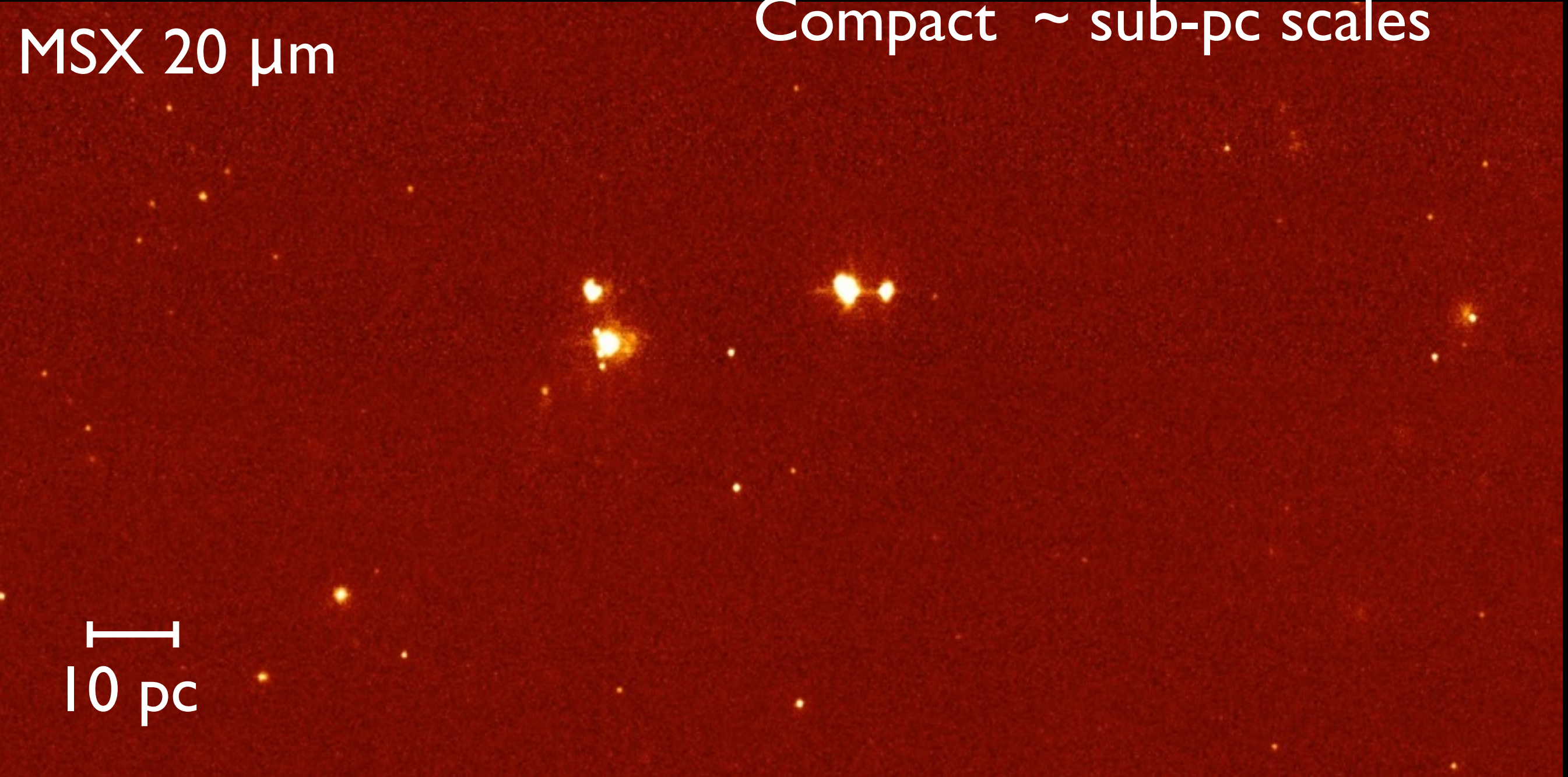
# Which gases are forming stars? - Galactic view

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MSX 20  $\mu\text{m}$

Compact  $\sim$  sub-pc scales

—  
10 pc





# Which gases are forming stars? - Galactic view

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GRS CS J=2-1

Compact  $\sim$  sub-pc scales  
High density  $\sim 10^4 - 10^6 \text{cm}^{-3}$

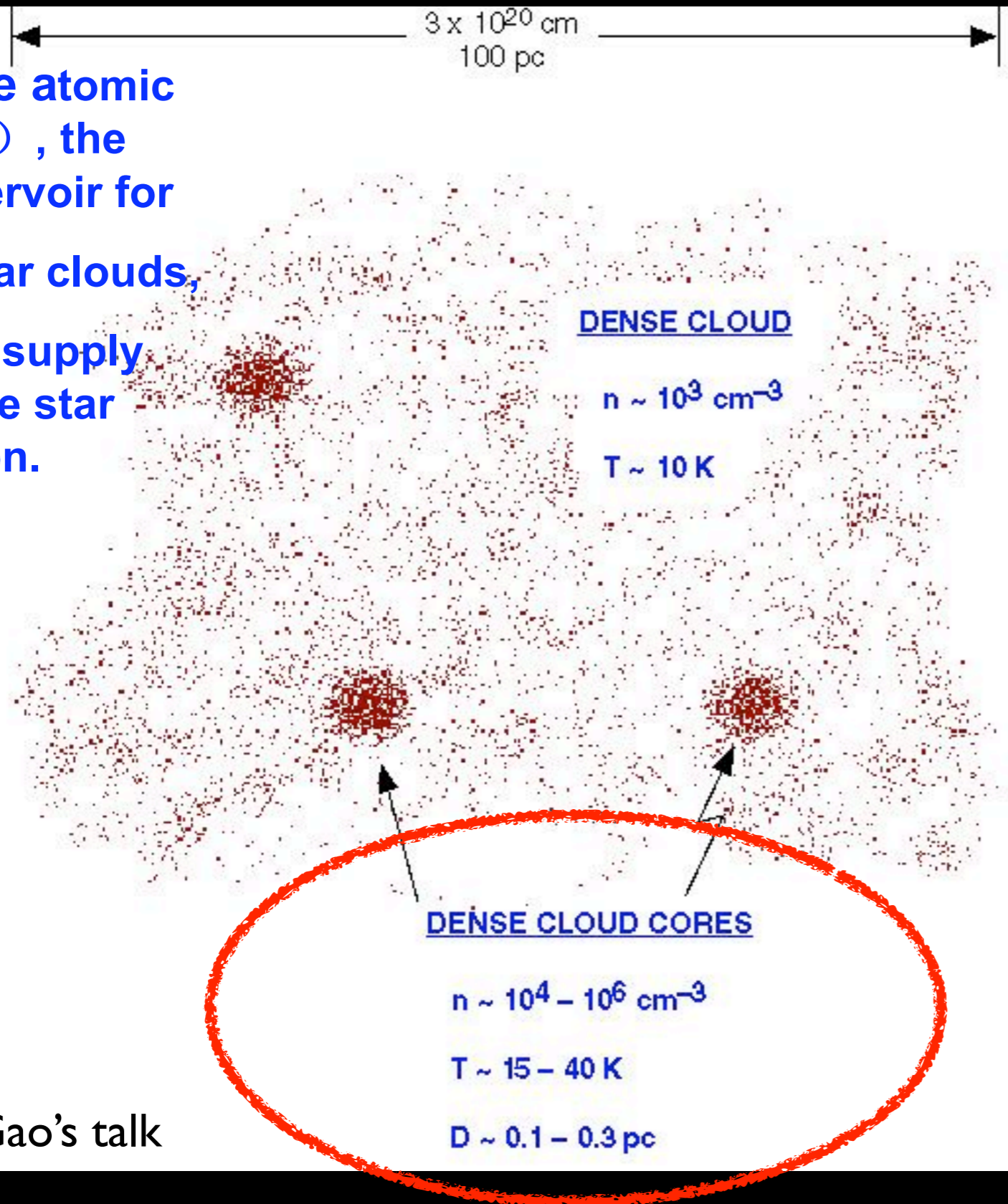
10 pc

The image displays a wide-field view of star-forming regions in the Galactic plane, captured using the GRS CS J=2-1 line. The emission is shown in shades of blue and cyan against a dark background. Several distinct, bright spots are visible, representing compact regions of high density. A scale bar in the bottom left corner indicates a length of 10 parsecs (pc).

# Stars are forming in dense molecular gas cores

Diffuse atomic gas (HI), the gas reservoir for molecular clouds, and the supply for future star formation.

PDRs



GMCs:

$n(\text{H}_2) \sim 10^2 - 10^3 \text{ cm}^{-3}$   
 $T_{\text{kin}} \sim 10 - 20 \text{ K}$   
 $D \sim 10 - 100 \text{ pc}$

Dense cores:

$n(\text{H}_2) \sim 10^4 - 10^6 \text{ cm}^{-3}$   
 $T_{\text{kin}} \sim 15 - 100 \text{ K}$   
 $D \sim 0.1 - 0.3 \text{ pc}$   
self-gravity bound



# Dense gas tracers

When  $n(\text{H}_2) > n_{\text{crit}}$ :

Collisional excitation dominant.

Easily be thermalized.

$$n_{\text{crit}} = \frac{\sum_{l < u} A_{ul}}{\sum_{l \neq u} C_{ul}}$$

$$n_{\text{crit}}(\text{HCN}) : 10^4 \sim 10^7 \text{ cm}^{-3}$$

$$n_{\text{crit}}(\text{HCO}^+) : 10^4 \sim 10^6 \text{ cm}^{-3}$$

$$n_{\text{crit}}(\text{CO}) : 10^2 \sim 10^5 \text{ cm}^{-3}$$

$$n_{\text{crit}}(\text{CS}) : 10^4 \sim 10^6 \text{ cm}^{-3}$$

**HCN** : IR-pumping, XDR, chemistry on  $T_{\text{kin}}$ .

e.g. Weiss et al. 2008; Graci-Carpio et al. 2006; Lintott & Viti 2006; Baan et al. 2008

**HCO<sup>+</sup>** : Shock, ionisation fields, etc.

e.g. Dickinson et al. 1980; Dickmann et al. 1992; Papadopolous et al. 2007

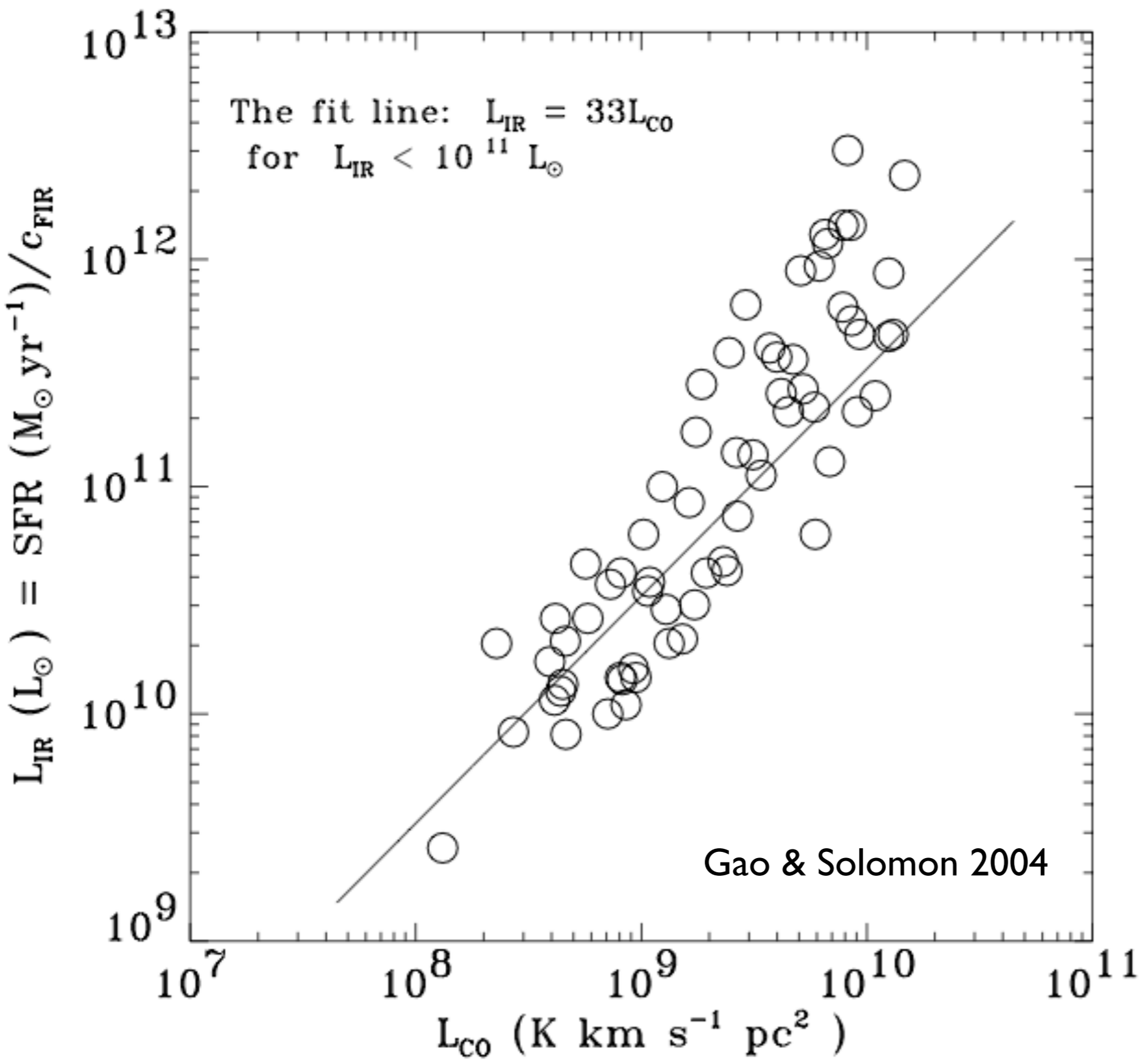
**High-J CO** : Do not trace cold and dense gas.

**CS** : Weaker emission (1/3-1/4 of HCN intensity)

**The best?** Less contaminated. Stable abundance.

e.g. Charnley 1997; Martín et al. 2008; 2009

# $L'_{\text{gas}}-L_{\text{IR}}$ correlations -- CO 1-0 ( $n_{\text{crit}} \sim 4 \times 10^2 \text{cm}^{-3}$ )

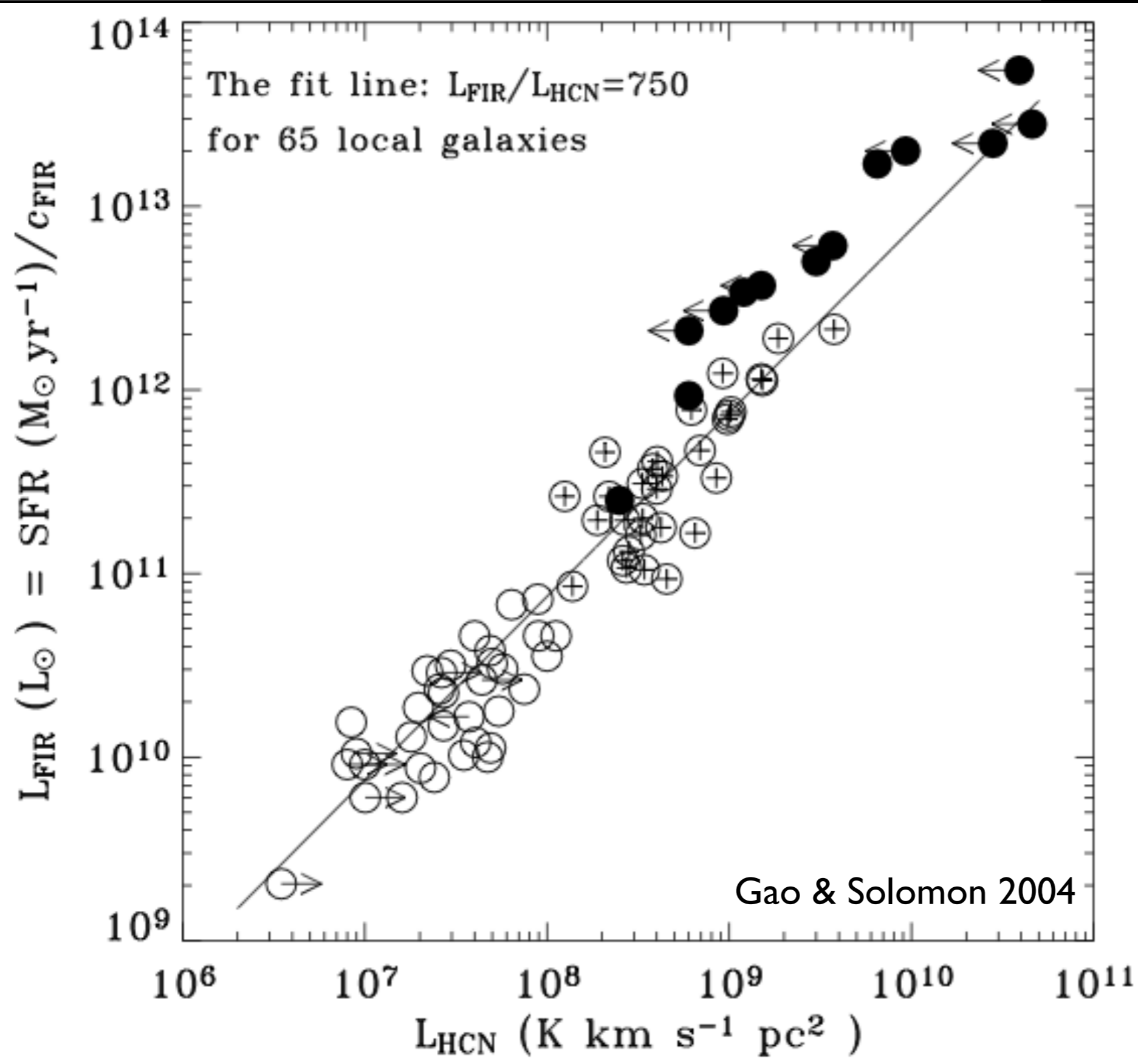


Slope  $\sim 1.4$

$L'_{\text{gas}} \propto M_{\text{gas}}$   
 $L_{\text{IR}} \propto \text{SFR}$



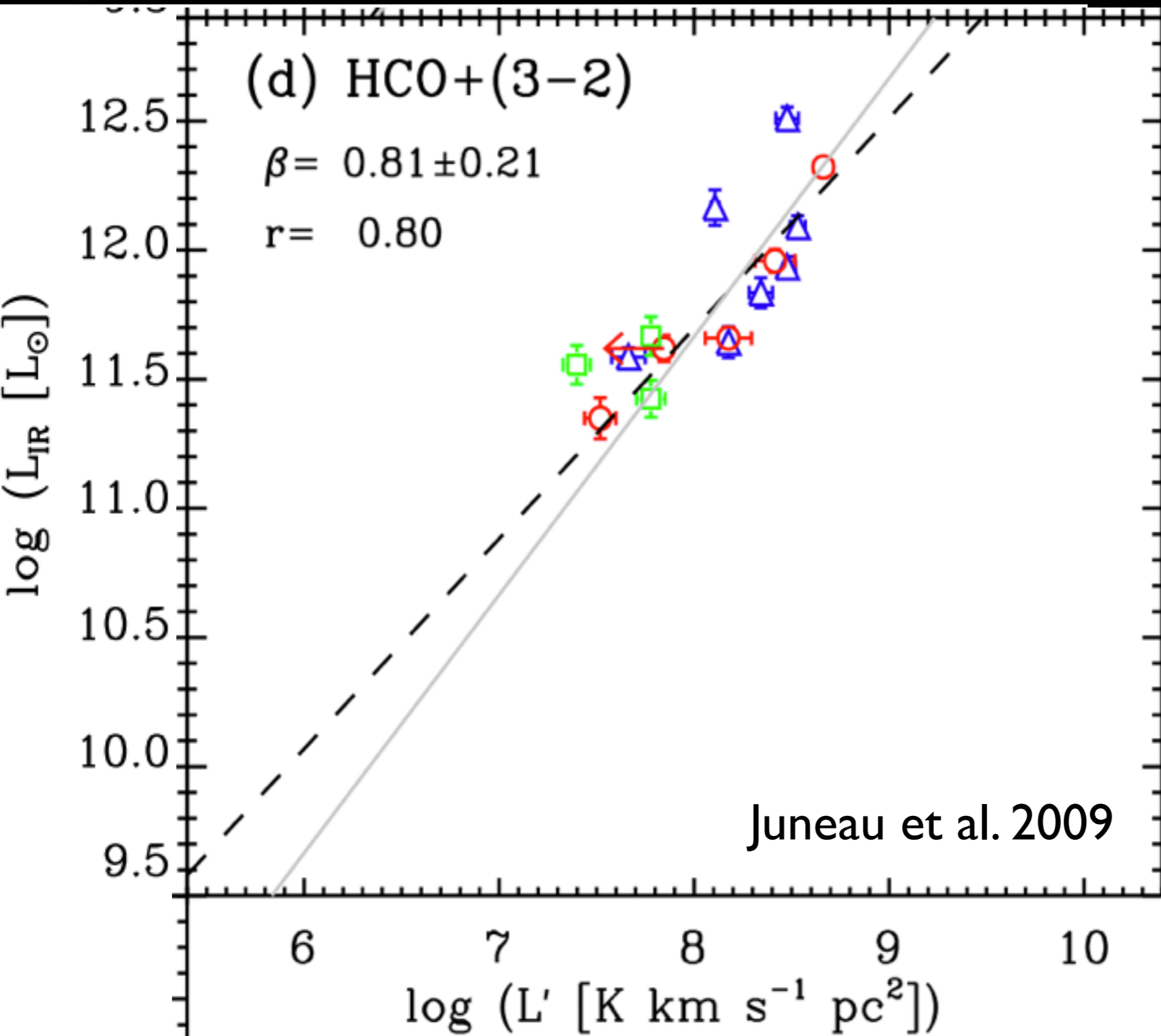
# $L'_{\text{gas}}-L_{\text{IR}}$ correlations -- HCN 1-0 ( $n_{\text{crit}} \sim 2 \times 10^5 \text{cm}^{-3}$ )



Slope=1

$L'_{\text{gas}} \text{ -- } M_{\text{gas}}$   
 $L_{\text{IR}} \text{ -- } \text{SFR}$

# $L'_{\text{gas}}-L_{\text{IR}}$ correlations -- $\text{HCO}^+$ 3-2 ( $n_{\text{crit}} \sim 1 \times 10^6 \text{cm}^{-3}$ )

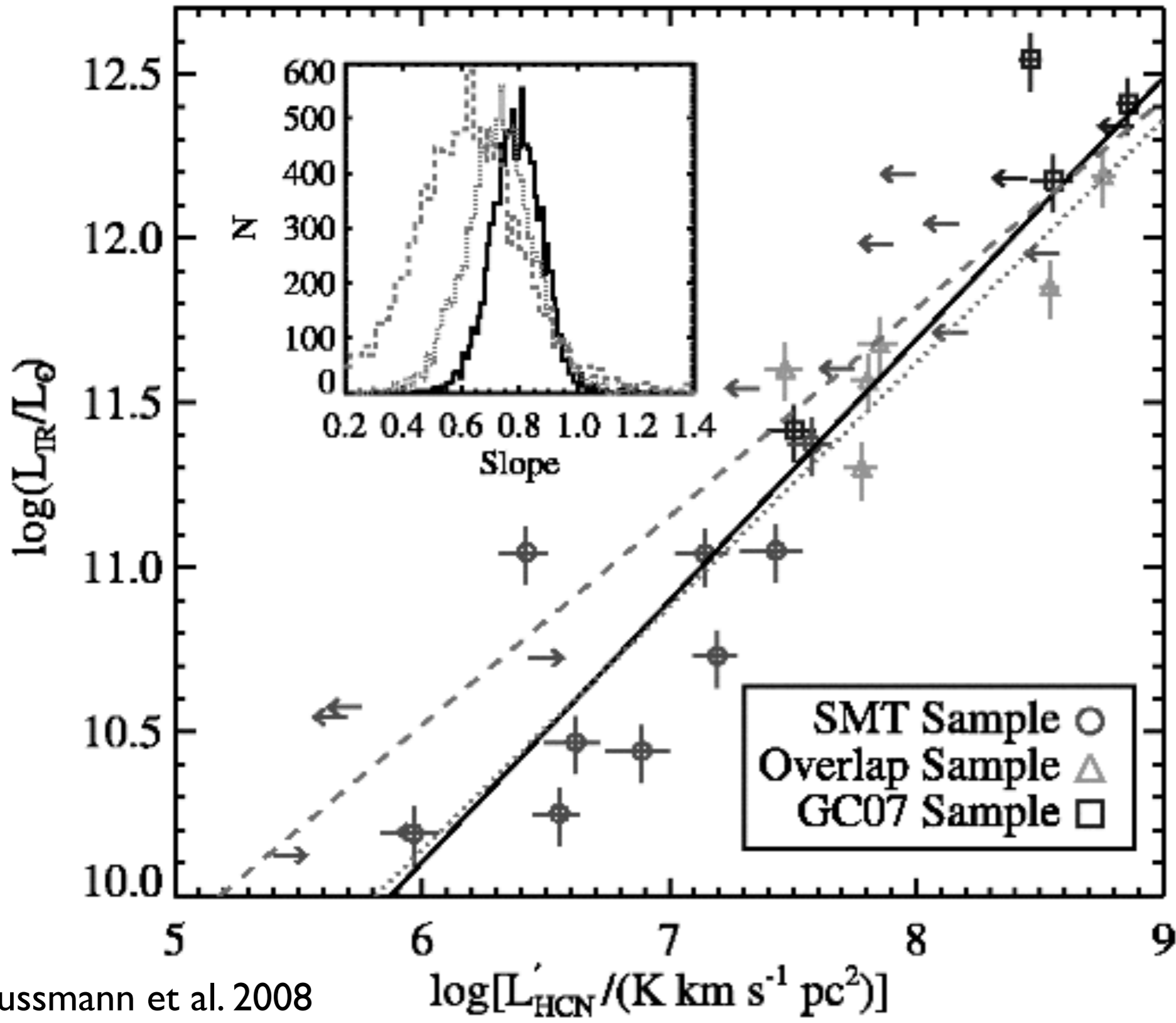


Slope=0.8

$L'_{\text{gas}} \propto M_{\text{gas}}$   
 $L_{\text{IR}} \propto \text{SFR}$



# $L'_{\text{gas}}-L_{\text{IR}}$ correlations -- HCN 3-2 ( $n_{\text{crit}} \sim 5 \times 10^6 \text{cm}^{-3}$ )



$N \sim 0.7$

$L'_{\text{gas}} \propto M_{\text{gas}}$   
 $L_{\text{IR}} \propto \text{SFR}$

# Galactic CS & HCN studies

CS 2-1:

Least squares :  $\log(L_{\text{IR}}) = 1.03(\pm 0.05) \times \log(L'_{\text{CS}2-1}) + 3.25(\pm 0.11); r = 0.80$

1.03(0.05)

Robust fit :  $\log(L_{\text{IR}}) = 0.87 \times \log(L'_{\text{CS}2-1}) + 3.56$

CS 5-4:

Least squares fit :  $\log(L_{\text{IR}}) = 1.05(\pm 0.05) \times \log(L'_{\text{CS}5-4}) + 3.77(\pm 0.08); r = 0.86$

1.05(0.05)

Robust fit :  $\log(L_{\text{IR}}) = 0.86 \times \log(L'_{\text{CS}5-4}) + 3.90$

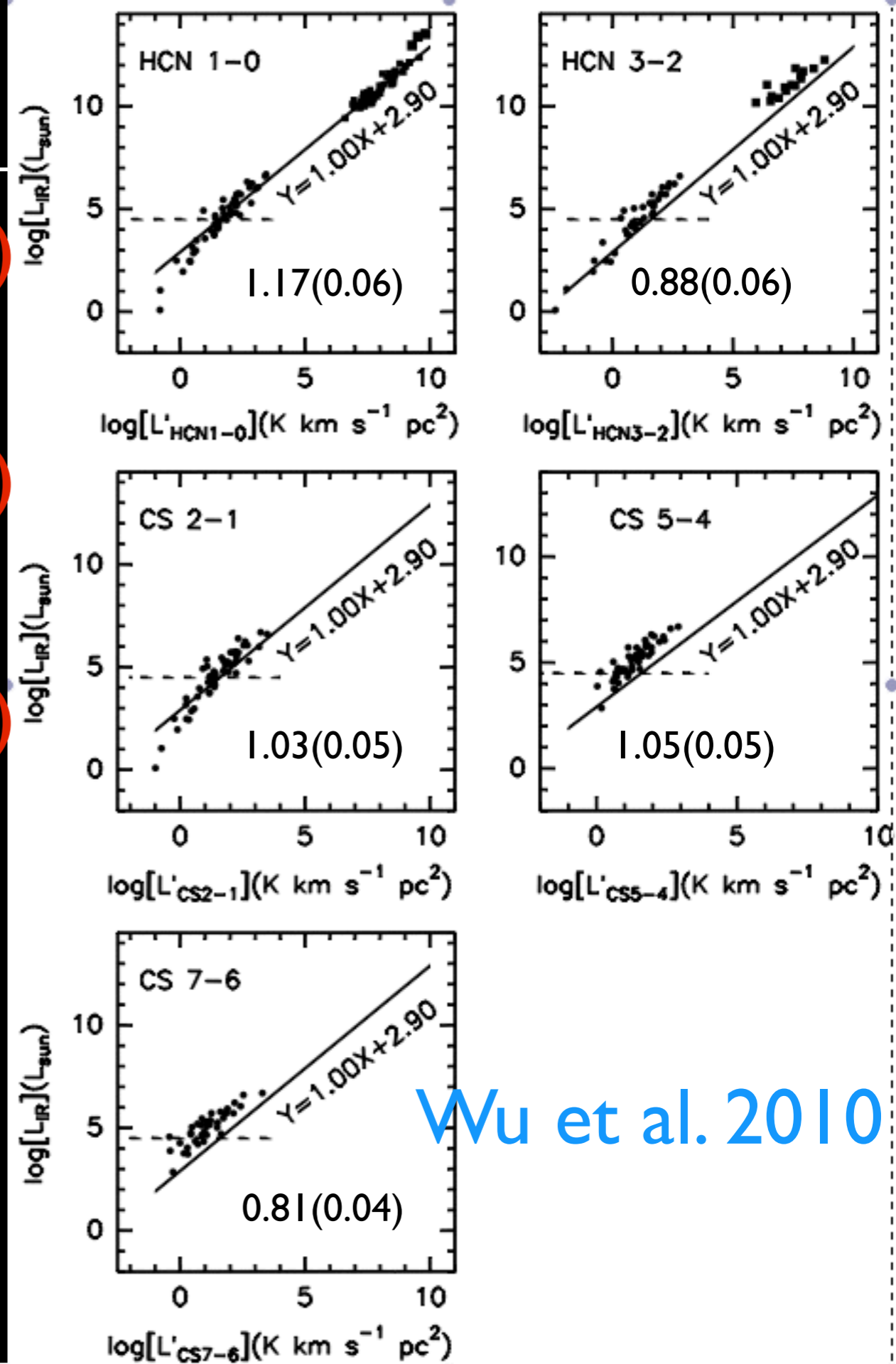
CS 7-6:

Least squares fit :  $\log(L_{\text{IR}}) = 0.81(\pm 0.04) \times \log(L'_{\text{CS}7-6}) + 4.31(\pm 0.06); r = 0.81$

0.81(0.04)

Robust fit :  $\log(L_{\text{IR}}) = 0.64 \times \log(L'_{\text{CS}7-6}) + 4.58$

The average density determined from CS excitation of the massive clumps in our sample is about  $10^{5.9} \text{ cm}^{-3}$  (Plume et al. 1997), less than the critical density of all the tracers in this study except for the CS 2-1 line (Table 9), but greater than the effective density (Table 9) and the density that was found to contribute most to the HCN 1-0 line in the simulations of Krumholz & Thompson (2007). In fact, a density derived from excitation analysis is biased toward the densest regions and the mean density of the clumps in the sense of mass divided by volume is generally less (e.g., Shirley et al. 2003). As noted above, the relations we find do not support the suggestions by Krumholz & Thompson (2007) or Narayanan et al. (2008).



Wu et al. 2010



# Theoretical works

1) Krumholz et al. (2007):

$n_{\text{crit}} < n_{\text{ave}}$ : slope  $\sim 1.5$  e.g., CO 1-0

$n_{\text{crit}} > n_{\text{ave}}$ : slope  $\sim 1$  e.g., HCN 1-0

2) Narayanan et al. (2008):

Sub-thermal excitation.

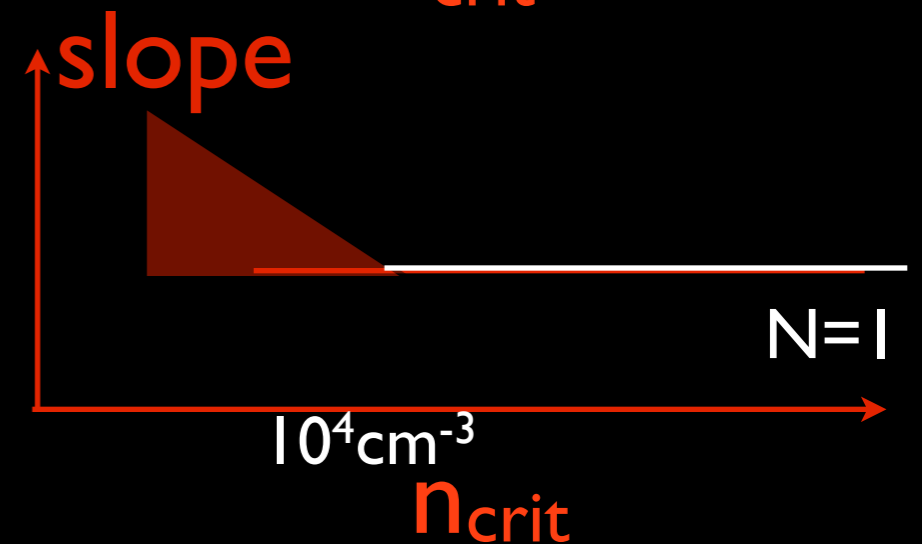
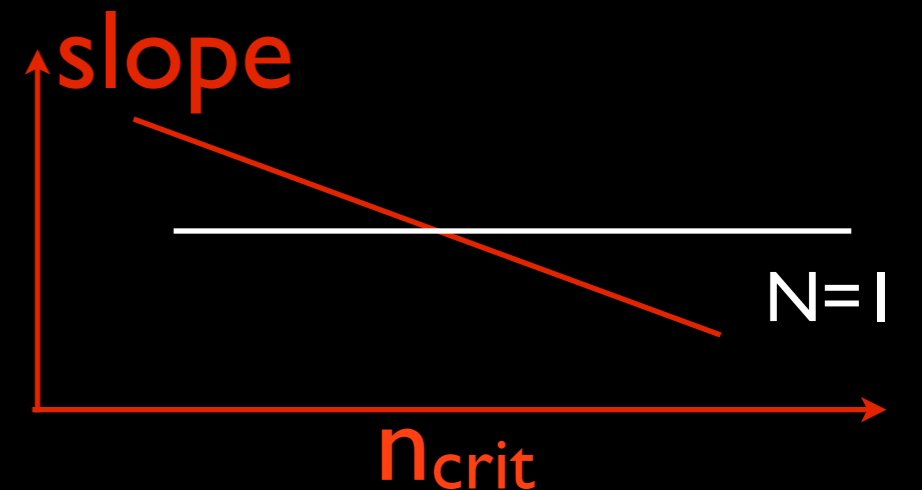
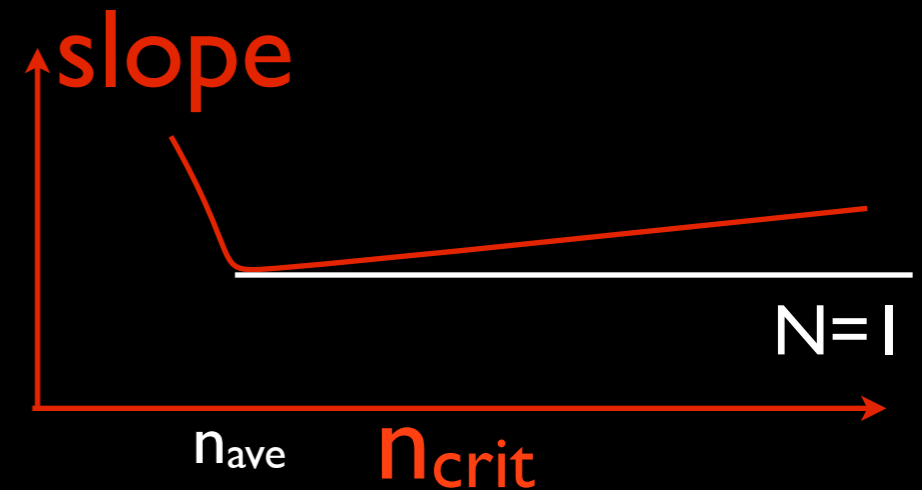
Slope decreases with  $n_{\text{crit}}$ .

3) Lada et al. (2012):

Linear slope for lines with  $n_{\text{crit}} > 10^4 \text{cm}^{-3}$

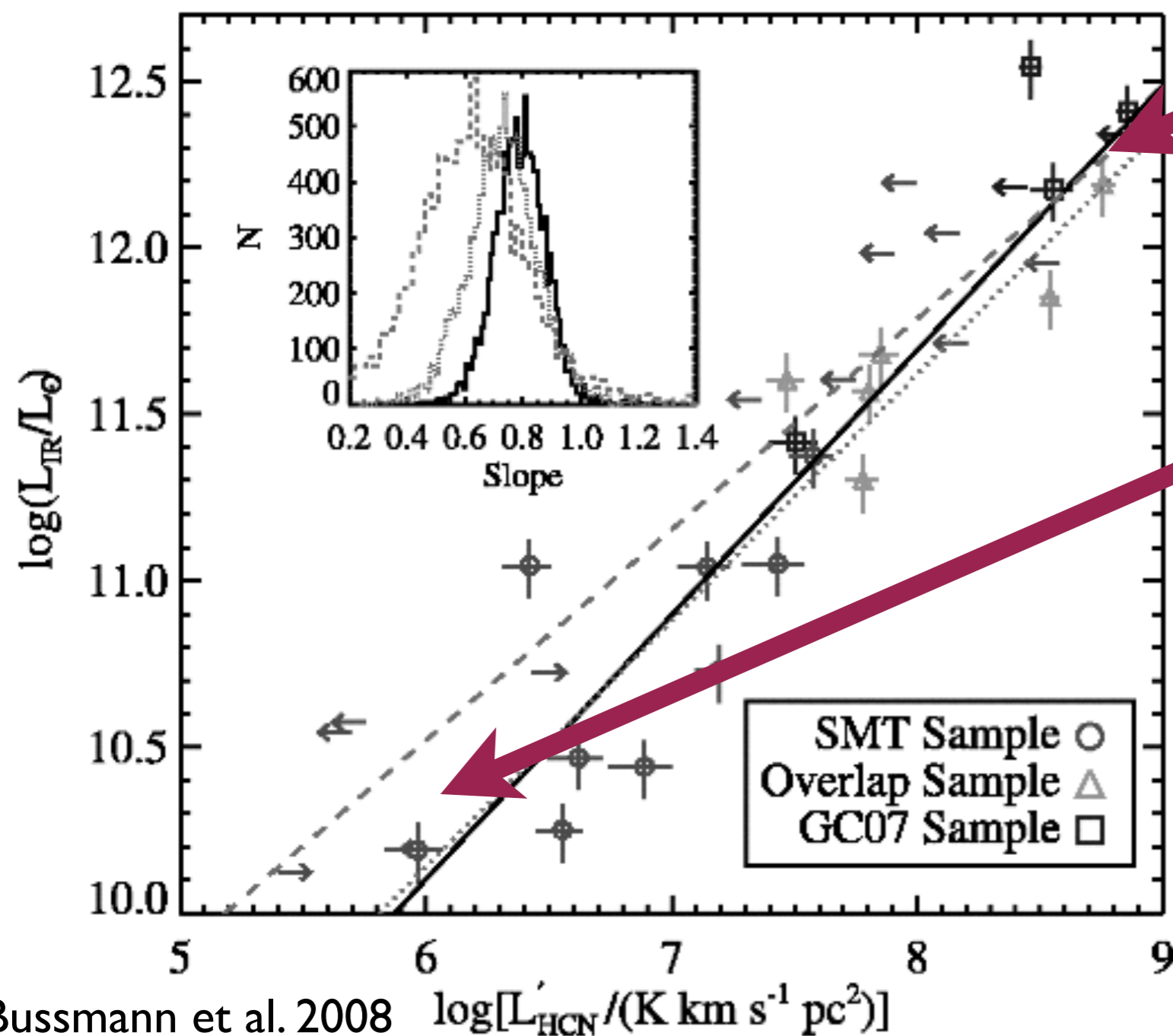
SFR is only related to  $M_{\text{dense}}$ .

K-S law slope is related to  $M_{\text{dense}}$  fraction.



# Potential Issues

IR pumping?  
Chemistry?



Stable tracers need.

IR size > beamsize

Either to map gas emission  
or  
to match IR with beam

To test the above models, a **multiple transition** survey of **clean** dense tracers is needed, e.g. CS lines



# Sample Selection:

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1. IRAS Revised Bright Galaxies sample (IRAS RBGs, Sanders 2003).

Flux cutoff:  $F_{100\mu\text{m}} > 100 \text{ Jy}$ ,  $F_{60\mu\text{m}} > 50 \text{ Jy}$ .

2. Rich detections of CO and HCN lines.

3. A large range of  $L_{\text{IR}}$ , measured with IRAS.

Nearby normal galaxies, starburst, and (U)LIRGs.

~ 40 galaxies are selected

# Multiple-J CS survey

~ 280 hours in total

Multiple transitions ( $J=1-0$  to  $7-6$ ) of CS lines towards  
~ 40 nearby normal galaxies, starburst, and (U)LIRGs

CS  $J=2-1/3-2/5-4$  IRAM 30m



CS  $J=5-4$  SMT(HHT) 10m



CS  $J=5-4/7-6$  APEX 12m



CS  $J=1-0$  GBT and the EVLA





# Spectra

CS J=1-0 : 20/24 galaxies

CS J=2-1 : 41/47 galaxies

CS J=3-2 : 30/41 galaxies

CS J=5-4 : 21/40 galaxies

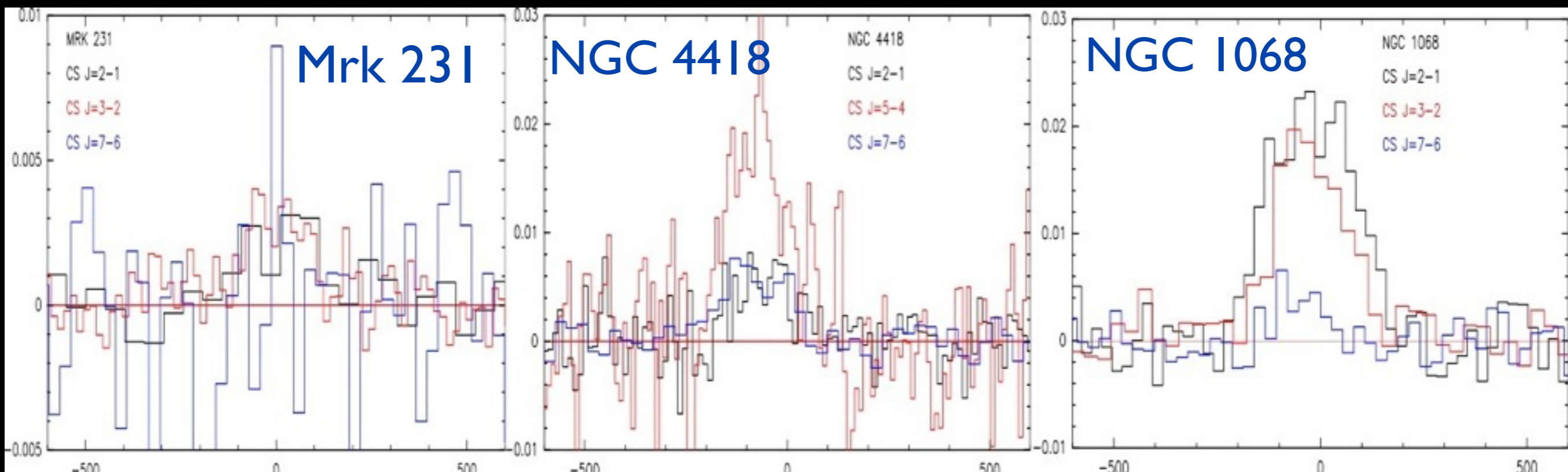
CS J=7-6 : 11/20 galaxies

C<sup>34</sup>S J=2-1: 5 detections

+

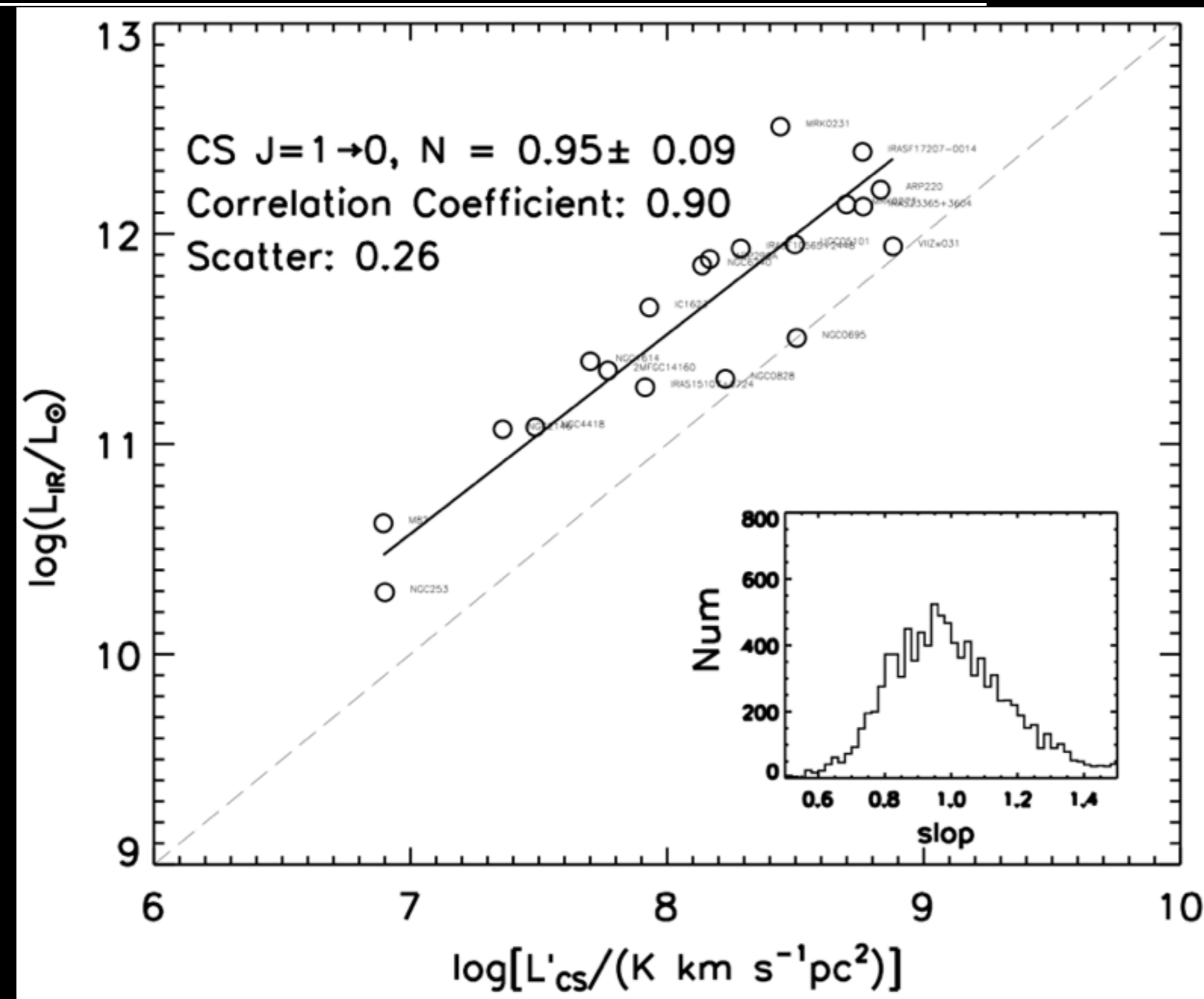
CS detections  
in literatures

HCN/HCO<sup>+</sup> 4-3 simultaneously



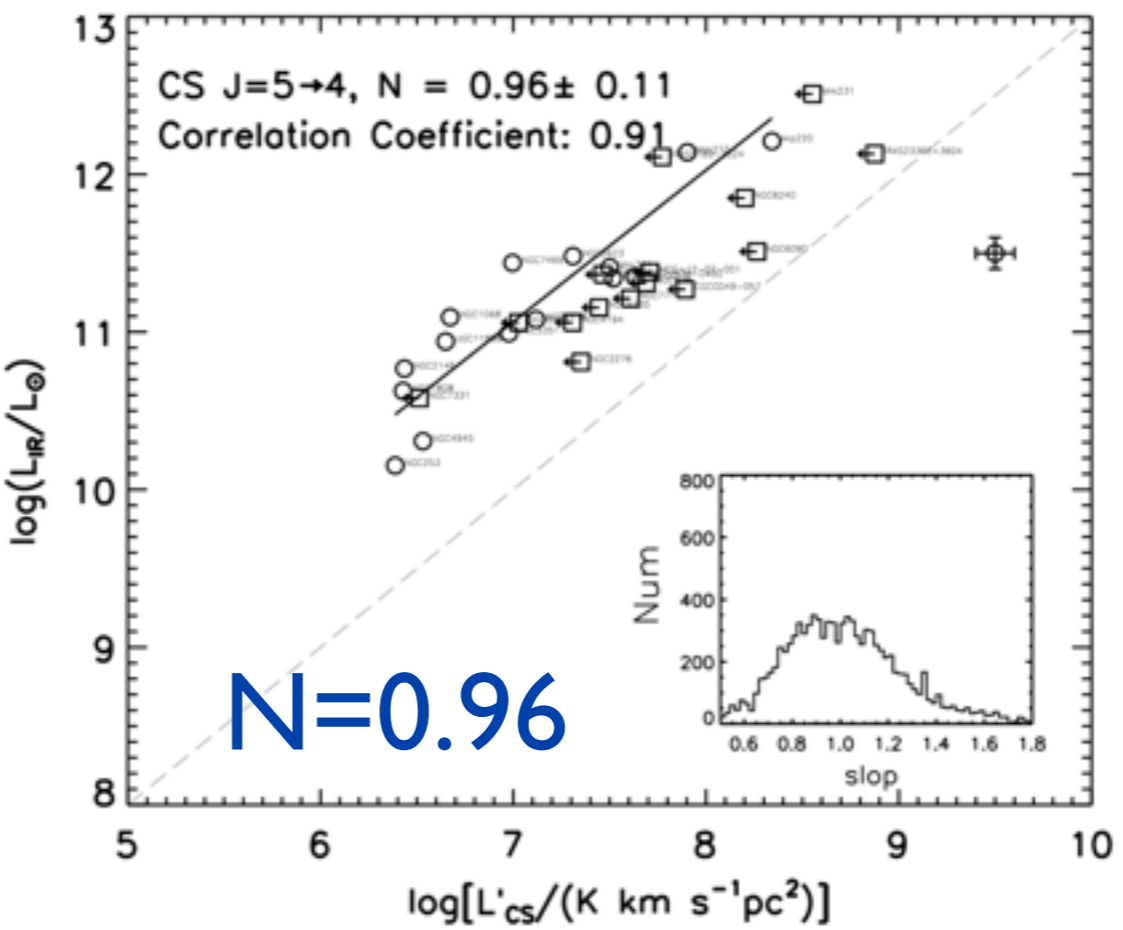
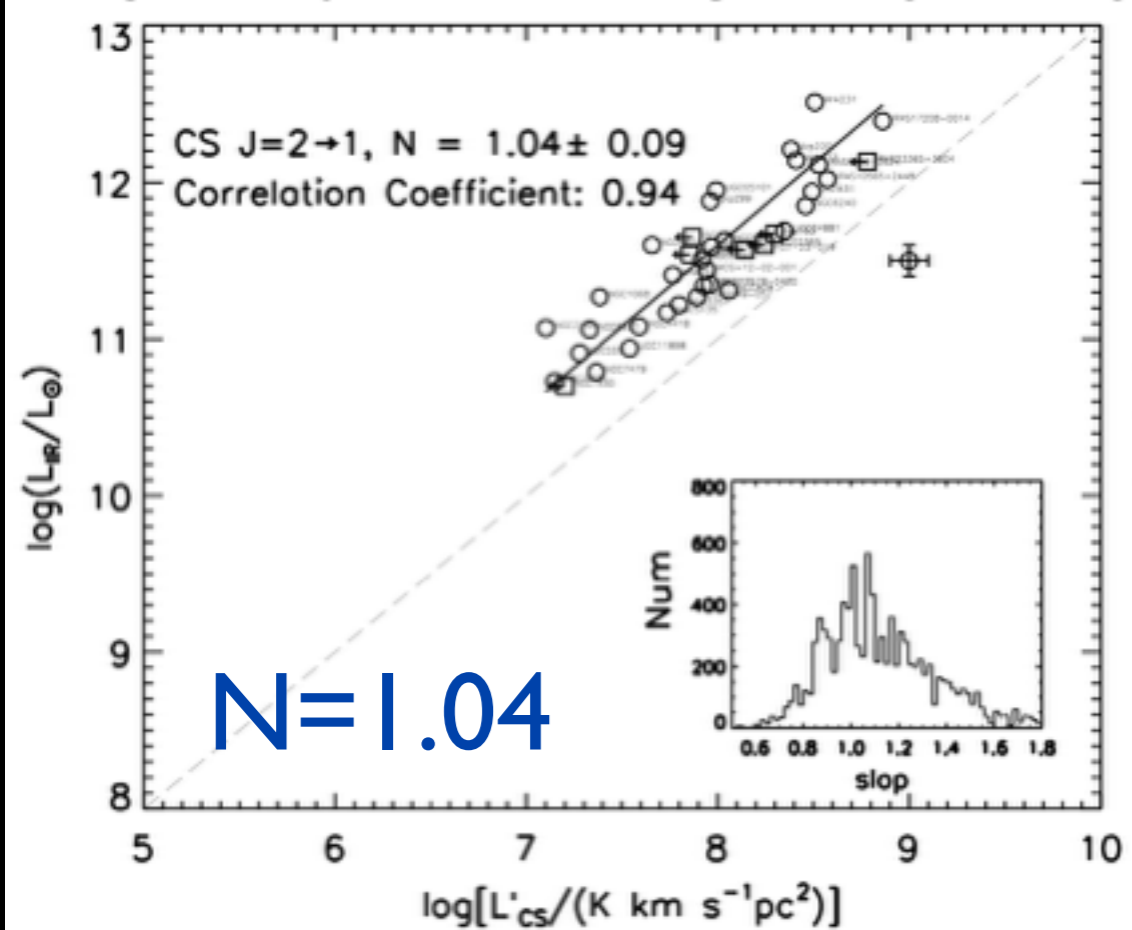
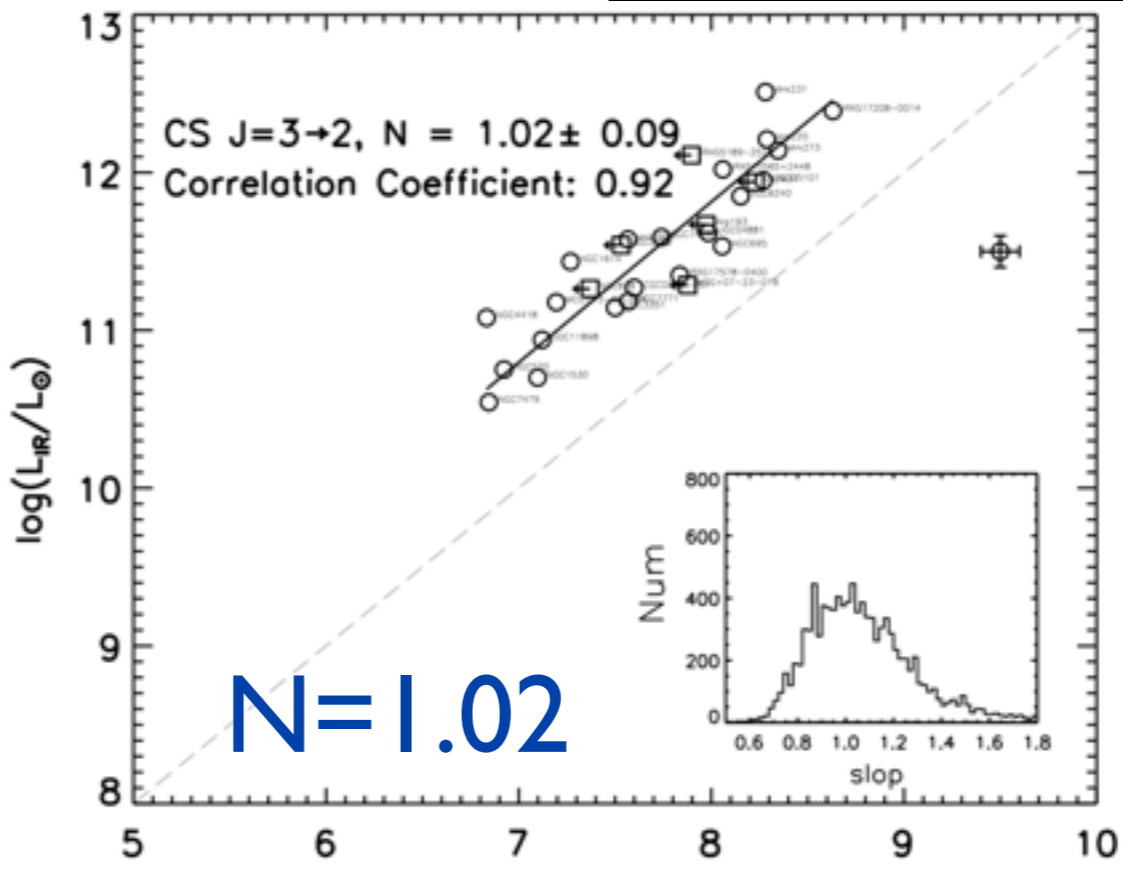
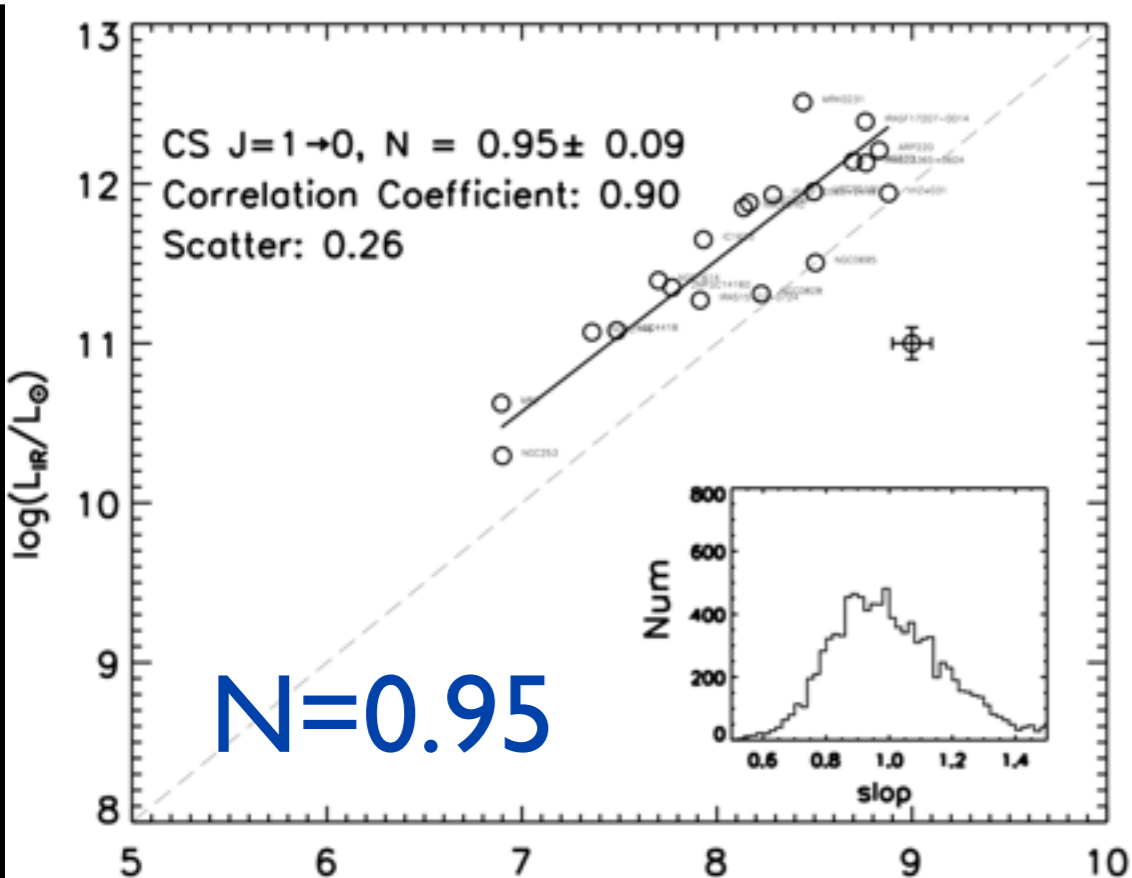
$L'_{\text{gas}} - L_{\text{IR}}$  (point source)

CS J=1-0  $n_{\text{crit}} \sim 1 \times 10^4 \text{cm}^{-3}$



# L'cs-L<sub>IR</sub> correlations

# Point sources only



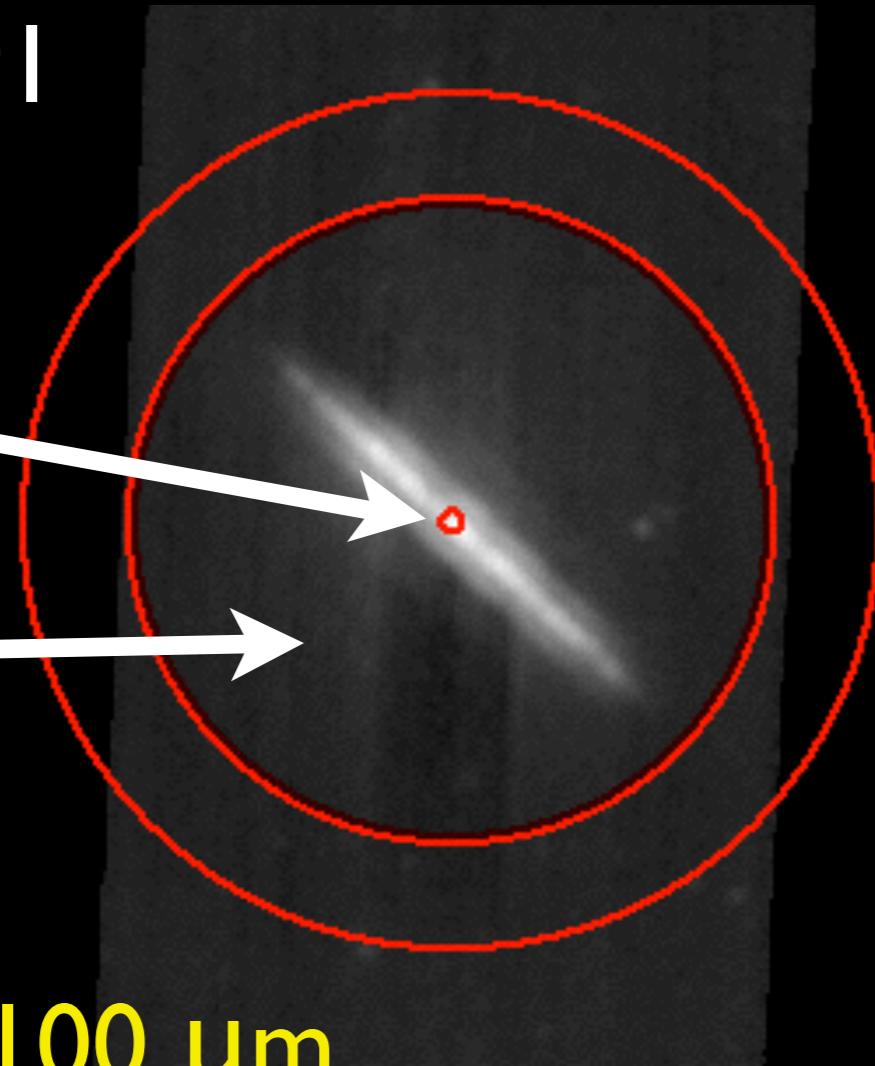


# Beam matching photometry

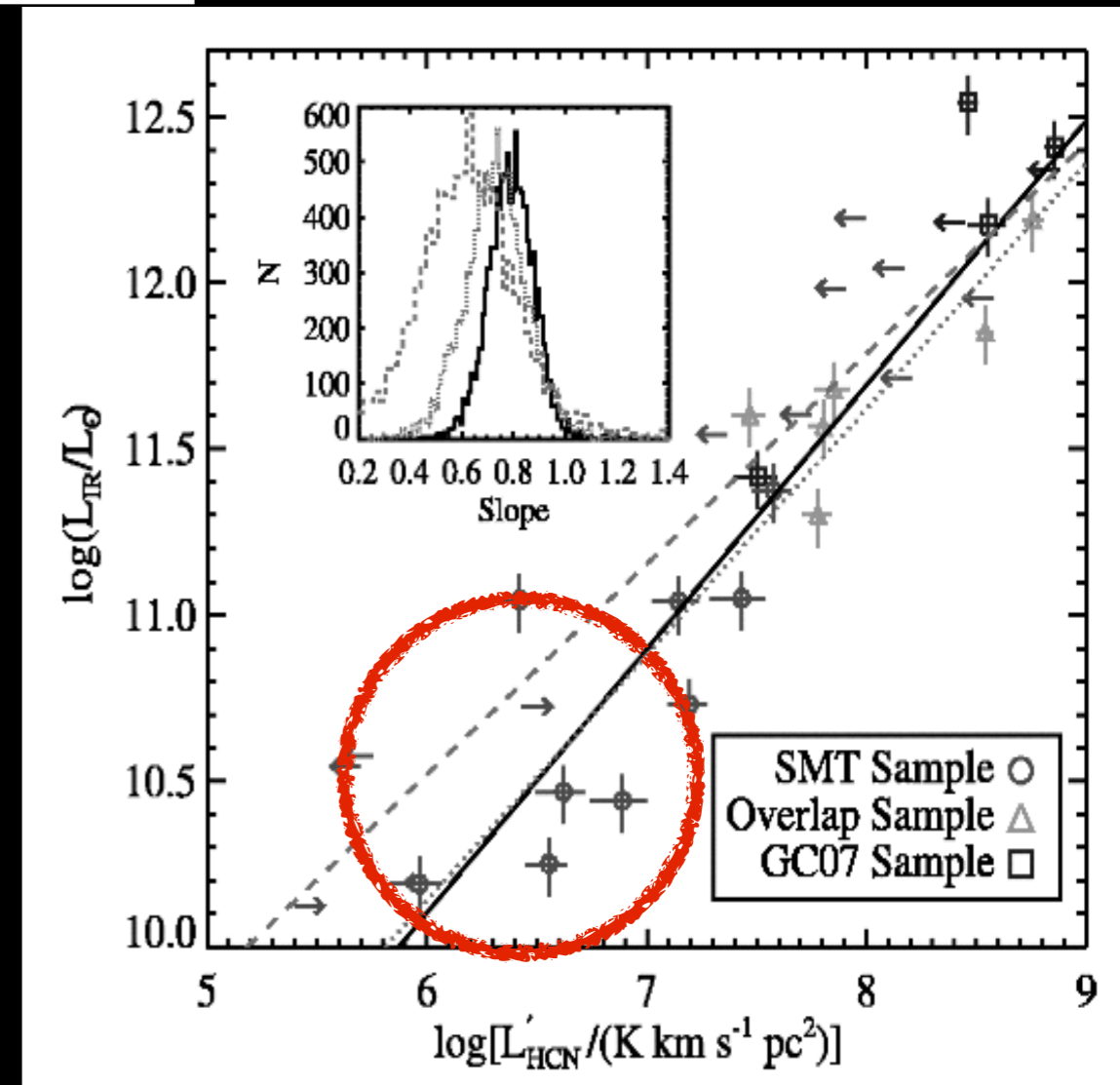
NGC 891

Beam

Whole



Herschel 100 μm



Bussmann et al. 2008

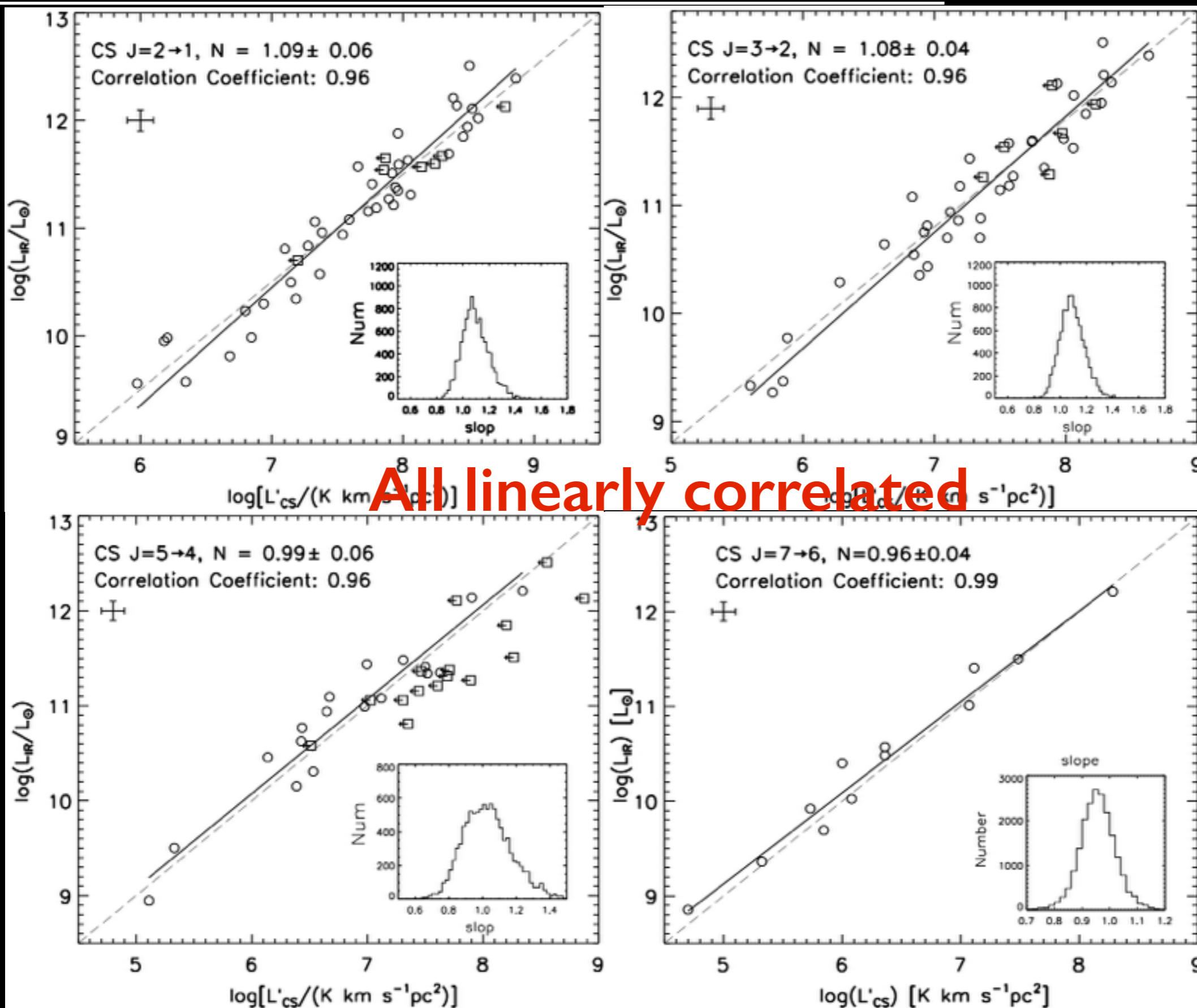
$$L_{\text{SD}} = R_{\text{SD}} \times L_{\text{TIR}}(\text{IRAS})$$

$R_{\text{SD}} = F_{\text{beam}} / F_{\text{total}}$  varies at different bands

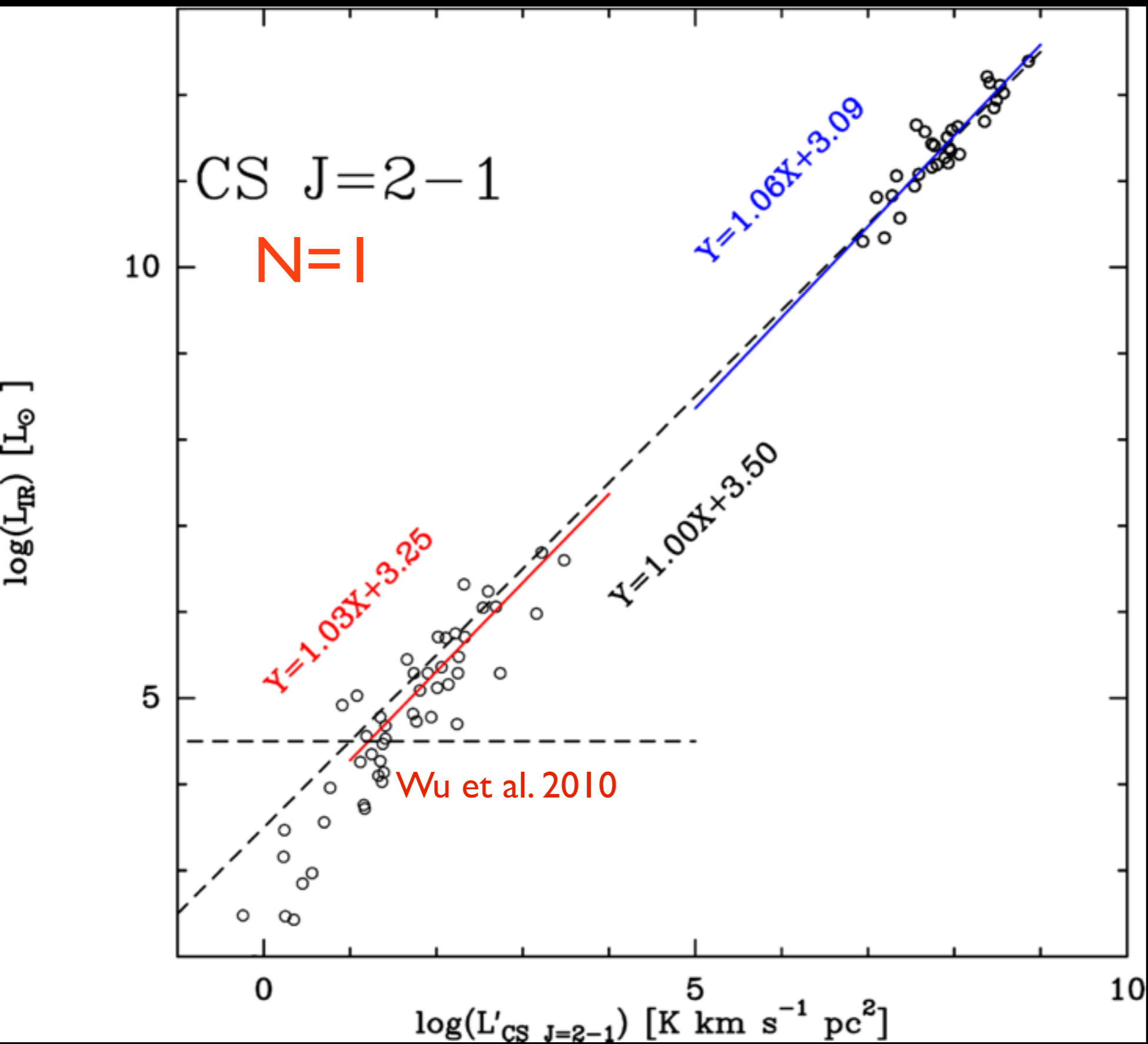
Assuming whole galaxy share one IR SED.

# L<sub>CS</sub>-L<sub>IR</sub> correlations

# Beam matching correction



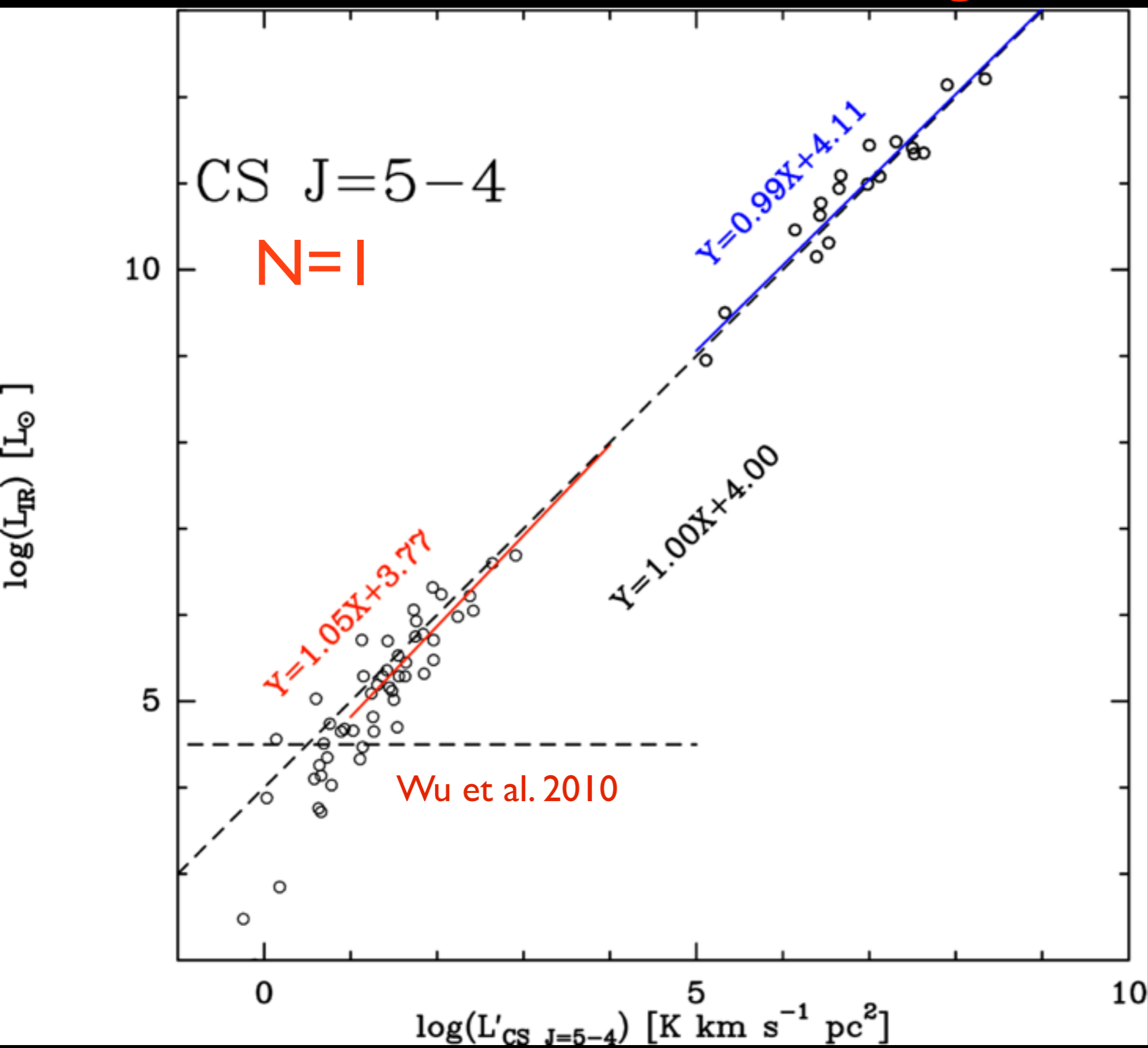
# L'CS-L<sub>IR</sub> correlations ~ 8 orders of magnitude



$n_{\text{crit}} \sim 1 \times 10^5 \text{ cm}^{-3}$

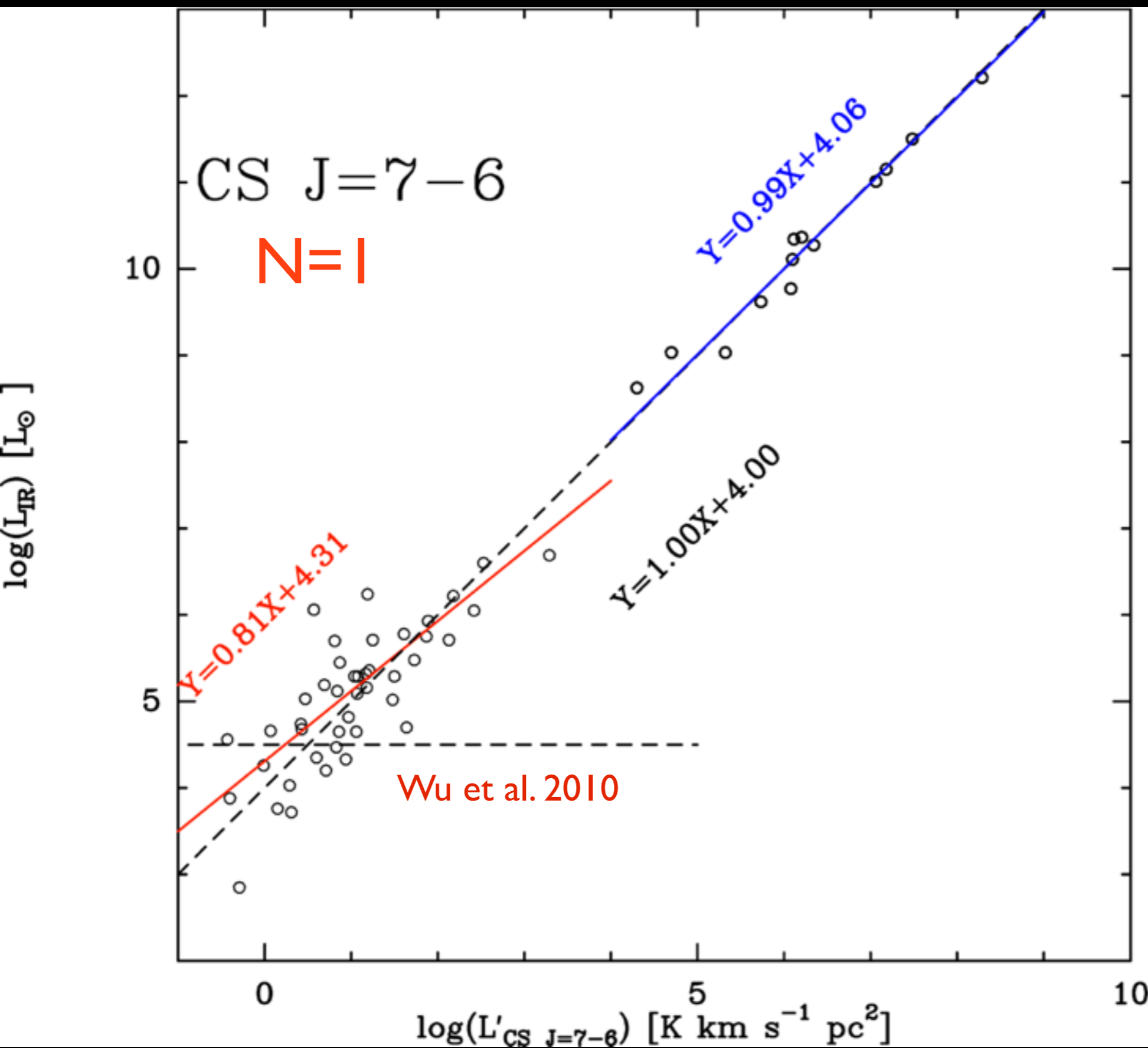


# L'CS-L<sub>IR</sub> correlations ~ 8 orders of magnitude



$$n_{\text{crit}} \sim 2 \times 10^6 \text{ cm}^{-3}$$

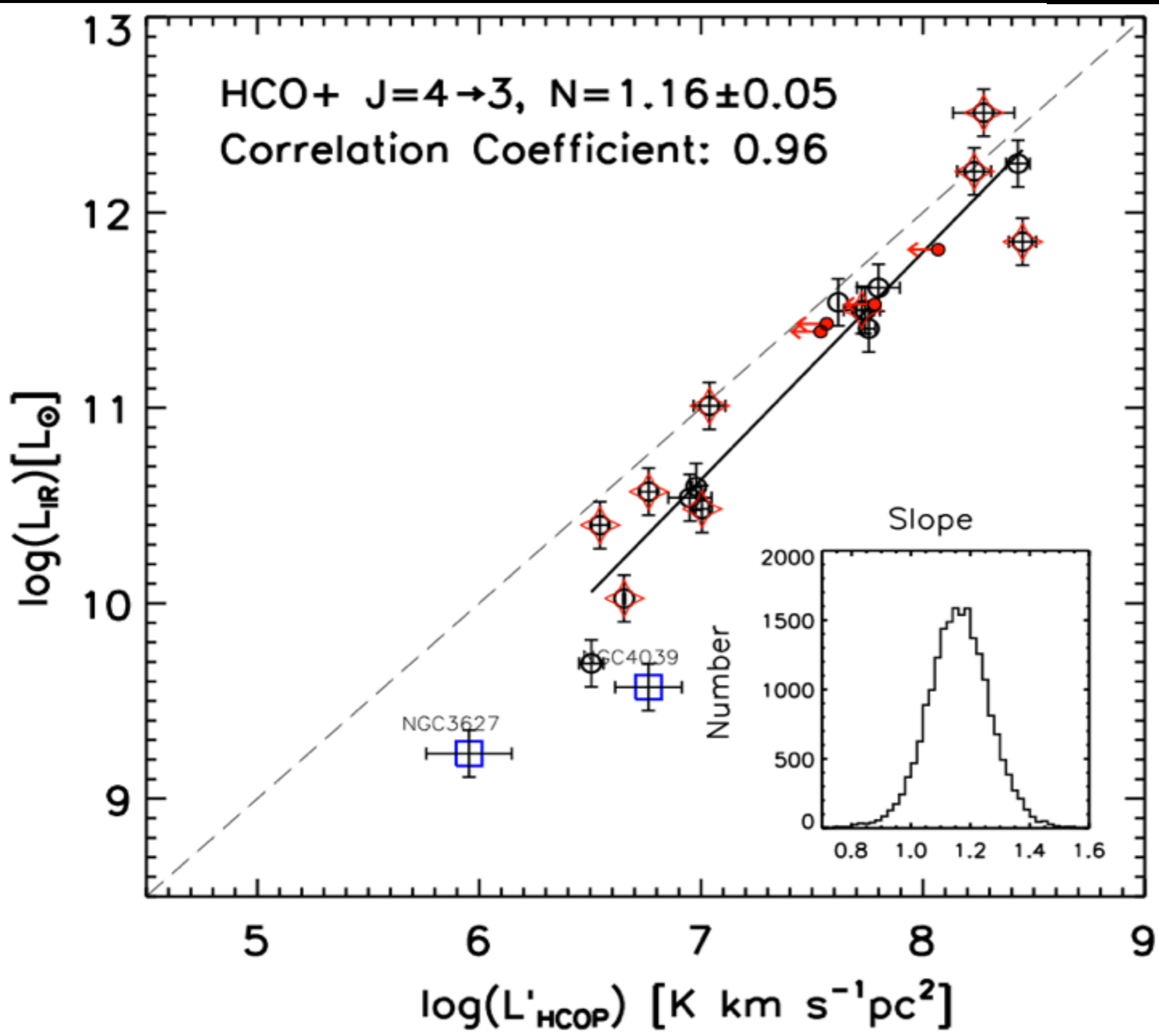
# L'CS-L<sub>IR</sub> correlations ~ 8 orders of magnitude



$n_{\text{crit}} \sim 5 \times 10^6 \text{ cm}^{-3}$

Zhang et al. 2014

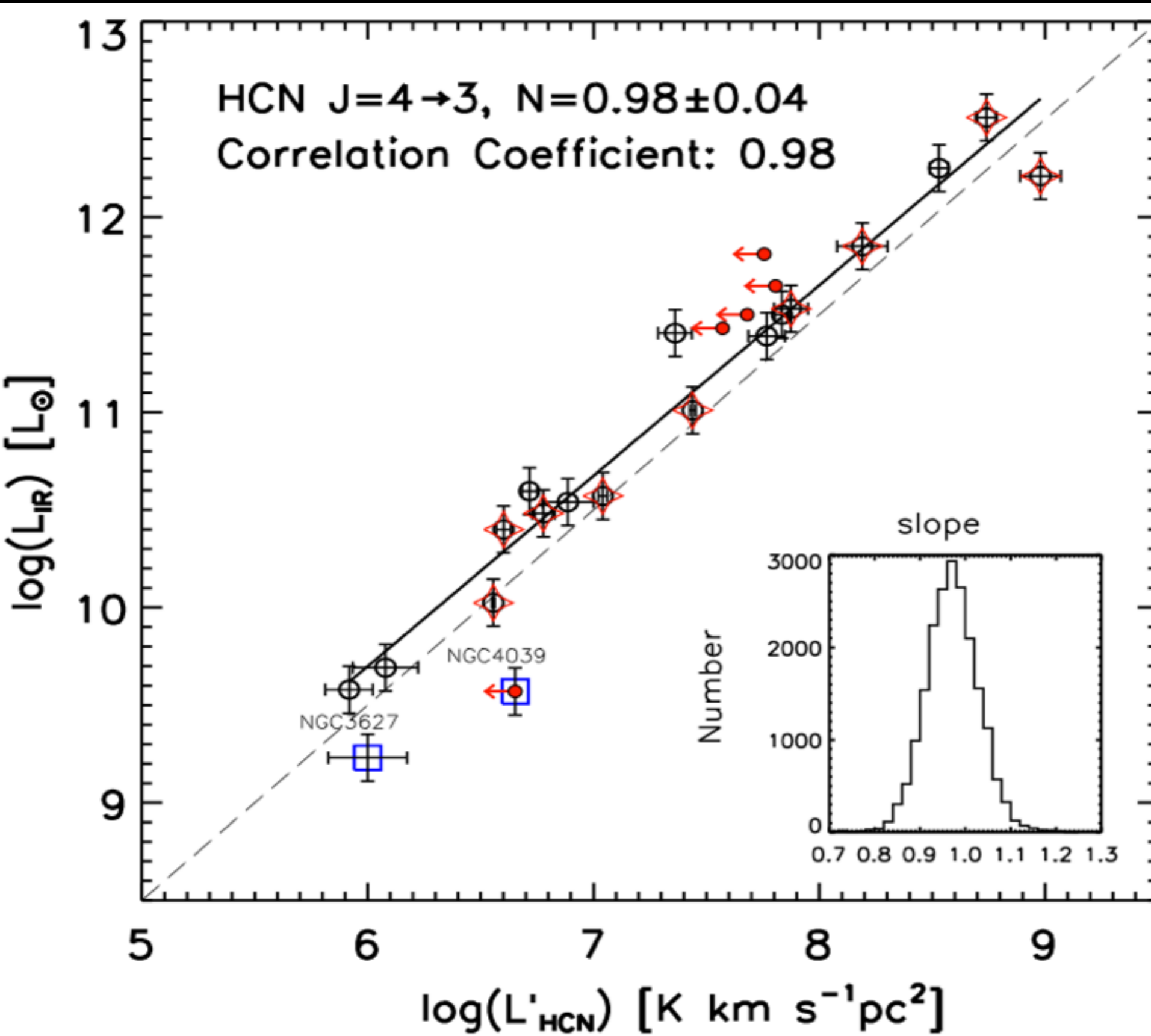
# HCO<sup>+</sup> J=4-3 -- observed simultaneously with CS J=7-6



$n_{\text{crit}} \sim 2 \times 10^6 \text{ cm}^{-3}$



# HCN J=4-3 -- observed simultaneously with CS J=7-6



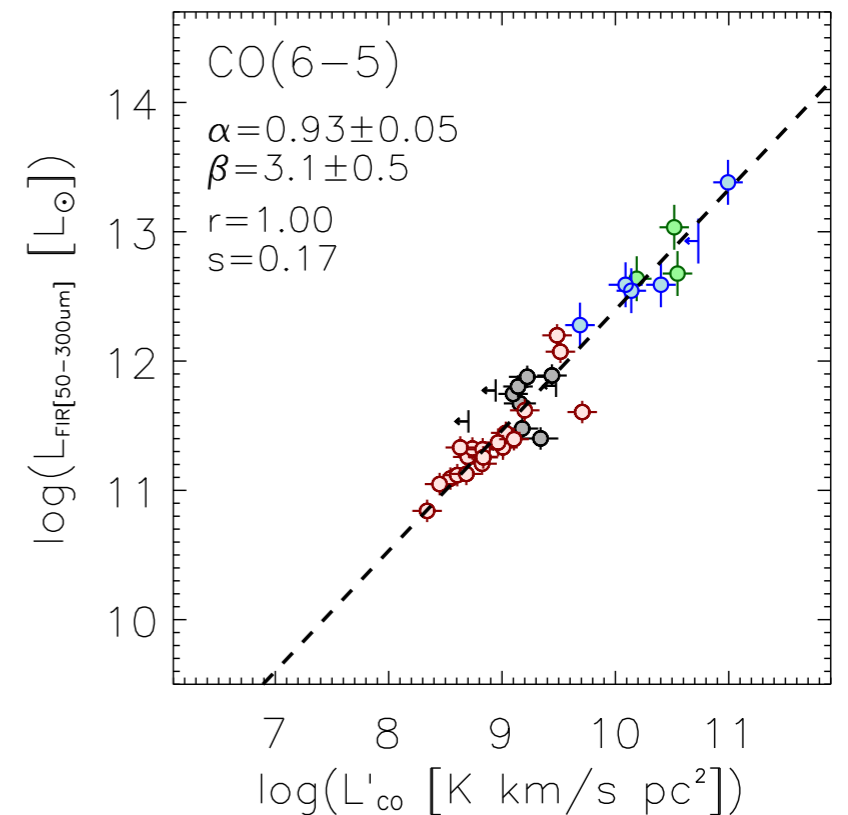
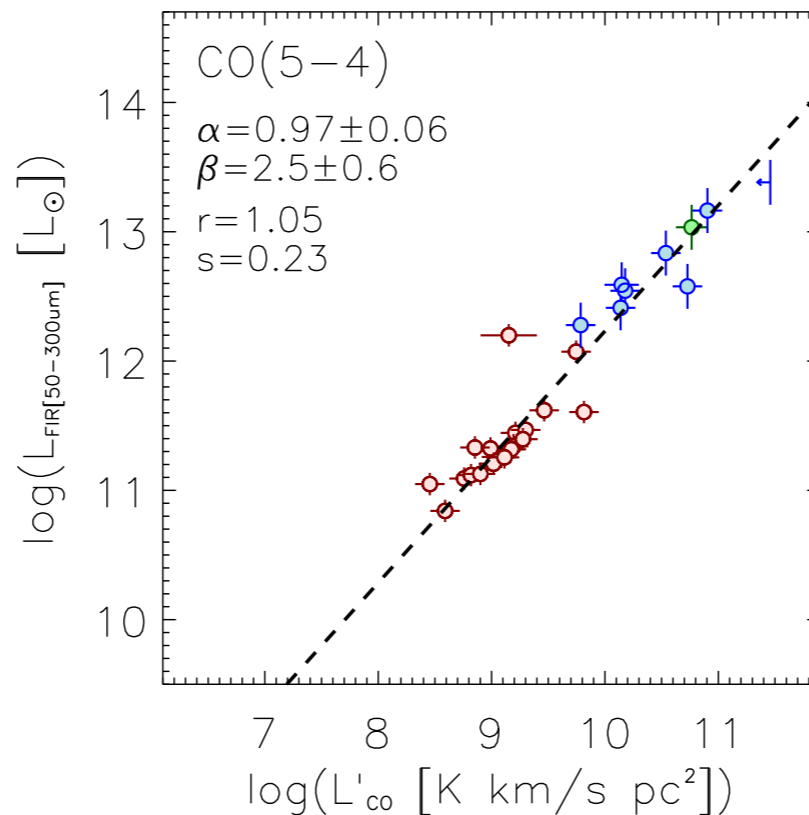
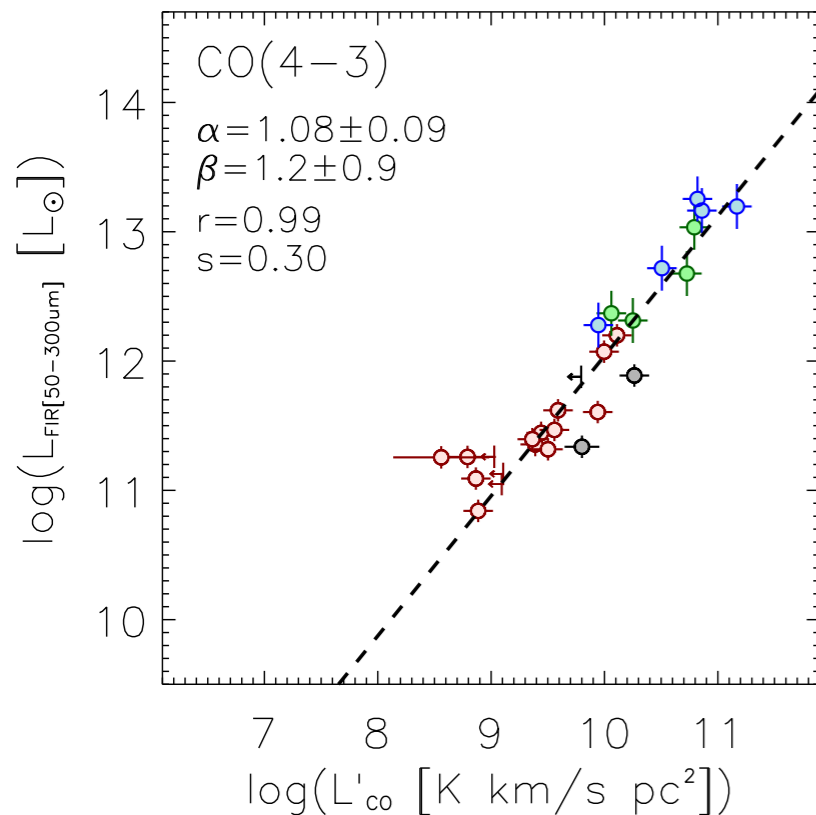
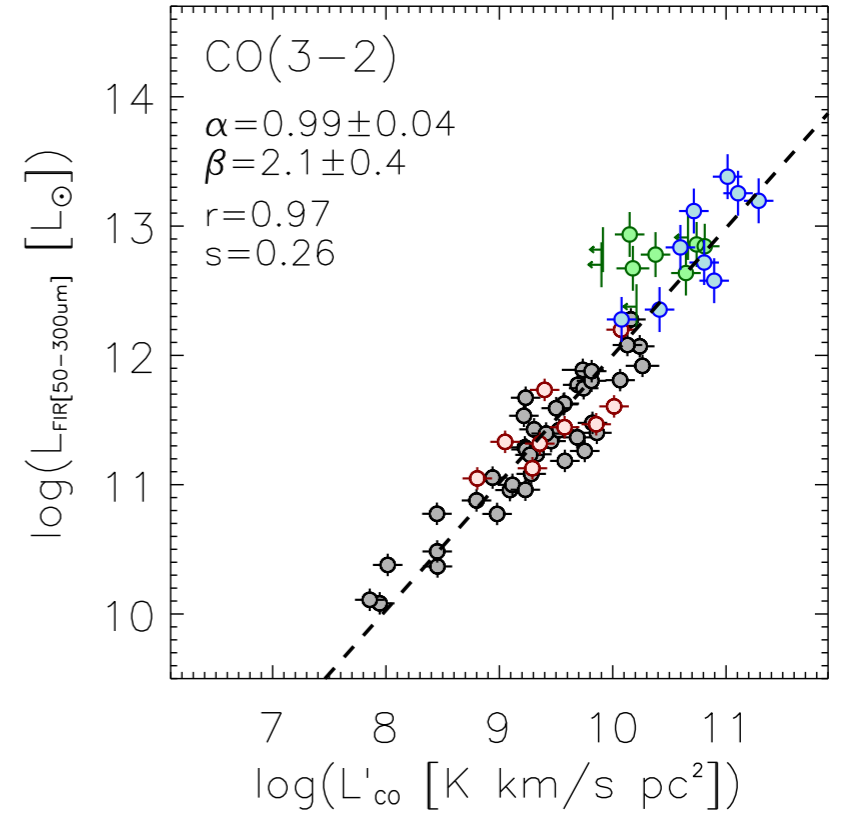
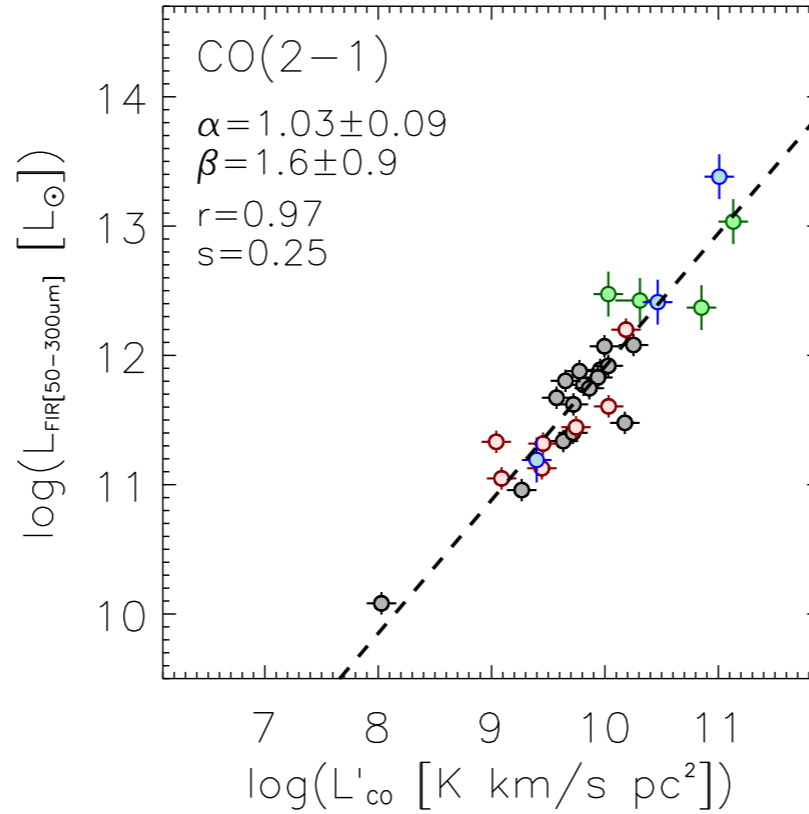
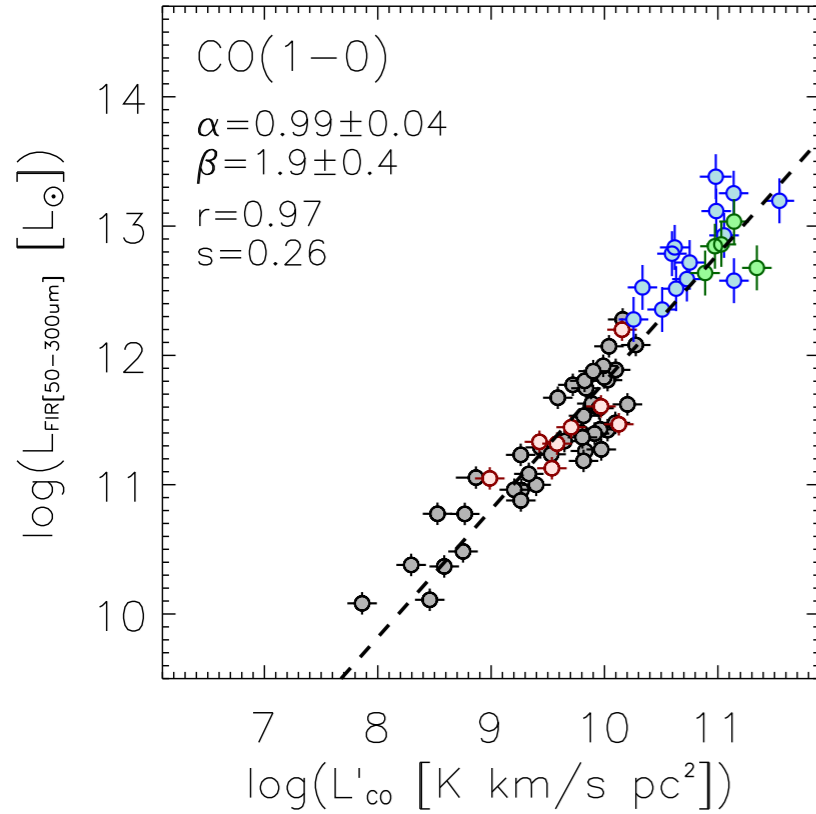
$$n_{\text{crit}} \sim 1 \times 10^7 \text{ cm}^{-3}$$

# LIR-L<sub>CO</sub> relations

- $z < 0.1$  (U)LIRGs (HerCULES)
- $z < 0.1$  (U)LIRGs
- $z > 1$  DSFGs (unlensed)
- $z > 1$  DSFGs (lensed)

# ULIRGs low/high-z

Greve+14

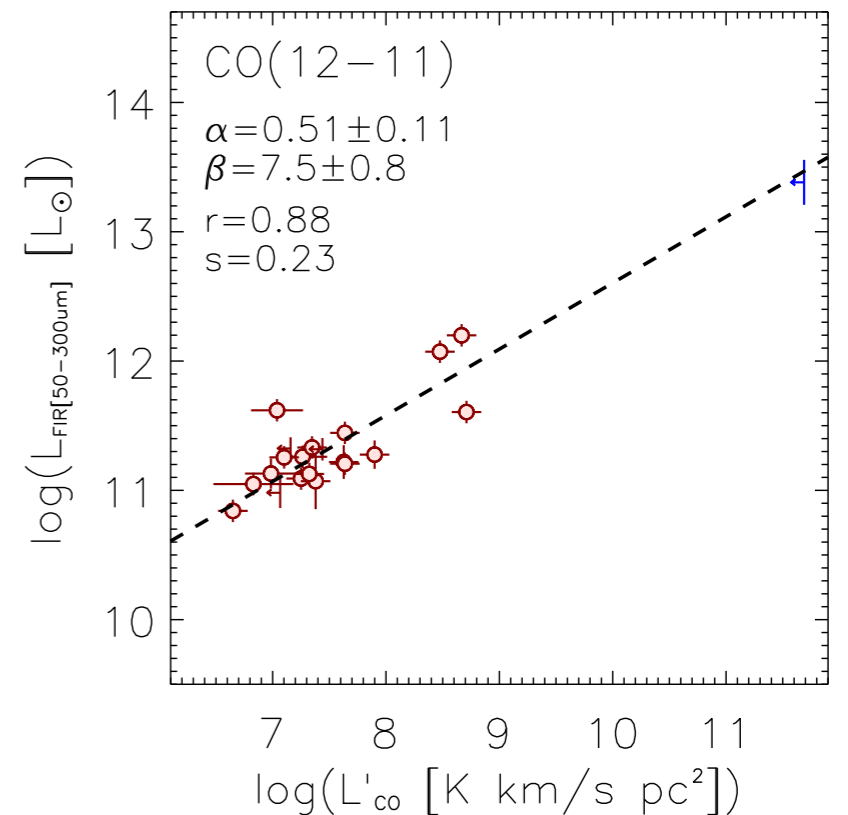
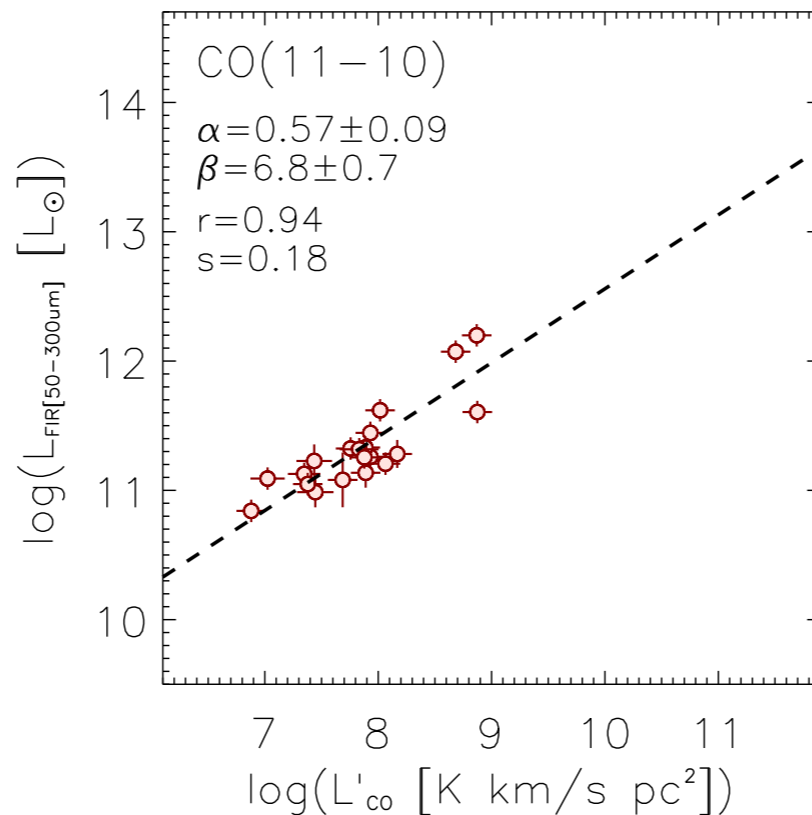
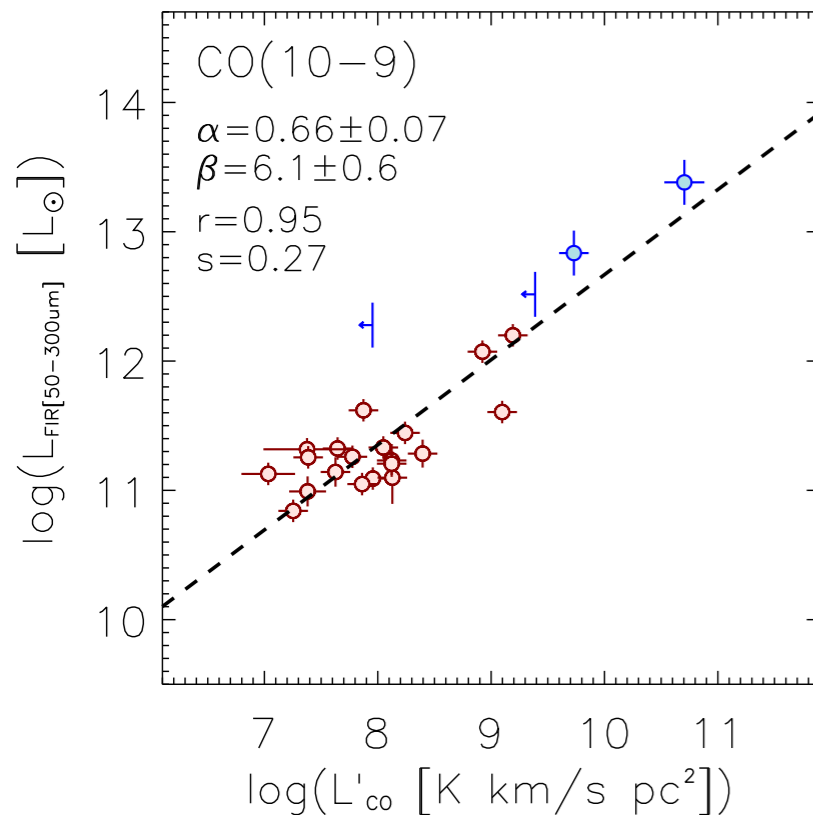
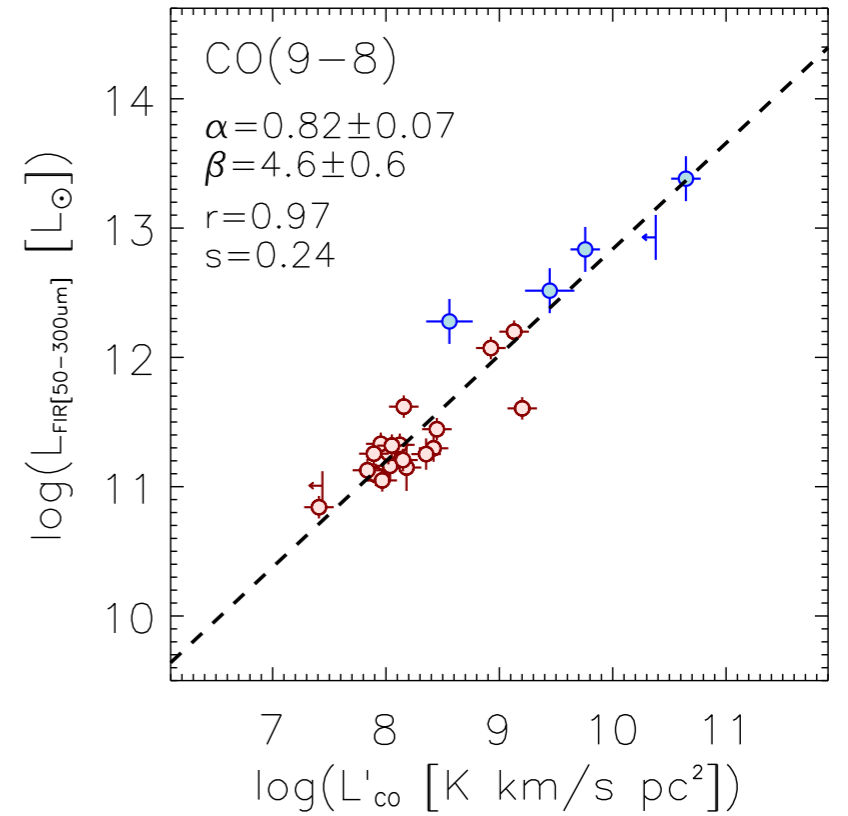
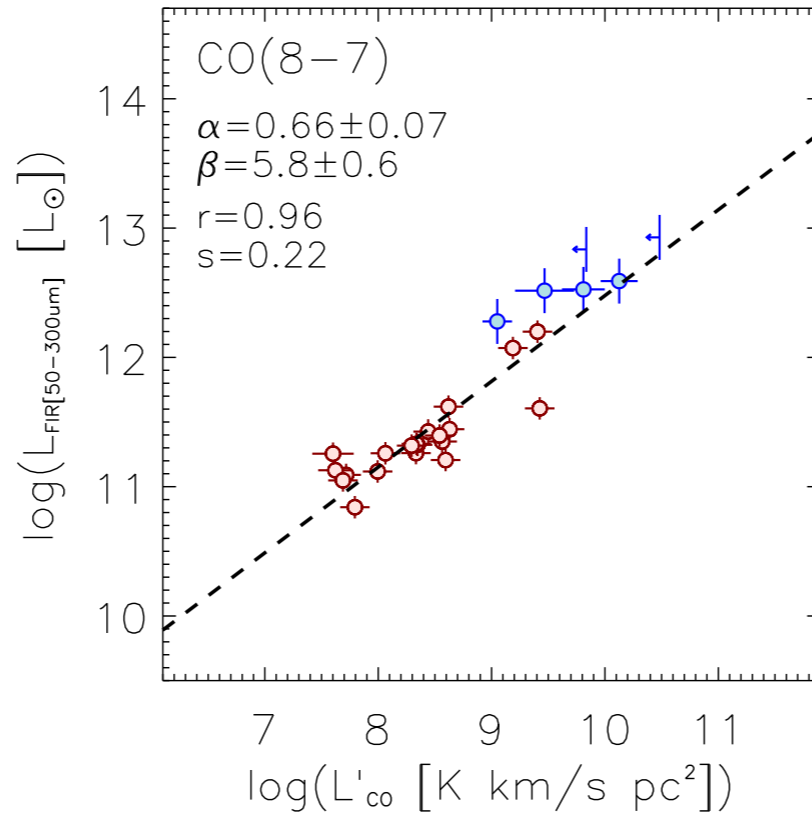
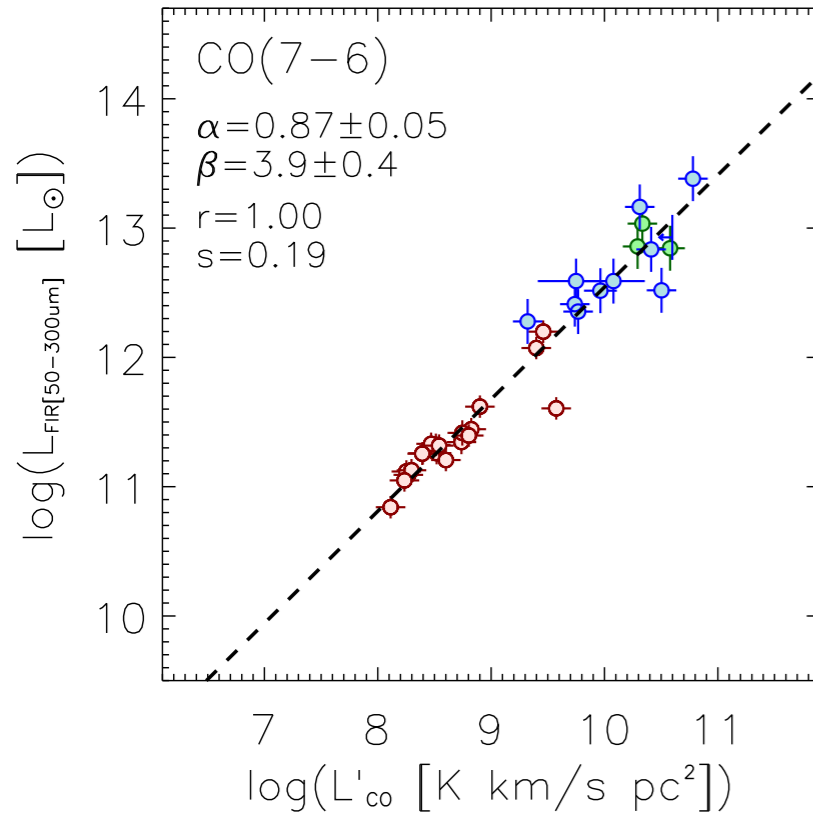


# LIR-L<sub>CO</sub> relations

- $z < 0.1$  (U)LIRGs (HerCULES)
- $z < 0.1$  (U)LIRGs
- $z > 1$  DSFGs (unlensed)
- $z > 1$  DSFGs (lensed)

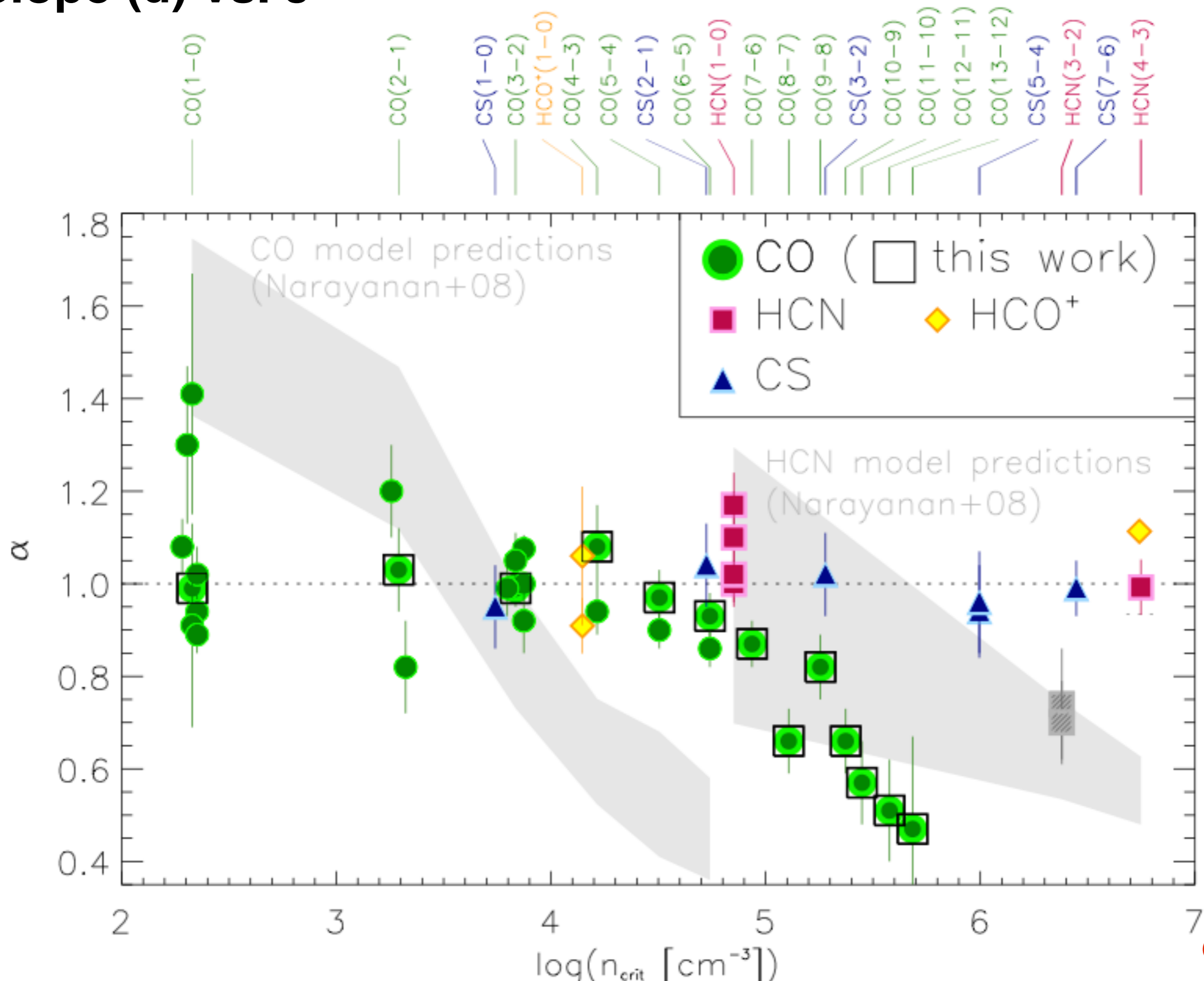
# ULIRGs low/high-z

Greve+14

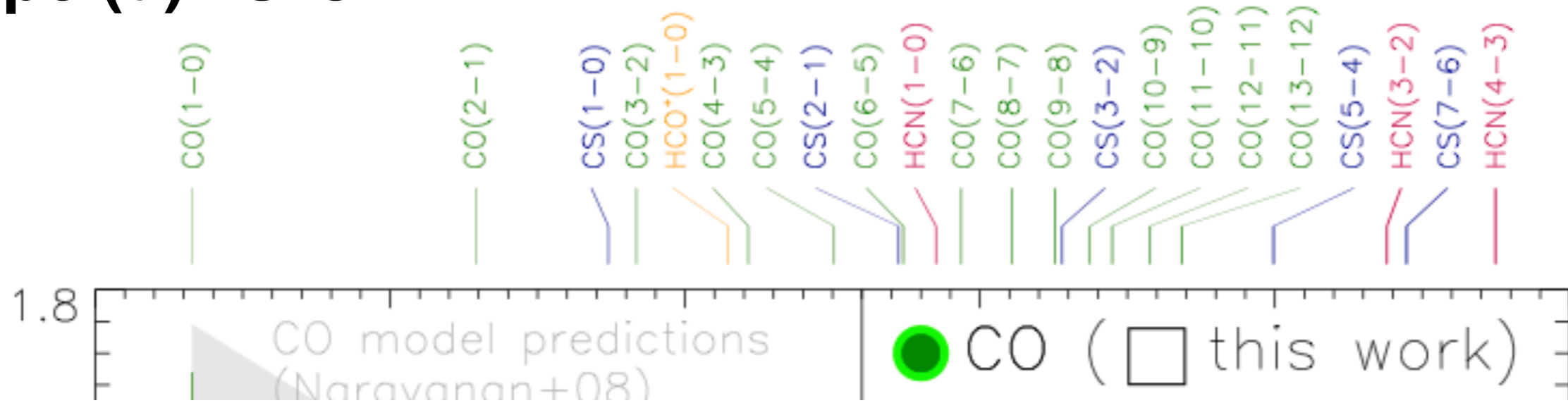




# Slope ( $\alpha$ ) vs. J

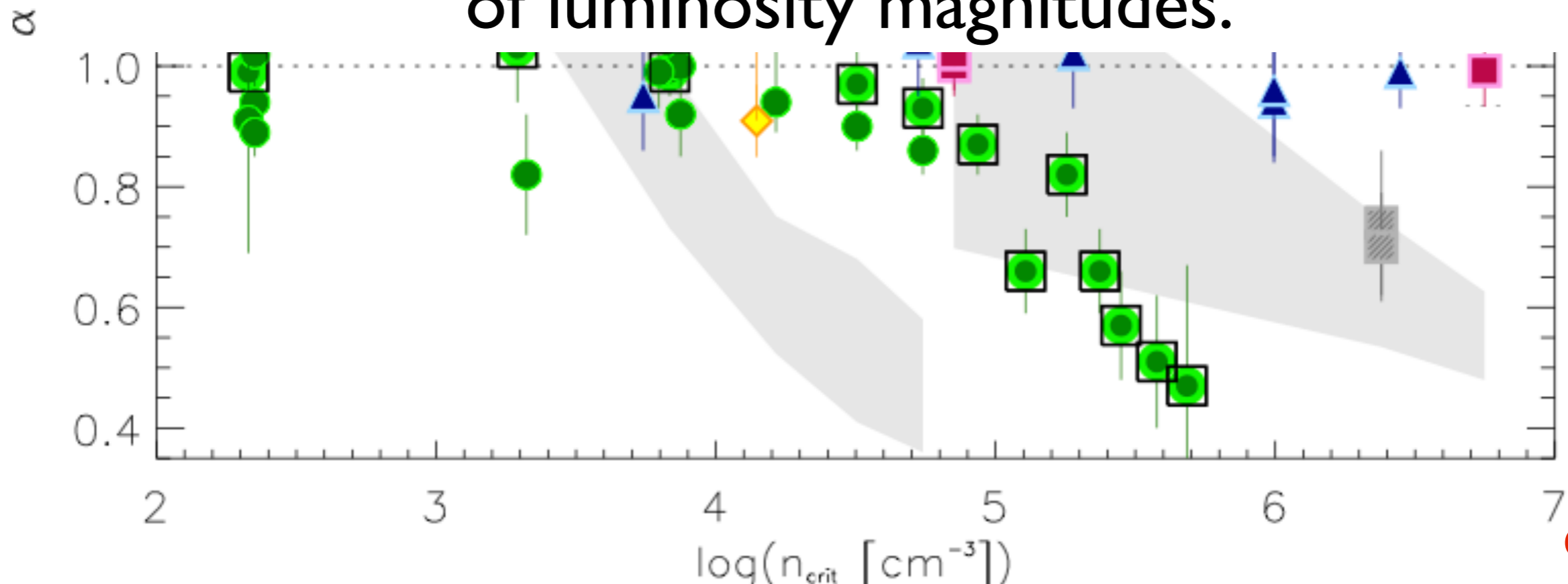


# Slope ( $\alpha$ ) vs. J



Dense and cold gas tracers have **linear** correlations **irrespective** to  $n_{\text{crit}}$ .

This is valid universally over 8 orders of luminosity magnitudes.



# Caveats

$M_{\text{dense}} - L'_{\text{dense}}$  is a first order approximation.

Detections of lines of high  $n_{\text{crit}}$  do not necessarily mean that the gas densities are above  $n_{\text{crit}}$ , because they can be sub-thermally excited.

Analysis on excitation conditions are needed.





## HerCULES sample

Full CO ladders (from  $J=1-0$  to  $13-12$ )

$^{13}\text{CO}$  ladders

Multiple molecules (HCN/HCO<sup>+</sup>/CS/etc.)

Multiple transitions ( $1-0, 2-1, \dots, 7-6$ )

The most complete dataset of dense gas tracers  
in nearby U/LIRGs

Manolis Xilouris

Ioanna Leonidaki

Padelis Papadopoulos

Paul van der Werf

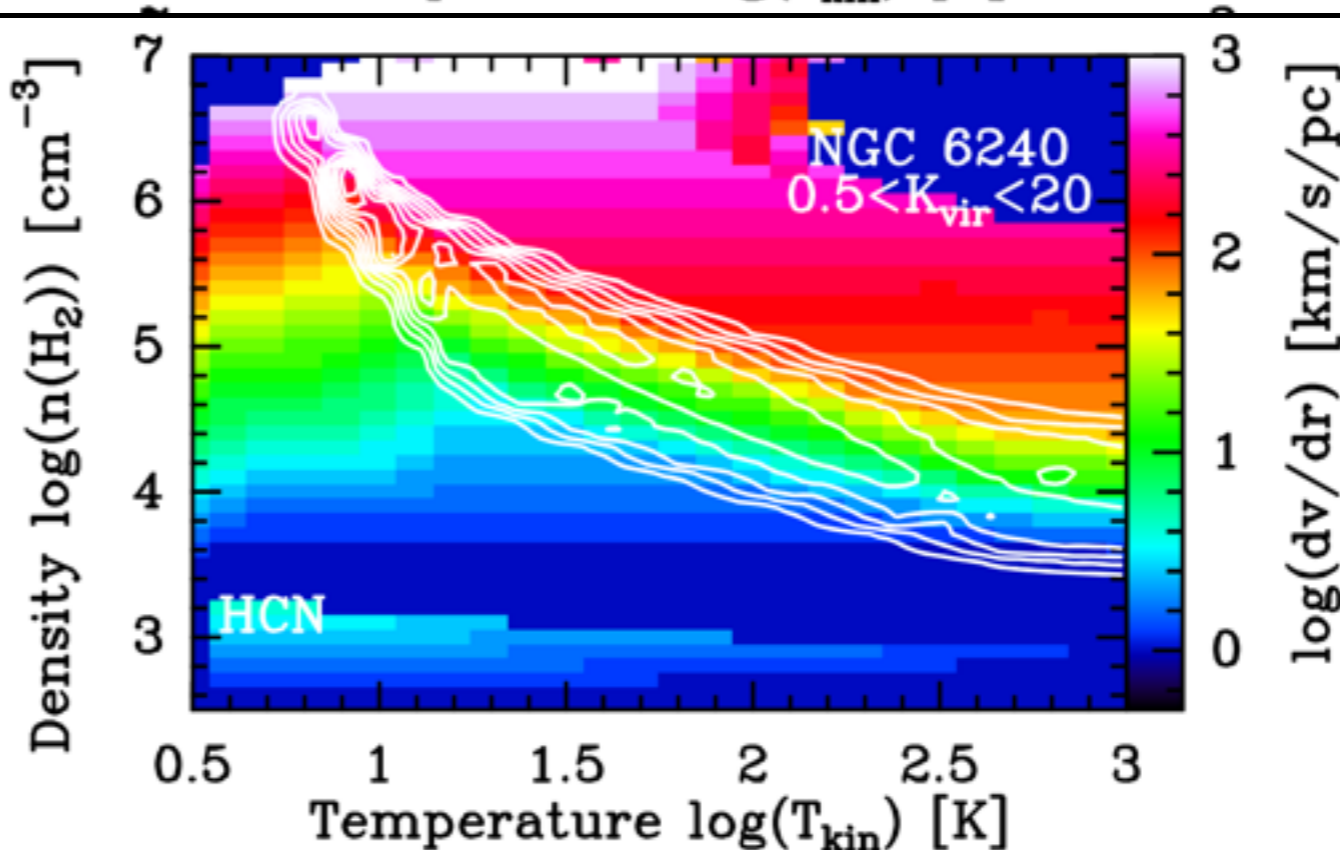
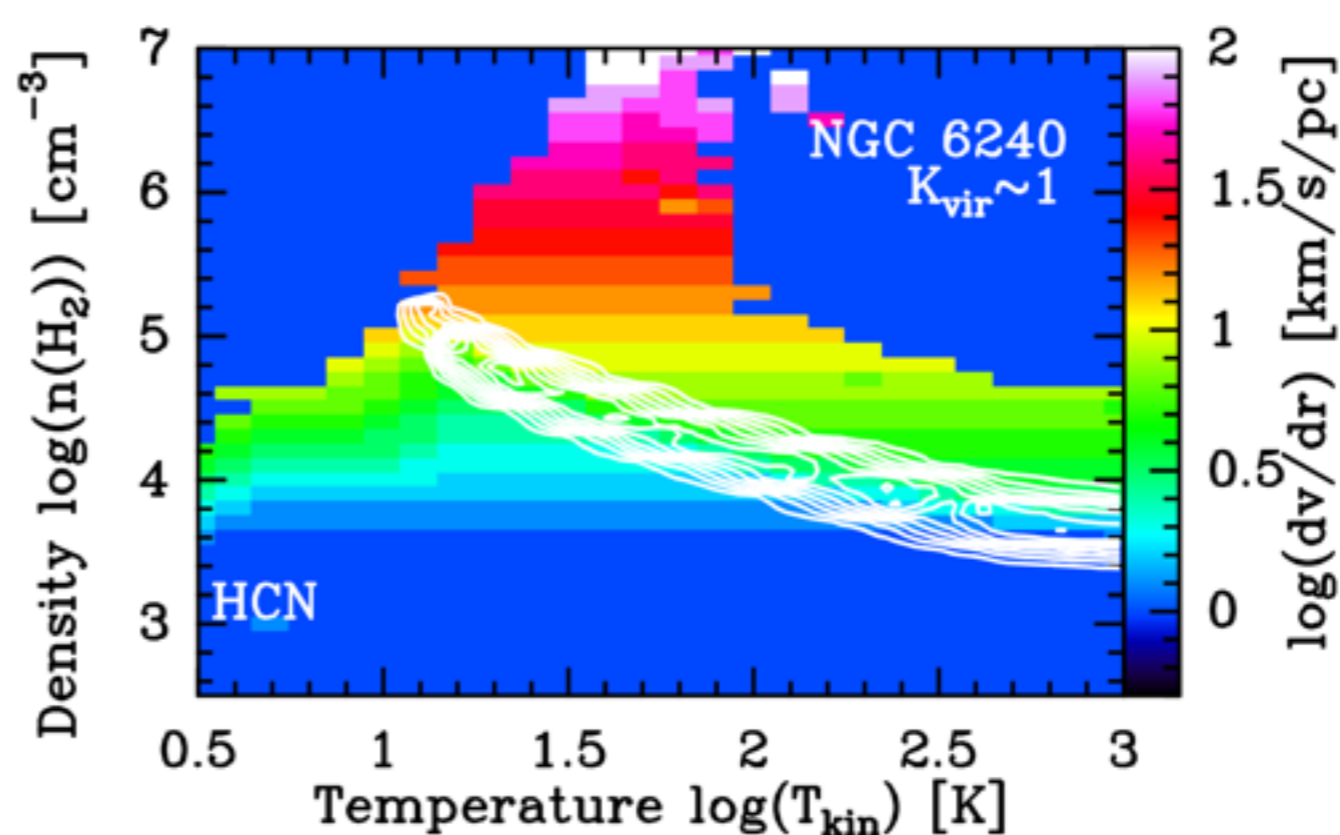
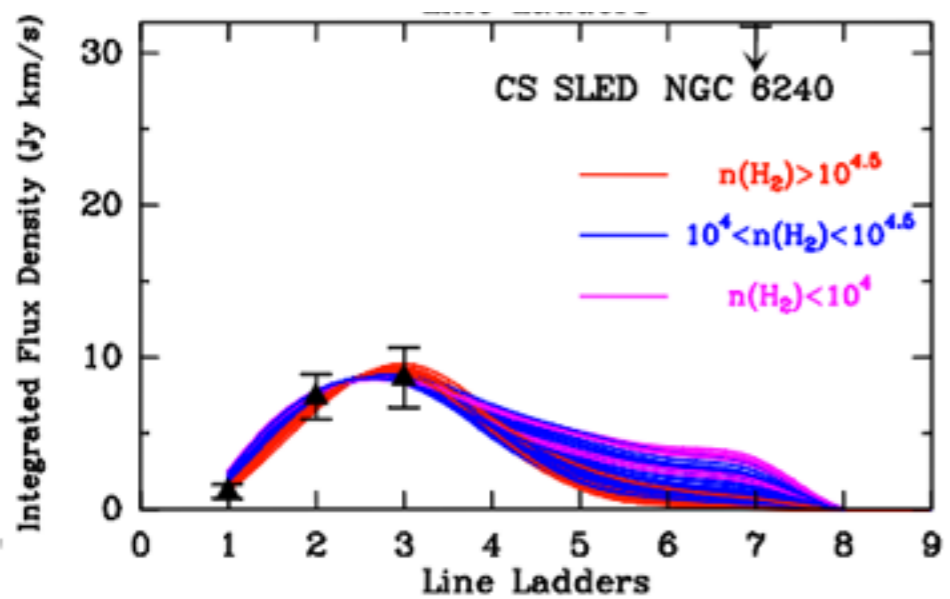
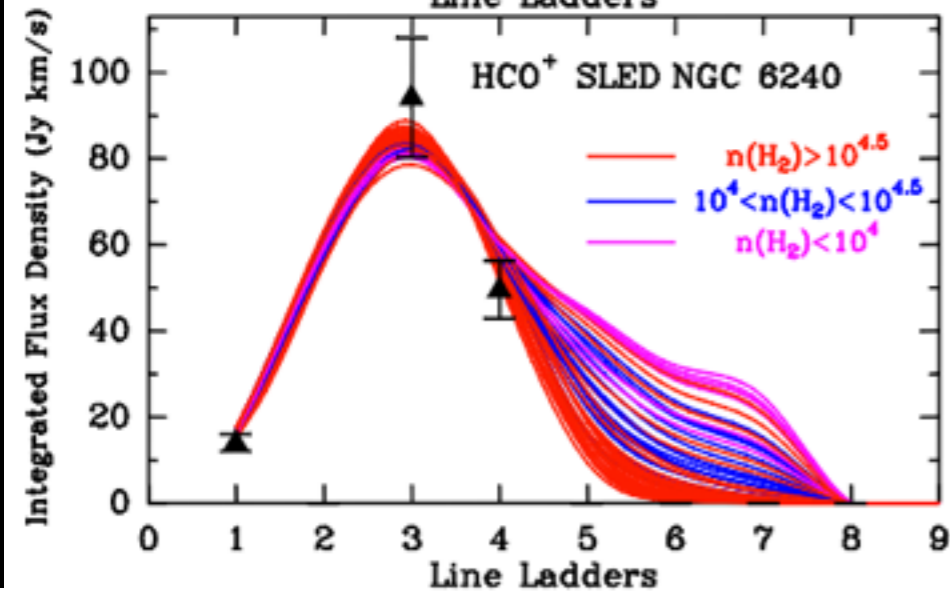
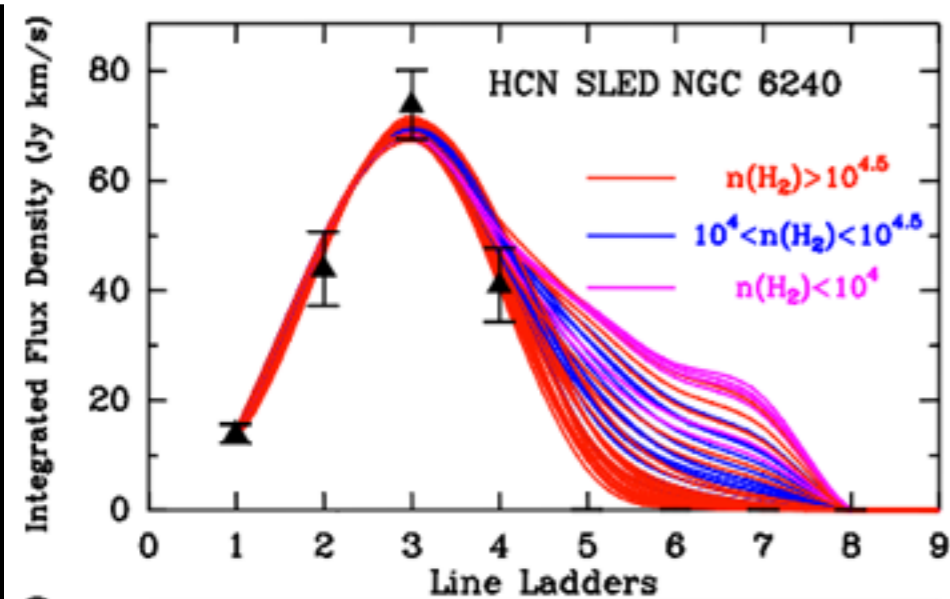
Thomas Greve

Zhi-Yu Zhang

Panos Boumis

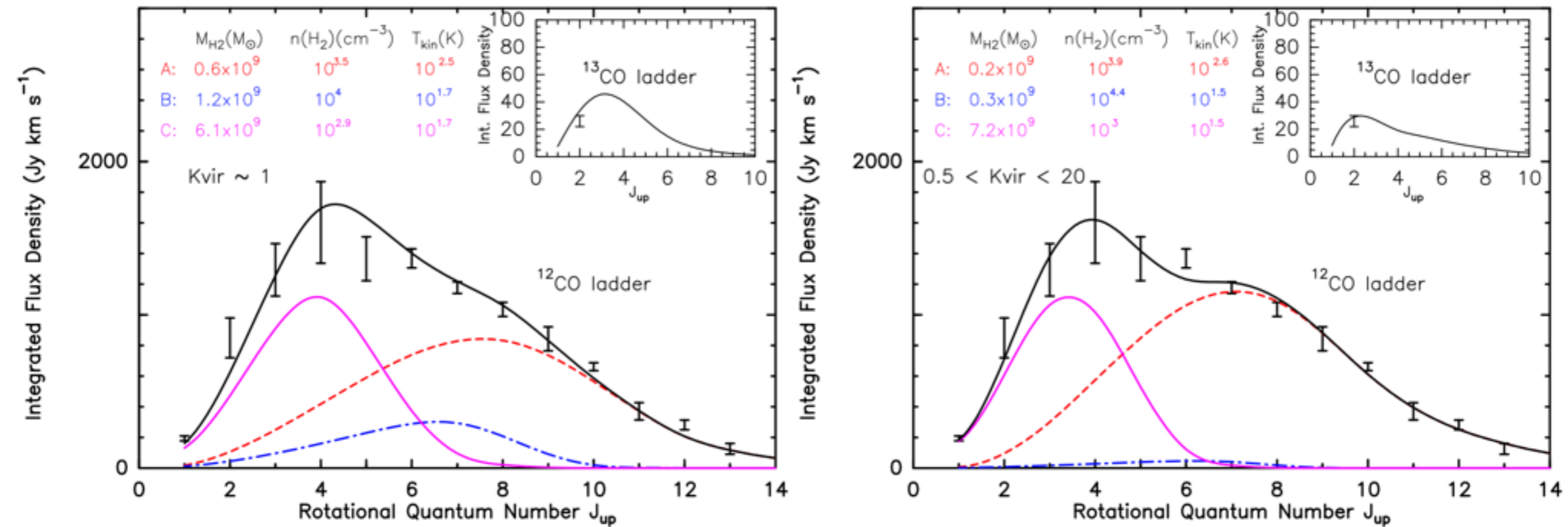
Alceste Bonanos

# LVG Modelling with HCN, HCO<sup>+</sup>, and CS



Papadopoulos  
+ 2014

# Model high-J CO using LVG results of HCN (NGC 6240)



~60-70% of the molecular gas is in dense gas phase.  
The thermal state of molecular gases can not be maintained by FUV from PDRs.

Detailed LVG analysis will be done for the whole sample.



# Take Home Messages

---

- 1) Dense molecular gases ( $n(\text{H}_2) \sim > 10^4 \text{ cm}^{-3}$ ) are forming stars.
- 2)  $M_{\text{dense}}$ -SFR linearly correlates.
- 3)  $M_{\text{dense}}$ -SFR stays universally linear from Galactic cores to galaxies.
- 4) More detailed modelings are on the way.

There are dense gas without SFR, and SFR without dense gas.  
Spatially resolved studies in external galaxies!

-- NOEMA/ALMA

Background music: broadcasting gymnastics for Chinese schools

**ALMA/NOEMA will be helpful!**

Thank you!

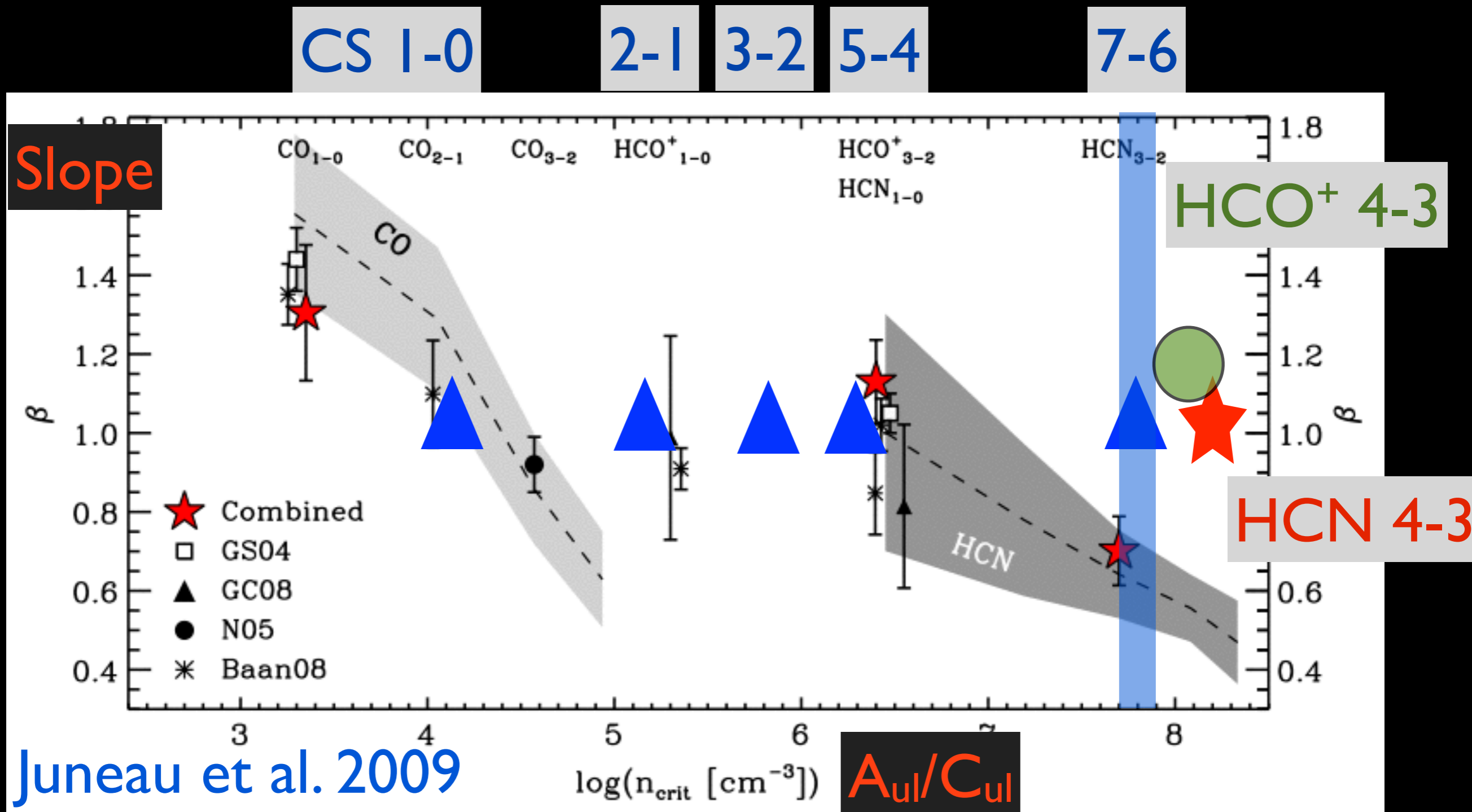




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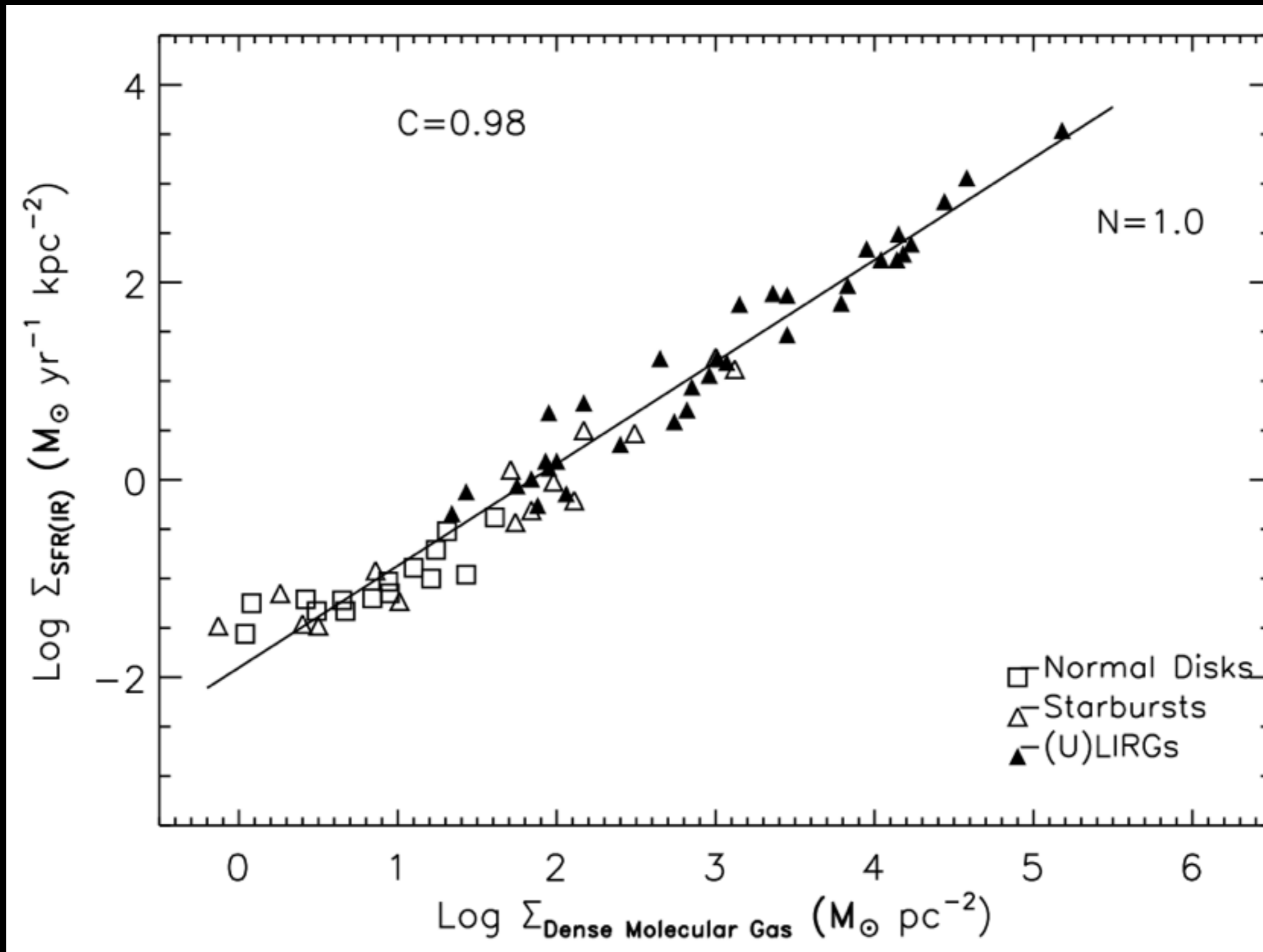
Backup Slides

# Dense gas tracers with $n_{\text{crit}} \sim 10^4 - 10^8 \text{ cm}^{-3}$

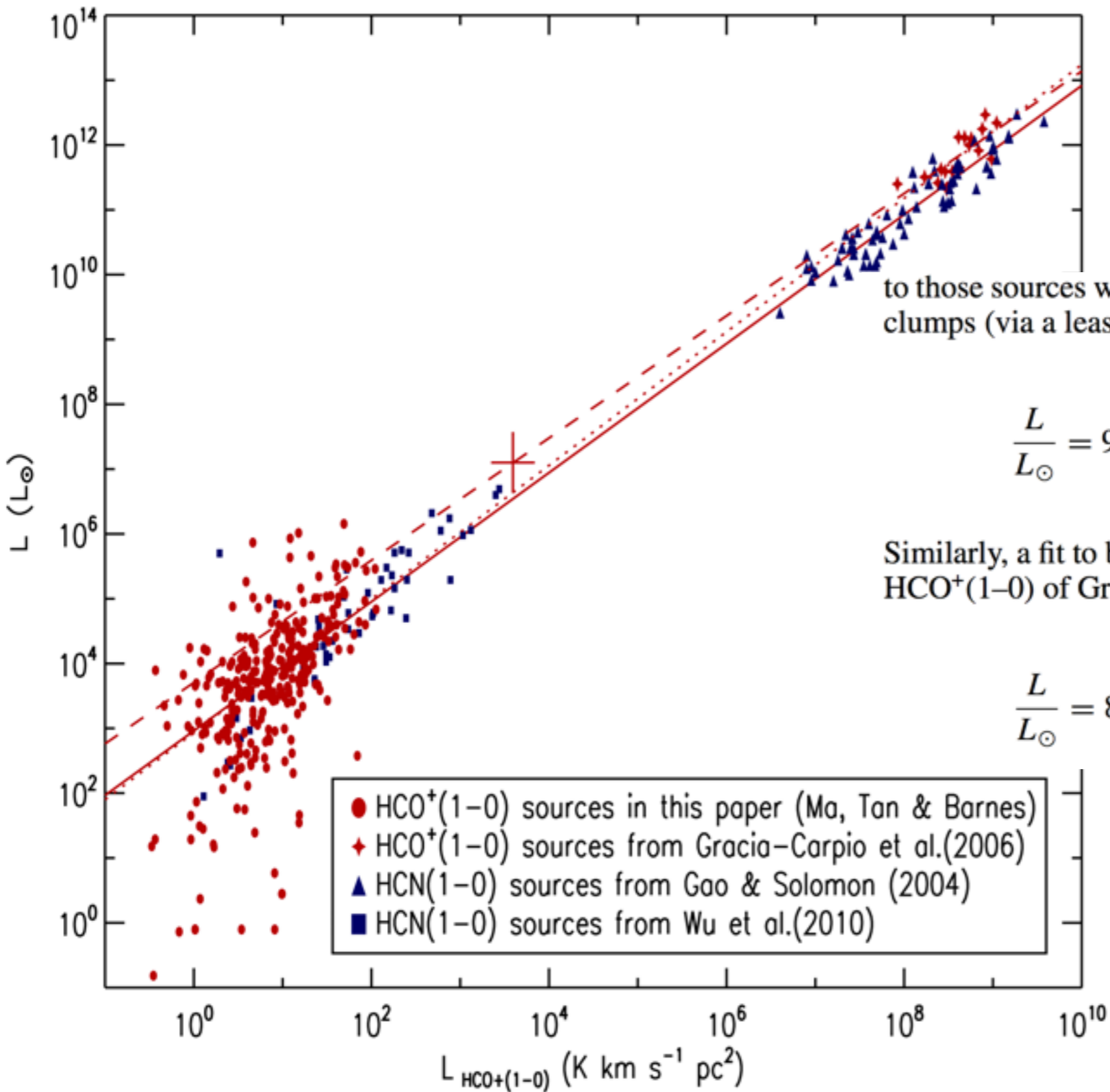


Dense gas tracers have linear correlations irrespective to  $n_{\text{crit}}$ , universally over 8 orders of luminosity magnitudes.

# Surface density correlation of HCN -10



# HCO<sup>+</sup> J=1-0



to those sources with  $L > 10^{1.5} L_{\odot}$ . Only fitting to the CHaMP clumps (via a least-squares fit in  $\log L$ ) yields

$$\frac{L}{L_{\odot}} = 917^{(+208)_{-170}} \left( \frac{L_{\text{HCO}^+(1-0)}}{\text{K km s}^{-1} \text{pc}^2} \right)^{1.00 \pm 0.09} \quad (41)$$

Similarly, a fit to both the CHaMP sample and the extragalactic HCO<sup>+</sup>(1-0) of Graciá-Carpio et al. (2006) yields

$$\frac{L}{L_{\odot}} = 857^{(+105)_{-93}} \left( \frac{L_{\text{HCO}^+(1-0)}}{\text{K km s}^{-1} \text{pc}^2} \right)^{1.03 \pm 0.02} \quad (42)$$

Ma et al. 2013

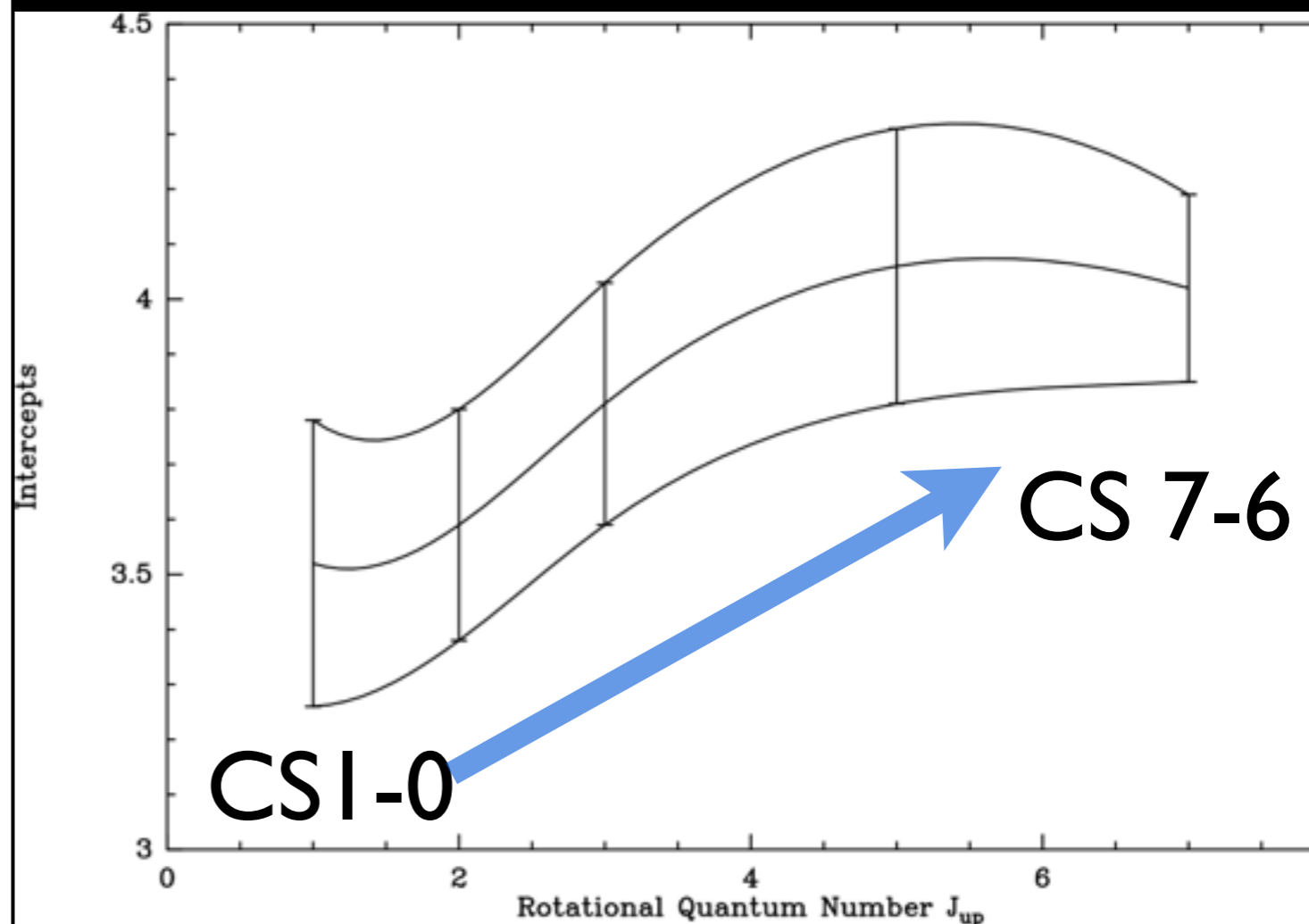


# Fitting results

Table 3.8: Fitting parameters of the correlations of  $L'_{CS}-L_{TR}$

Transition	Slope index	Intercepts	$r^a$	$s^b$
fitting without beam match correction				
CS $J=1 \rightarrow 0$	0.71(0.10)	5.99(0.76)	0.82	0.31
CS $J=2 \rightarrow 1$	0.88(0.05)	4.57(0.40)	0.94	0.24
CS $J=3 \rightarrow 2$	0.83(0.05)	5.17(0.34)	0.93	0.26
CS $J=5 \rightarrow 4$	0.69(0.06)	6.40(0.42)	0.91	0.25
CS $J=7 \rightarrow 6$	0.68(0.08)	6.60(0.56)	0.89	0.33
fitting with beam match correction				
CS $J=1 \rightarrow 0$	0.94(0.07)	3.96(0.52)	0.93	0.24
CS $J=2 \rightarrow 1$	1.20(0.06)	1.95(0.44)	0.96	0.27
CS $J=3 \rightarrow 2$	1.13(0.05)	2.80(0.34)	0.96	0.25
CS $J=5 \rightarrow 4$	0.99(0.06)	4.11(0.44)	0.96	0.24
CS $J=7 \rightarrow 6$	0.99(0.06)	4.06(0.43)	0.98	0.17
fitting with only point sources				
CS $J=1 \rightarrow 0$	0.95(0.09)	3.93(0.69)	0.90	0.26
CS $J=2 \rightarrow 1$	1.04(0.09)	3.30(0.72)	0.94	0.22
CS $J=3 \rightarrow 2$	1.02(0.09)	3.67(0.69)	0.92	0.22
CS $J=5 \rightarrow 4$	0.96(0.11)	4.33(0.80)	0.91	0.24

## Intercept vs. J

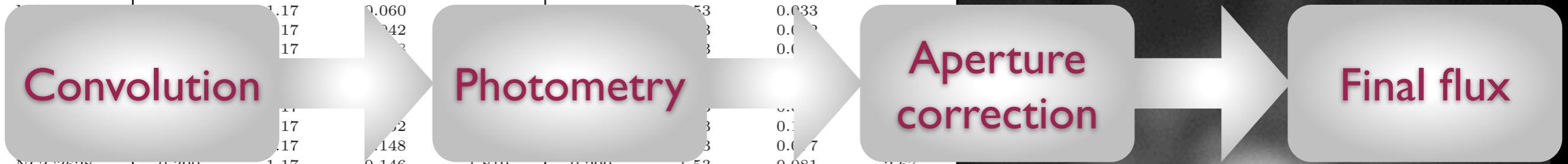


sub-linear slope indices for uncorrected targets  
 linear correlations for point targets and beam  
 matched targets

# Aperture Correction -- beams are small

3: Parameters of the photometry.

Source name	CS2-1 (25'')				CS 3-2 (17'')			
	24Ratio	24Apercor	70Ratio	70Apercor	24Ratio	24Apercor	70Ratio	70Apercor
NGC3628	0.390	1.17	0.146	1.819	0.299	1.53	0.081	2.67
NGC3079	0.068	1.17	0.182	1.819	0.052	1.53	0.103	2.67
NGC0520	0.763	1.17	0.359	1.819	0.600	1.53	0.206	2.67
NGC7479	0.697	1.17	0.228	1.819	0.550	1.53	0.134	2.67
NGC1530	1.	1.	1.	1.	1.	1.	1.	1.
NGC7771	0.465	1.17	0.201	1.819	0.364	1.53	0.110	2.67
NGC7469	1.	1.	1.	1.	1.	1.	1.	1.
NGC1614	1.	1.	1.	1.	1.	1.	1.	1.
NGC828	0.740	1.17	0.373	1.819	0.530	1.53	0.213	2.67
ARP193	1.	1.	1.	1.	1.	1.	1.	1.
UGC02369	1.	1.	1.	1.	1.	1.	1.	1.
NGC0695	1.	1.	1.	1.	1.	1.	1.	1.
IRAS10565	1.	1.	1.	1.	1.	1.	1.	1.
VIIZW31	1.	1.	1.	1.	1.	1.	1.	1.
IRAS23365	1.	1.	1.	1.	1.	1.	1.	1.



$$\text{Flux}_{\text{beam}} = F_{\text{total}} \times R_{\text{beam/total}} \times \text{Aper}_{\text{corr}}$$

50K blackbody PSF

The IR flux corresponding to CS beams are calculated with  $\text{Flux}_{\text{beam}} = \text{Flux}_{\text{gal}} \times R_{\text{beam/gal}} \times \text{Aper}$ , where  $\text{Flux}_{\text{beam}}$  is the IR flux with in the CS beam,  $\text{Flux}_{\text{gal}}$  is the IRAS flux of the total galaxies,  $R_{\text{beam/gal}}$  is the ratio of the flux inside CS beam to the flux of the whole galaxies measured in the Spitzer MIPS  $24\mu\text{m}$  or  $70\mu\text{m}$  images, and  $\text{Aper}$  is the aperture correction factor measured on the Spitzer MIPS PSF of a 50K blackbody for the corresponding beamsizes.

# Wu et al. 2010 Galactic CS

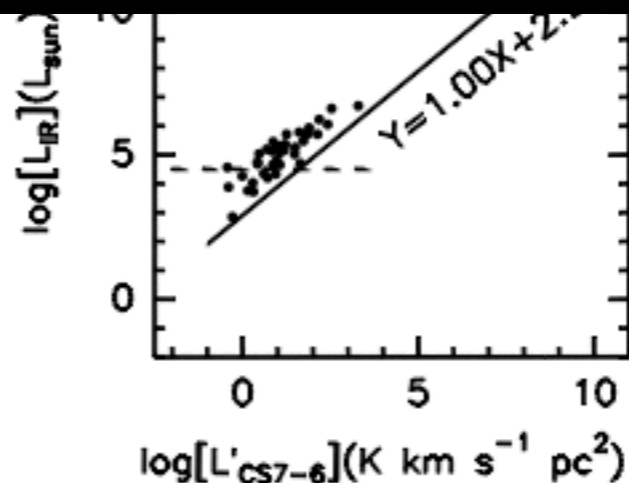
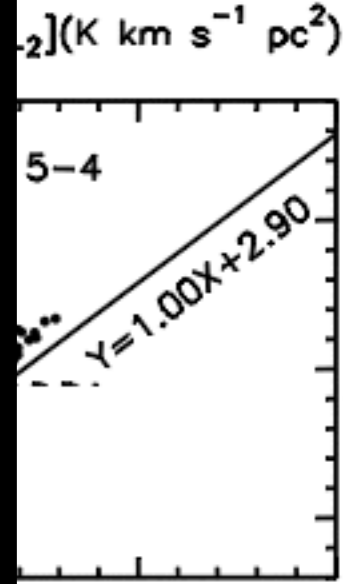
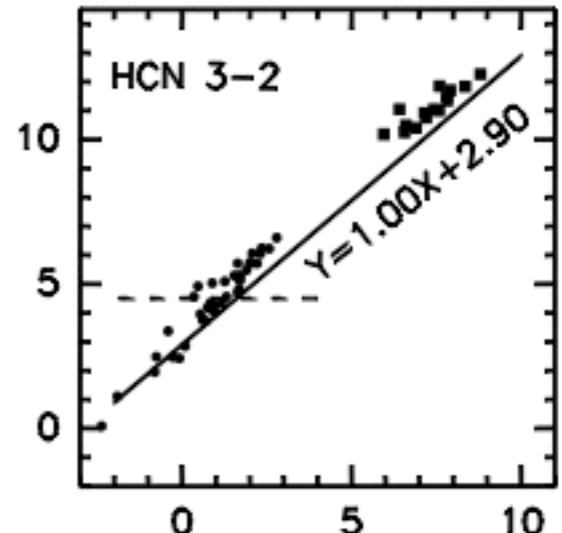
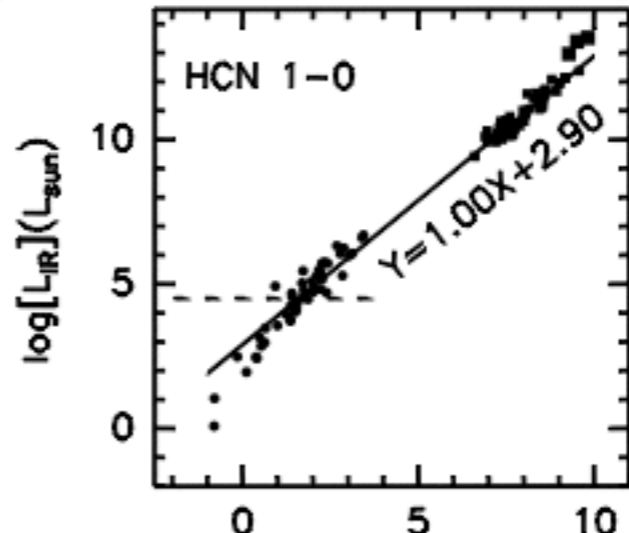
# HOW ARE GALAXIES?

CS 2-1:  
Least squares :  $\log(L_{\text{IR}}) = 1.03(\pm 0.05) \times \log(L'_{\text{CS}2-1}) + 3.25(\pm 0.11); r = 0.80$   
Robust fit :  $\log(L_{\text{IR}}) = 0.87 \times \log(L'_{\text{CS}2-1}) + 3.56$

CS 5-4:  
Least squares fit :  $\log(L_{\text{IR}}) = 1.03(\pm 0.05) \times \log(L'_{\text{CS}5-4}) + 3.25(\pm 0.11); r = 0.80$   
Robust fit :  $\log(L_{\text{IR}}) = 0.87 \times \log(L'_{\text{CS}5-4}) + 3.56$

CS 7-6:  
Least squares fit :  $\log(L_{\text{IR}}) = 1.03(\pm 0.05) \times \log(L'_{\text{CS}7-6}) + 3.25(\pm 0.11); r = 0.80$   
Robust fit :  $\log(L_{\text{IR}}) = 0.87 \times \log(L'_{\text{CS}7-6}) + 3.56$

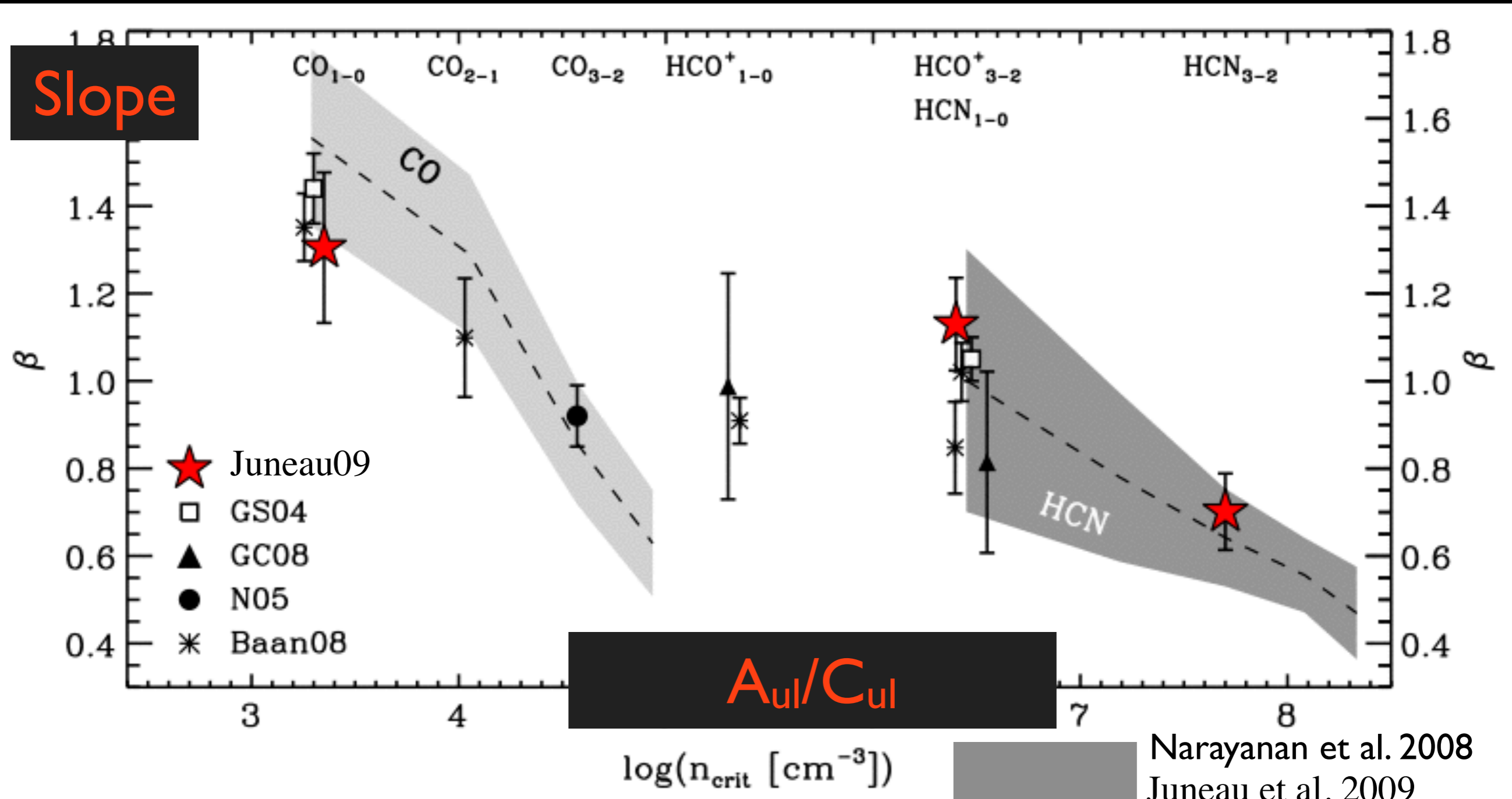
The average density of massive clumps (Kruschwitz et al. 1997), less than this study except for the effective density (Table 9) and the density that was found to contribute most to the HCN 1-0 line in the simulations of Krumholz & Thompson (2007). In fact, a density derived from excitation analysis is biased toward the densest regions and the mean density of the clumps in the sense of mass divided by volume is generally less (e.g., Shirley et al. 2003). As noted above, the relations we find do not support the suggestions by Krumholz & Thompson (2007) or Narayanan et al. (2008).





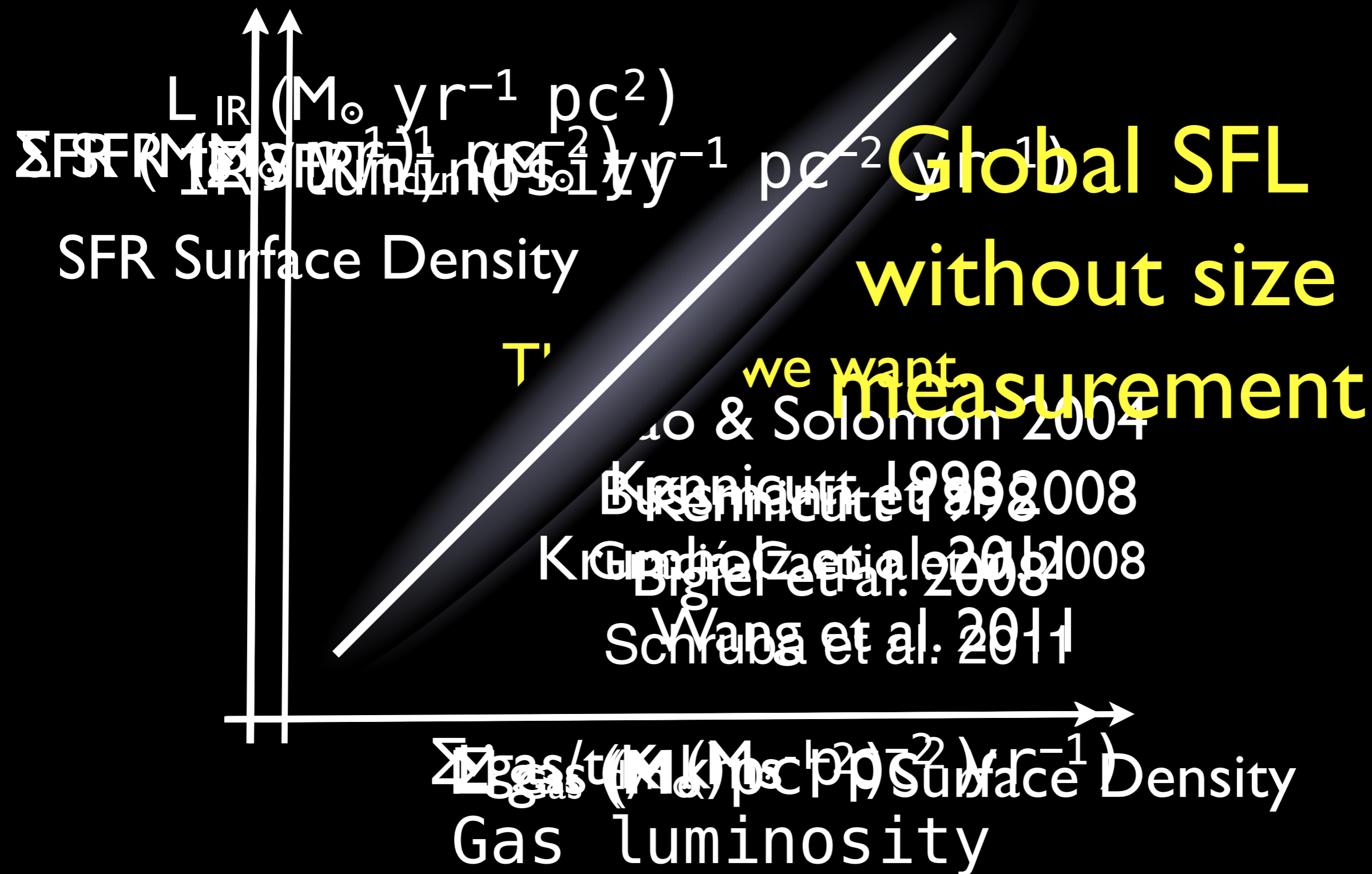
# Simulations vs. Observations

higher transitions/densities have lower slope indices.



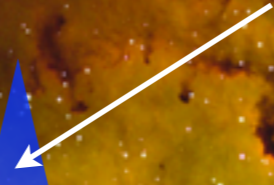


# Star Formation Law (Units)



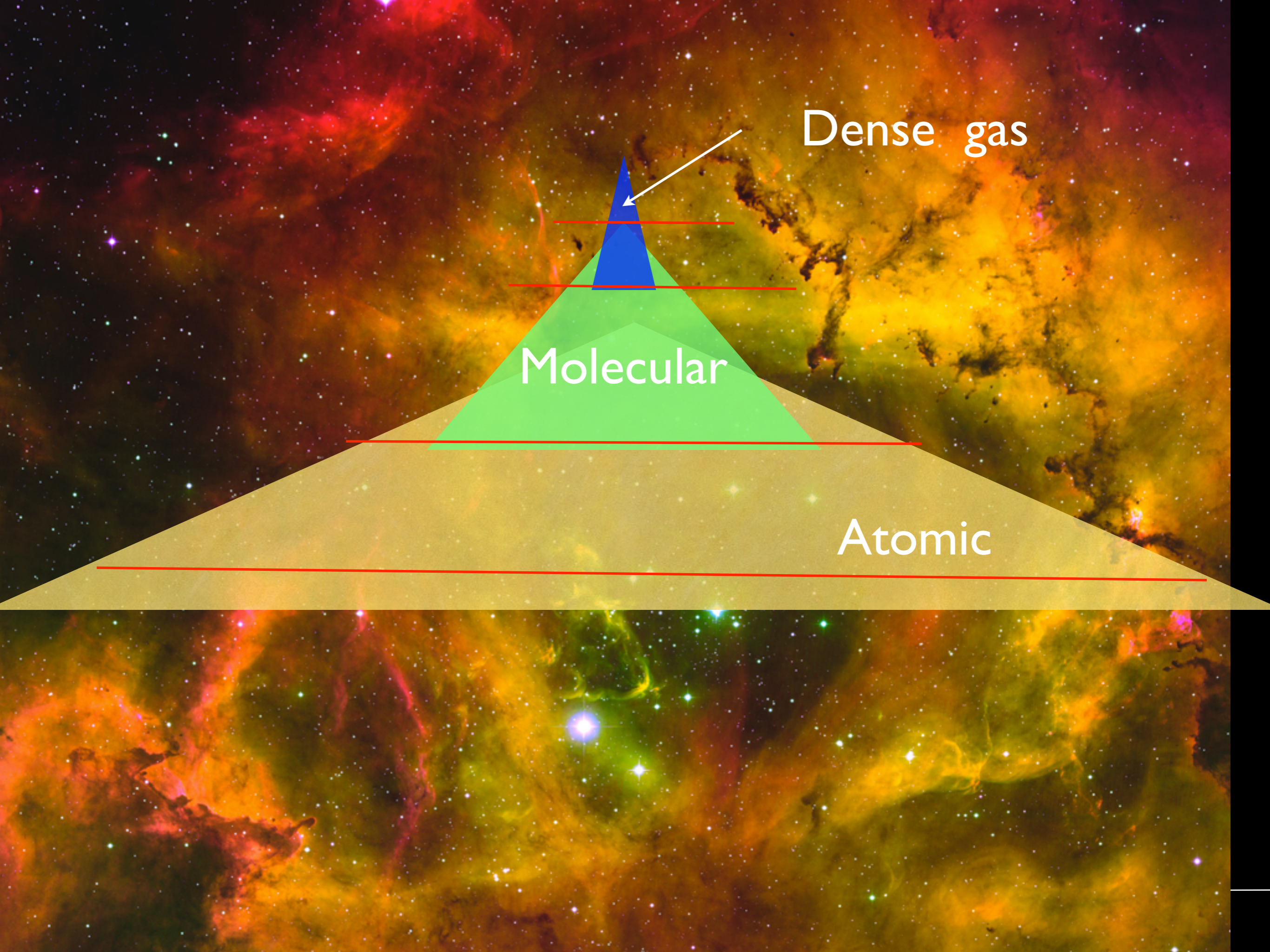


Dense gas



Molecular

Atomic

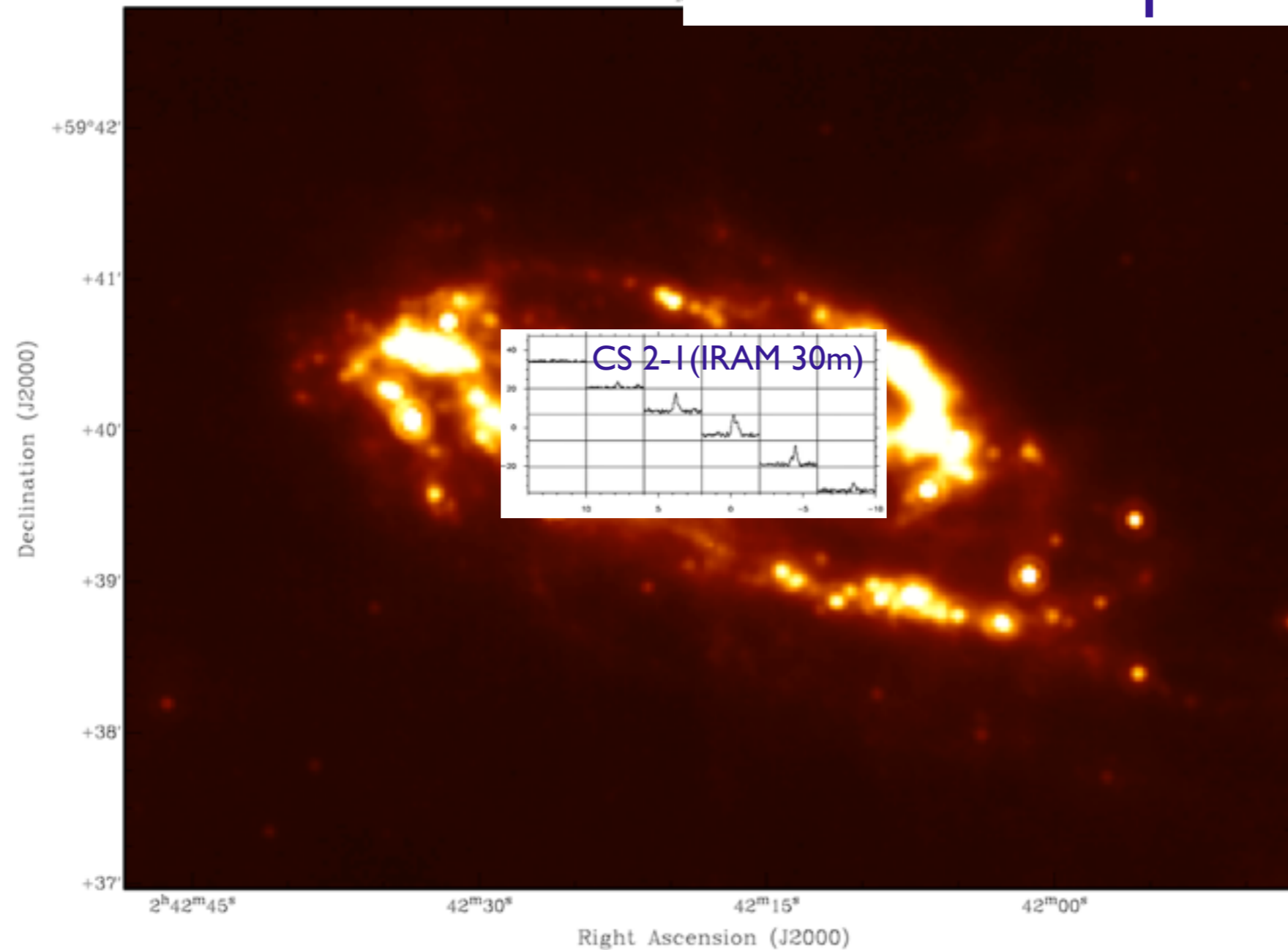




# Extended CS emission on the disk

MAFFEI 2

Spitzer 24  $\mu\text{m}$



# Dense gas tracers

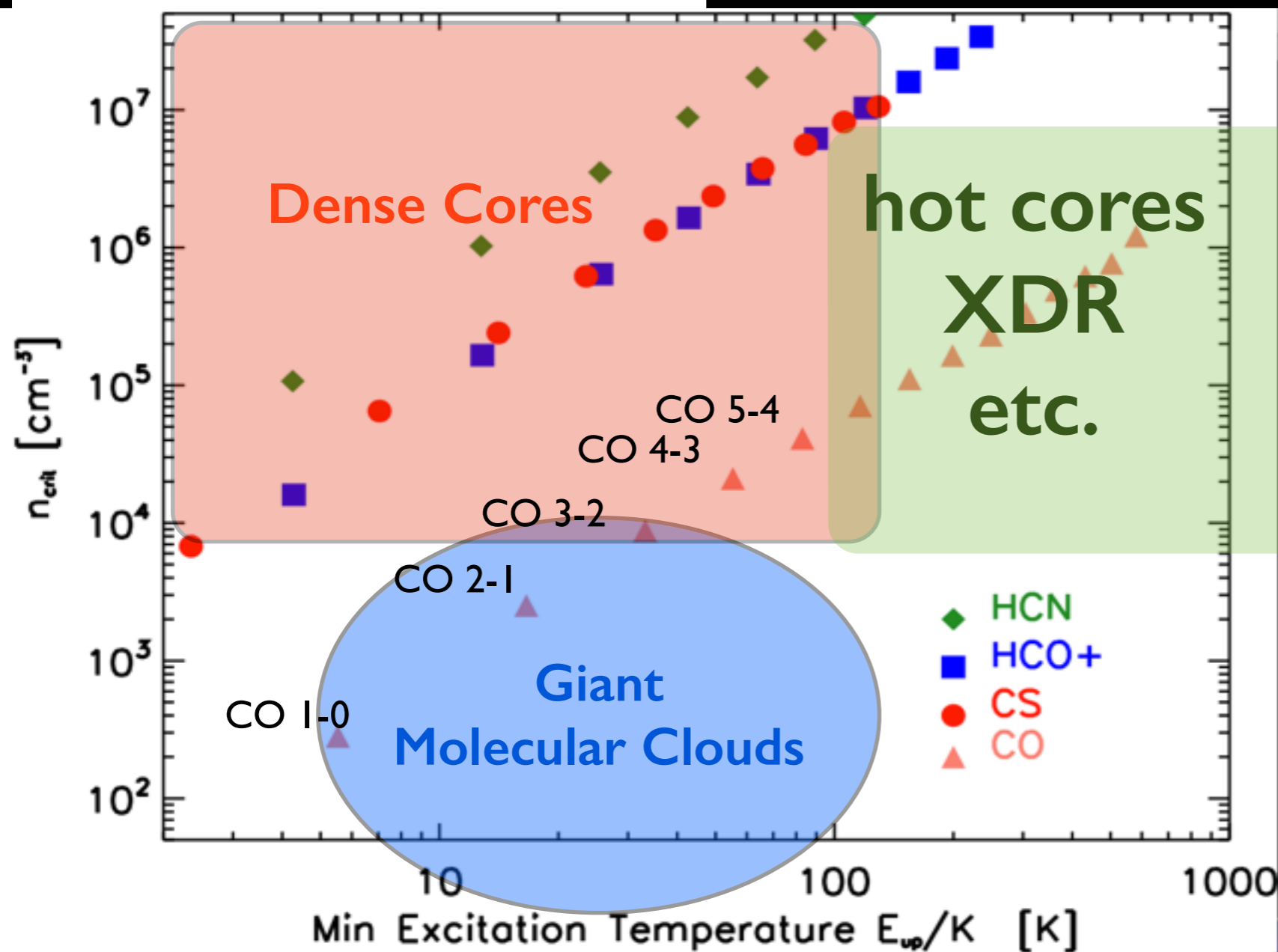
Critical Density:

$$n_{\text{crit}} = \frac{\sum_{l < u} A_{ul}}{\sum_{l \neq u} C_{ul}}$$

Rotational transitions of heavy molecules

**HCN, HCO+, CS, high-J CO** etc.

Dense gas tracer:  $n_{\text{crit}} > 10^4 \text{cm}^{-3}$



Except for abundance and excitation, molecular emissions can be influenced by:

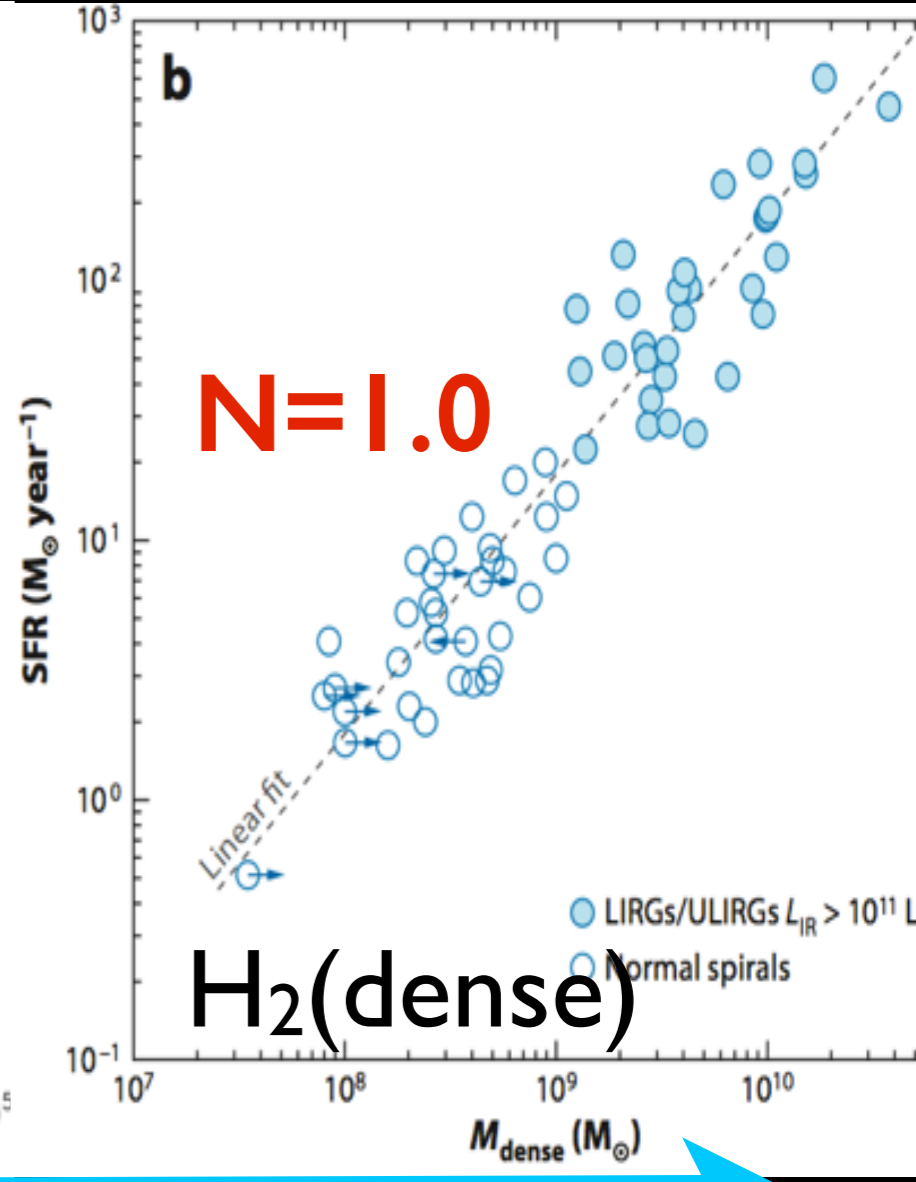
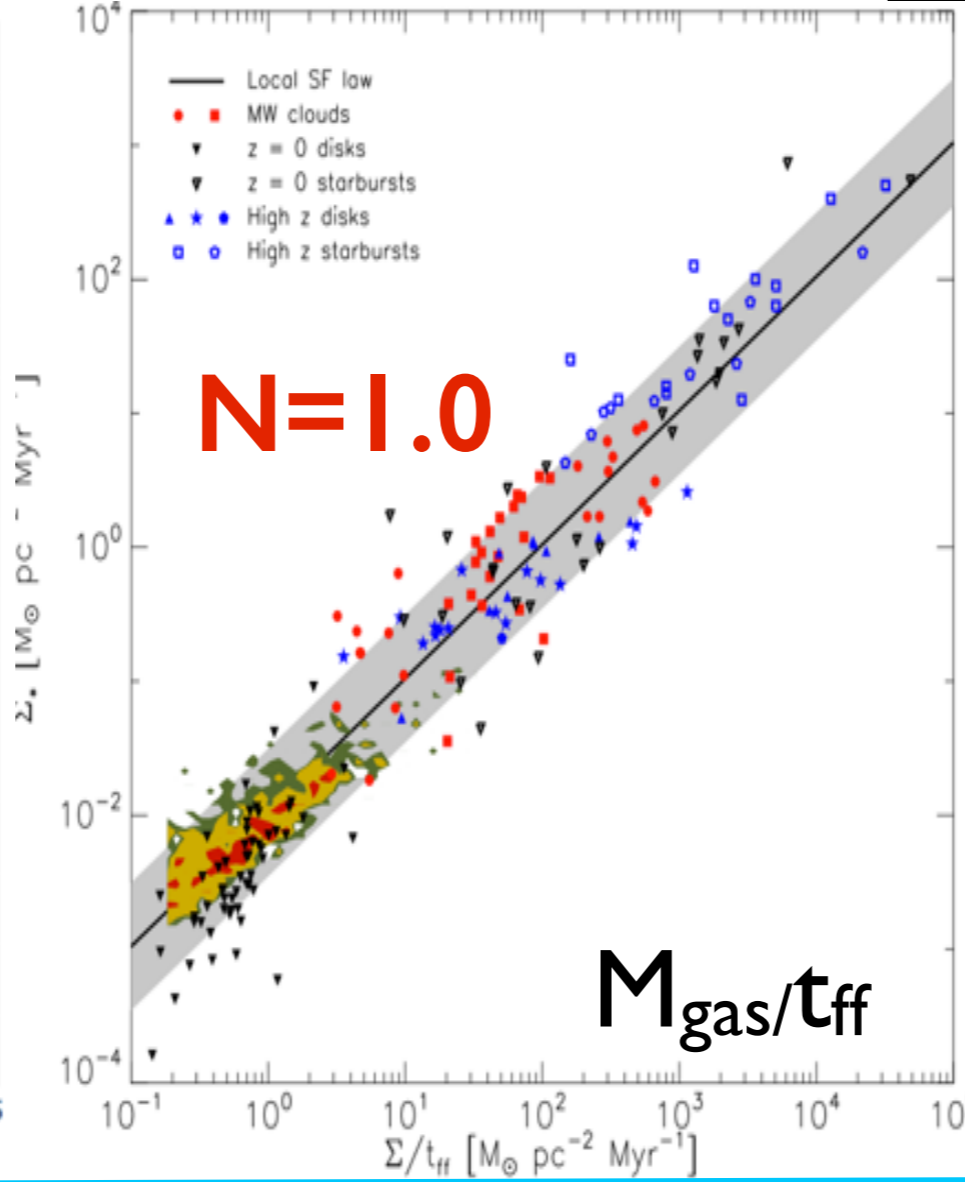
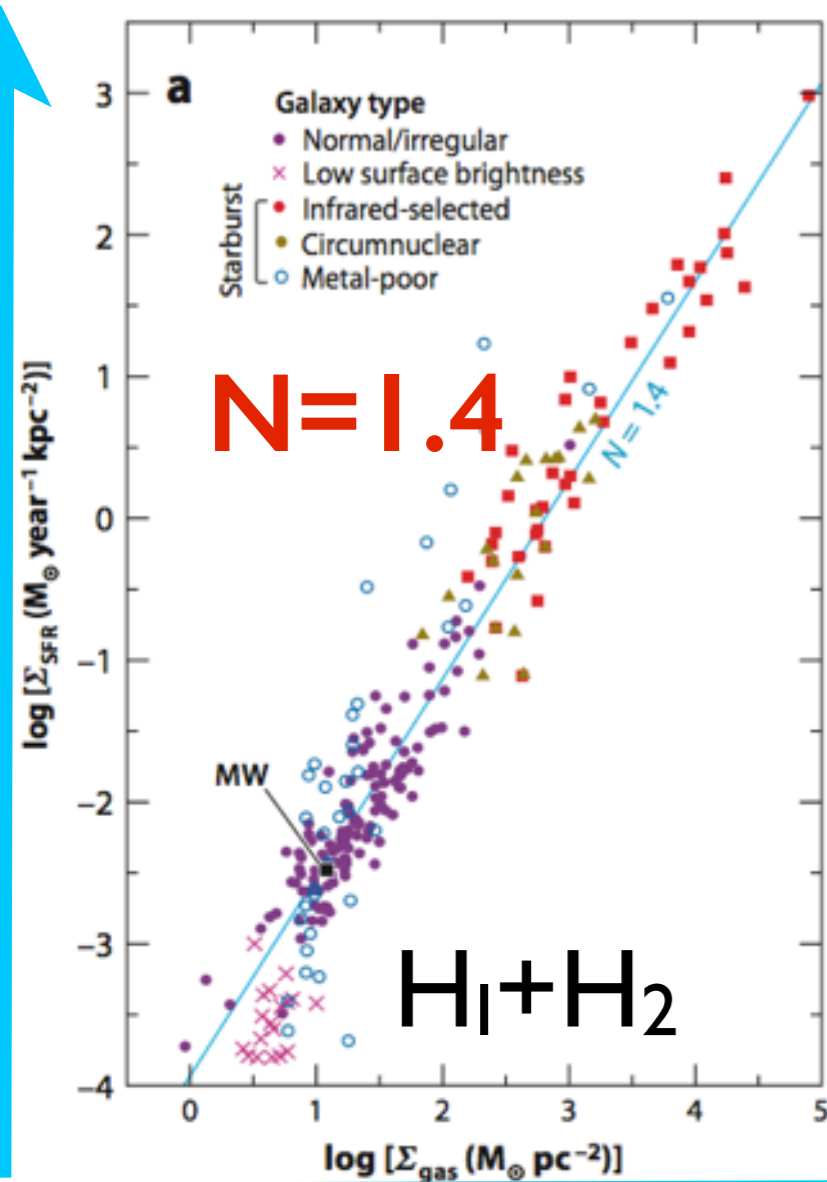
radiative pumping,  
chemistry,  
electron density,  
shock dissociation,  
etc.



Molecule	Transitions $J$	Frequency (GHz)	$E_{\text{upper}}$ (K)	$n_{\text{crit}}(100 \text{ K})$ ( $\text{cm}^{-3}$ )	$A_{\text{ul}}/\Gamma_{\text{ul}}(100 \text{ K})$ ( $\text{cm}^{-3}$ )	$n_{\text{crit}}(20 \text{ K})$ ( $\text{cm}^{-3}$ )	$A_{\text{ul}}/\Gamma_{\text{ul}}(20 \text{ K})$ ( $\text{cm}^{-3}$ )
CO	1→0	115.2711912	5.53	$2.1 \times 10^2$	$2.1 \times 10^3$	$4.4 \times 10^2$	$2.2 \times 10^3$
	2→1	230.5379938	16.60	$1.9 \times 10^3$	$2.2 \times 10^4$	$3.6 \times 10^3$	$2.3 \times 10^4$
	3→2	345.7959762	33.19	$6.8 \times 10^3$	$4.0 \times 10^4$	$1.3 \times 10^4$	$3.5 \times 10^4$
	4→3	461.0406784	55.32	$1.6 \times 10^4$	$6.1 \times 10^5$	$3.0 \times 10^4$	$1.2 \times 10^6$
	5→4	576.2679118	82.97	$3.2 \times 10^4$	$2.4 \times 10^5$	$5.9 \times 10^4$	$2.4 \times 10^5$
	6→5	691.4731878	116.16	$5.4 \times 10^4$	$3.1 \times 10^5$	$1.0 \times 10^5$	$2.7 \times 10^5$
	7→6	806.6514744	154.87	$8.6 \times 10^4$	$7.3 \times 10^5$	$1.5 \times 10^5$	$1.1 \times 10^6$
$^{13}\text{CO}$	1→0	110.20135428	5.29	$1.8 \times 10^2$	$1.8 \times 10^3$	$3.7 \times 10^2$	$1.9 \times 10^3$
	2→1	220.39868413	15.87	$1.7 \times 10^3$	$1.9 \times 10^4$	$3.1 \times 10^3$	$2.0 \times 10^4$
	3→2	330.58796522	31.73	$5.9 \times 10^3$	$3.5 \times 10^4$	$1.1 \times 10^4$	$3.4 \times 10^4$
$\text{C}^{18}\text{O}$	1→0	109.7821734	5.27	$1.8 \times 10^2$	$1.9 \times 10^3$	$3.7 \times 10^2$	$1.9 \times 10^3$
	2→1	219.5603541	15.81	$1.7 \times 10^3$	$2.0 \times 10^4$	$3.1 \times 10^3$	$1.9 \times 10^4$
	3→2	329.3305525	31.61	$5.9 \times 10^3$	$3.0 \times 10^4$	$1.1 \times 10^4$	$3.4 \times 10^4$
$\text{HCO}^+$	1→0	89.1885230	4.28	$1.4 \times 10^4$	$2.3 \times 10^5$	$2.6 \times 10^4$	$1.8 \times 10^5$
	2→1	178.3750650	12.84	$1.4 \times 10^5$	$4.6 \times 10^6$	$2.6 \times 10^5$	$3.4 \times 10^6$
	3→2	267.5576190	25.68	$5.2 \times 10^6$	$4.2 \times 10^6$	$1.0 \times 10^6$	$4.0 \times 10^6$
	4→3	356.7342880	42.80	$1.3 \times 10^6$	$5.8 \times 10^7$	$2.5 \times 10^6$	$4.0 \times 10^7$
CS	1→0	48.9909549	2.35	$5.5 \times 10^3$	$6.2 \times 10^4$	$8.3 \times 10^3$	$4.7 \times 10^4$
	2→1	97.9809533	7.05	$5.3 \times 10^4$	$5.2 \times 10^5$	$7.9 \times 10^4$	$6.0 \times 10^5$
	3→2	146.9690287	14.11	$1.9 \times 10^5$	$1.4 \times 10^6$	$3.0 \times 10^5$	$1.1 \times 10^6$
	4→3	195.9542109	23.51	$4.8 \times 10^5$	$2.7 \times 10^6$	$7.7 \times 10^5$	$3.3 \times 10^7$
	5→4	244.9355565	35.27	$9.9 \times 10^5$	$6.1 \times 10^6$	$1.8 \times 10^6$	$7.5 \times 10^6$
	6→5	293.9120865	49.37	$1.7 \times 10^6$	$1.2 \times 10^7$	$3.1 \times 10^6$	$1.1 \times 10^7$
	7→6	342.8828503	65.83	$2.8 \times 10^6$	$1.8 \times 10^8$	$4.9 \times 10^6$	$2.8 \times 10^8$

# SFR

# Gas - SFR relations

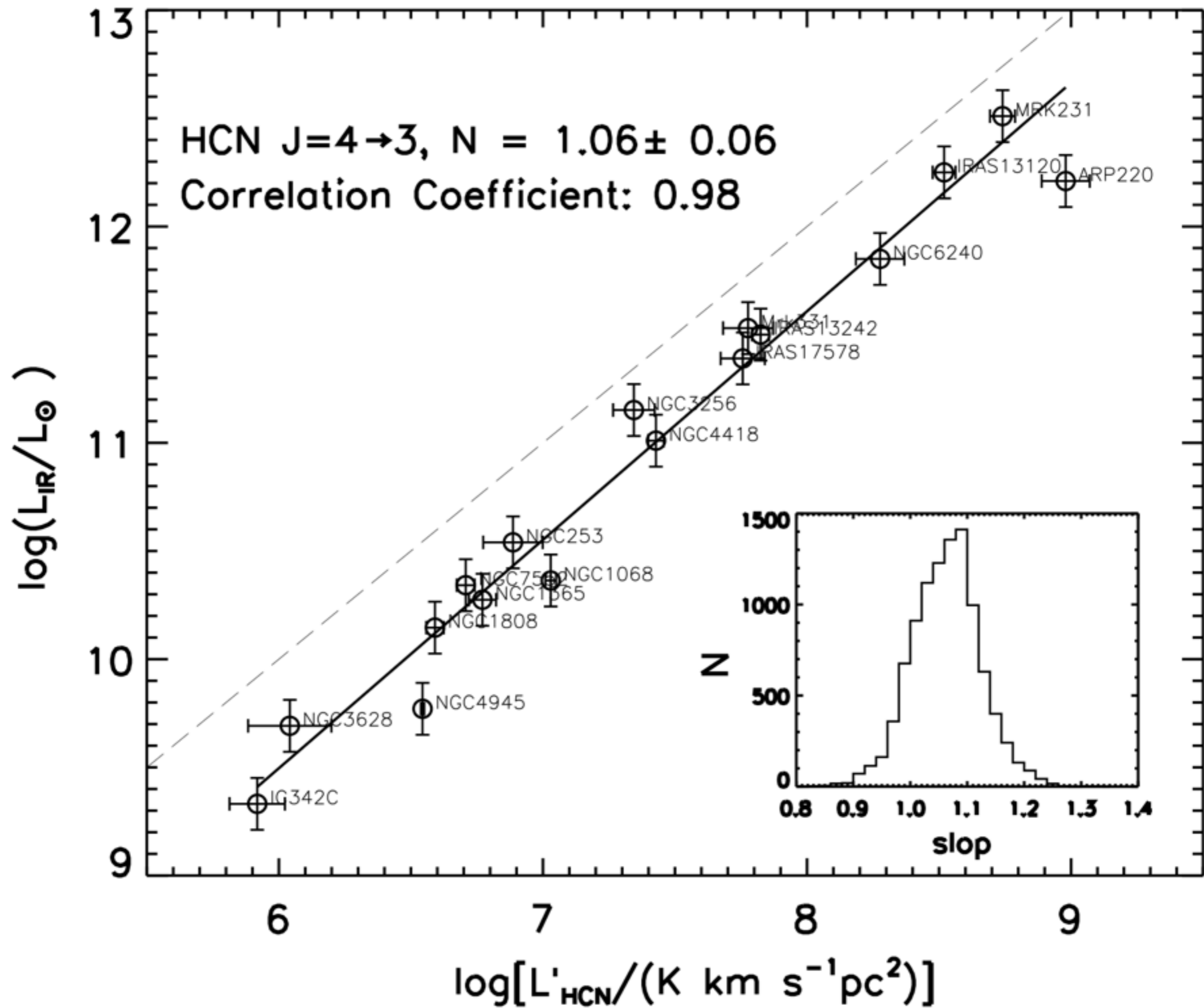


# Gas Mass

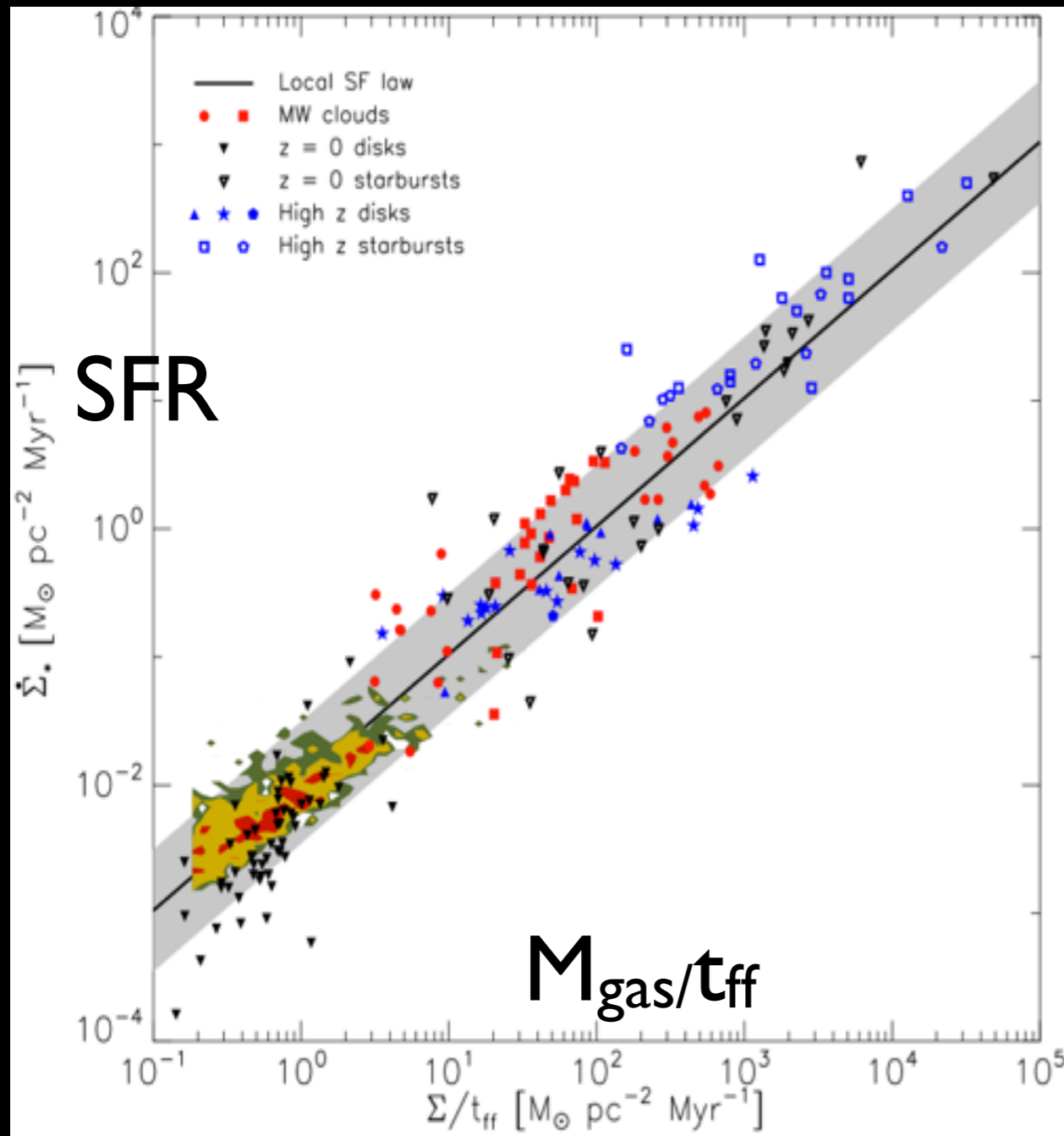
Kennicutt 1998

Krumholz et al. 2012

Gao & Solomon 2004



# Does time scales matter? -- For Dense gas: No.



$$\dot{\rho}_* = f_{\text{H}_2} \epsilon_{\text{ff}} \frac{\rho}{t_{\text{ff}}} = f_{\text{H}_2} \epsilon_{\text{ff}} \sqrt{\frac{32G\rho^3}{3\pi}}$$

Krumholz et al. 2012

$f_{\text{H}_2}$  : H<sub>2</sub> fraction

$\epsilon_{\text{ff}}$  : constant, dimensionless measure of SFR

$$t_{\text{ff}} \propto \rho^{-1/2}$$

If  $L_{\text{IR}} = (L'_{\text{dense}})^N / t_{\text{ff}}$ , N will decrease with  $n_{\text{crit}}$ .

This will be contradictory to our observed results.



# HCO<sup>+</sup> deficient in extreme conditions??

---

Higher slopes for HCO<sup>+</sup> (only) in galaxies.

Gracia-Carpio et al. 2006, 2008; Imanishi et al. 2007

Linear in Galactic cores, e.g., Ma et al. 2013

HCO<sup>+</sup> is an **ionic molecule**.



High radiation fields in ULIRGs

X-ray / Cosmic Rays => high n(e)

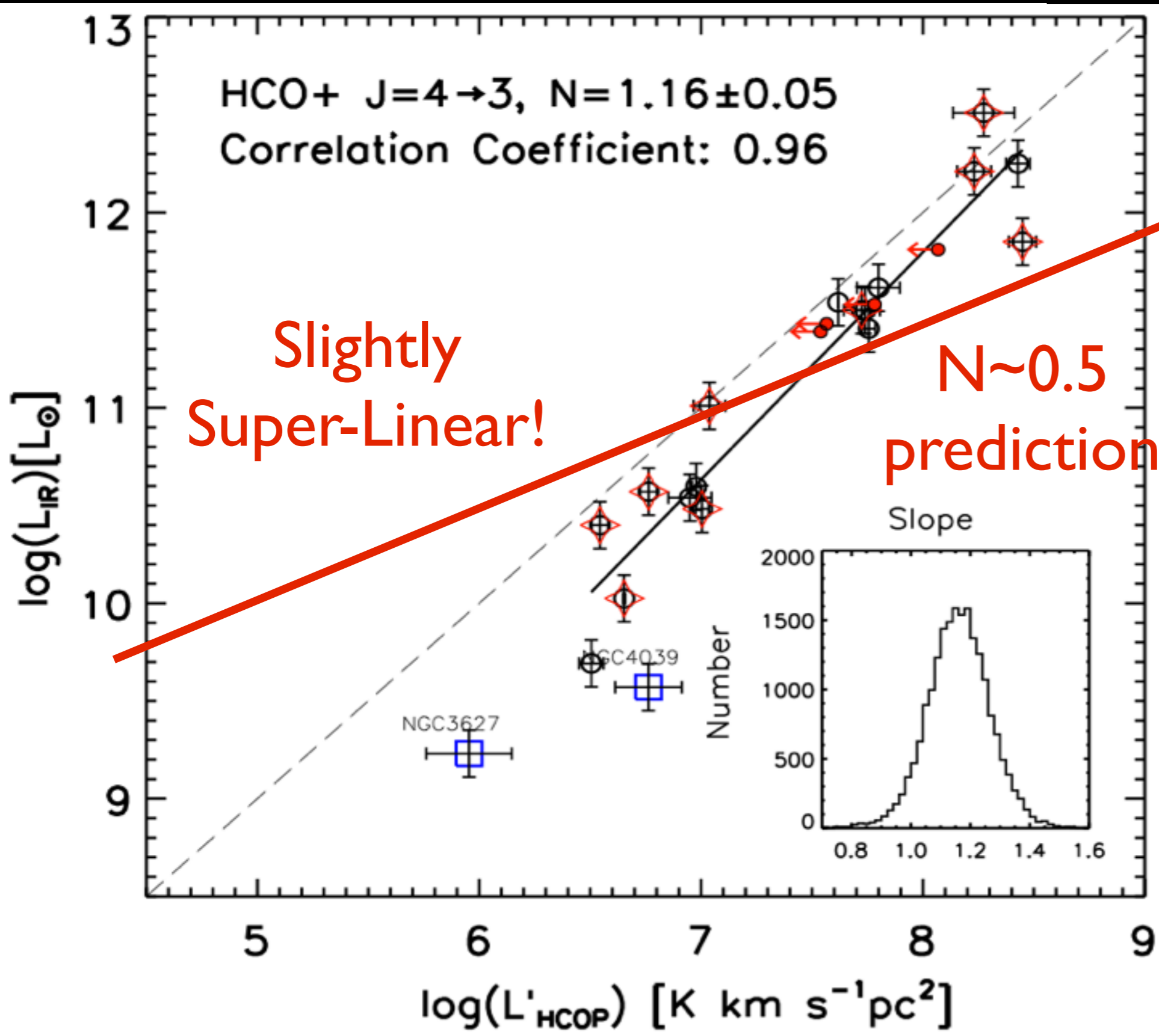
Papadopoulos et al. 2007

Shock environment

Shocks produce electron-rich outer layers

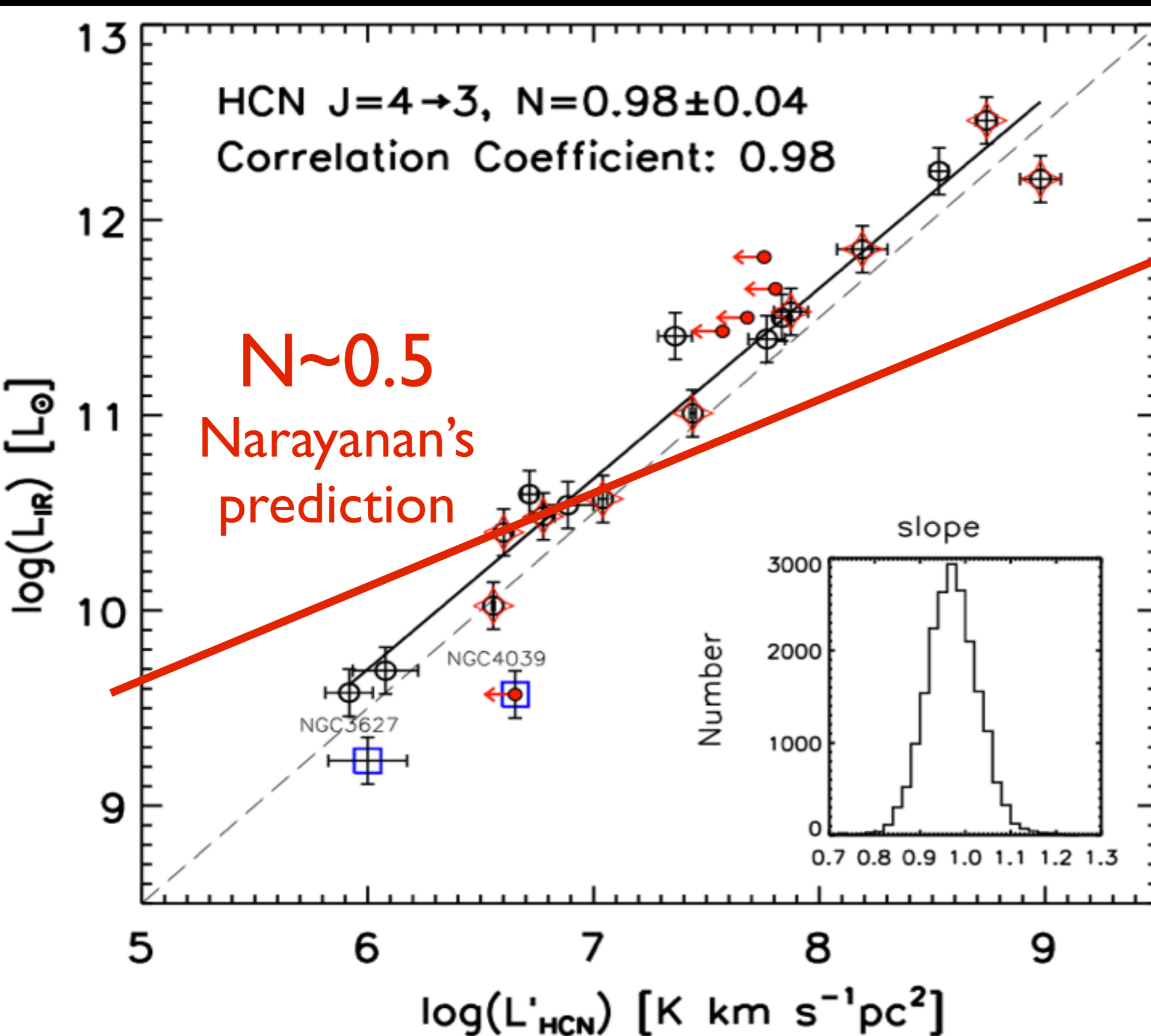
Xie et al. 1995

# HCO<sup>+</sup> J=4-3 -- observed simultaneously with CS J=7-6



$n_{\text{crit}} \sim 2 \times 10^6 \text{ cm}^{-3}$

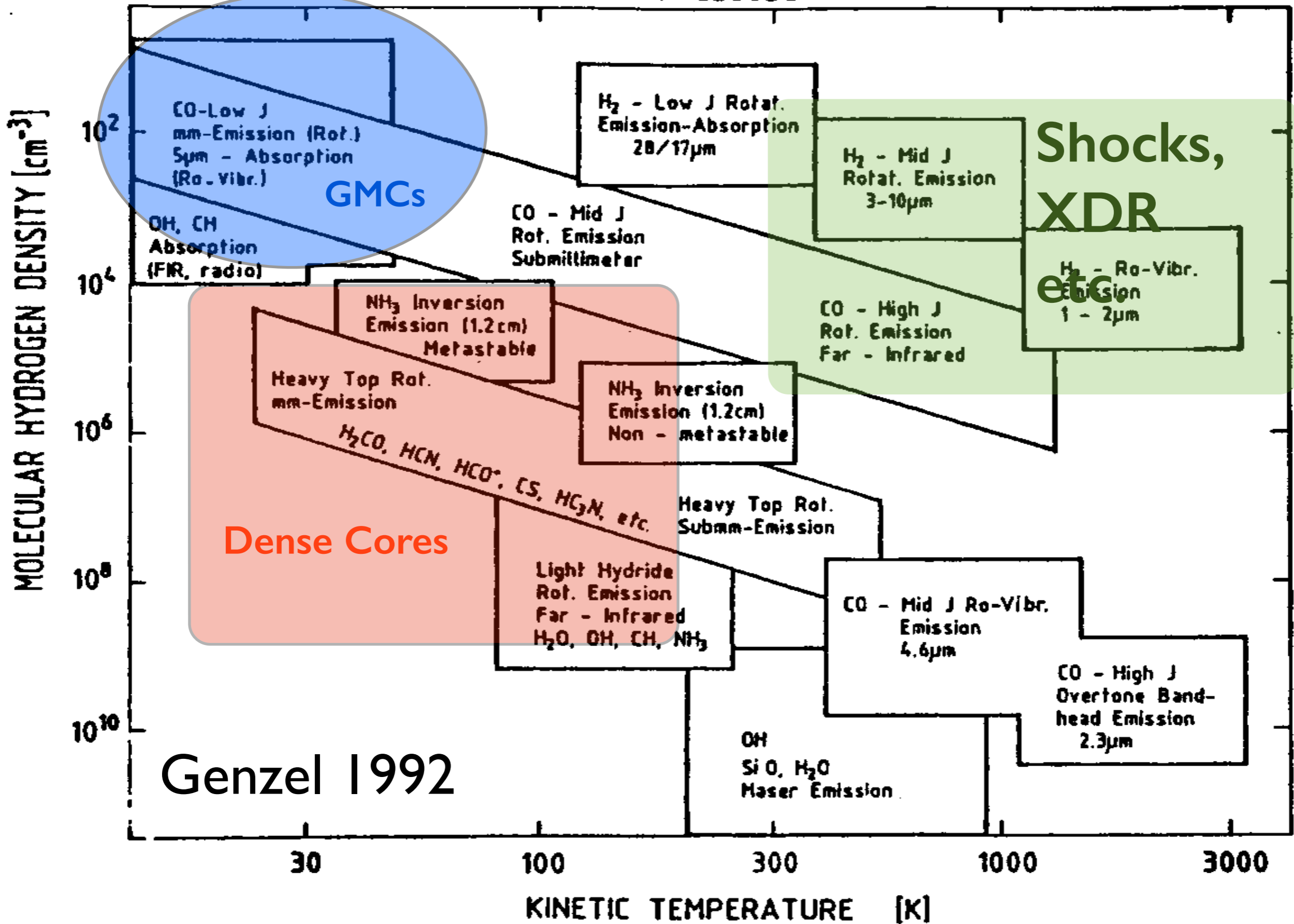
# HCN J=4-3 -- the highest $n_{\text{crit}}$ tracer



$$n_{\text{crit}} \sim 1 \times 10^7 \text{ cm}^{-3}$$

# Tracers of Physical Conditions in Molecular Clouds

INFRARED AND MICROWAVE MOLECULAR LINES AS PROBES OF PHYSICAL CONDITIONS IN MOLECULAR CLOUDS





# Why slopes matter?

Different SFE

## Which gases are forming stars?

